

# Inflation, Tuning and Measures

Andreas Albrecht; UC Davis  
Cosmocruise Sep 5 2015

Infl and Measures

THANKS!

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Infl... d I

**THANKS!**



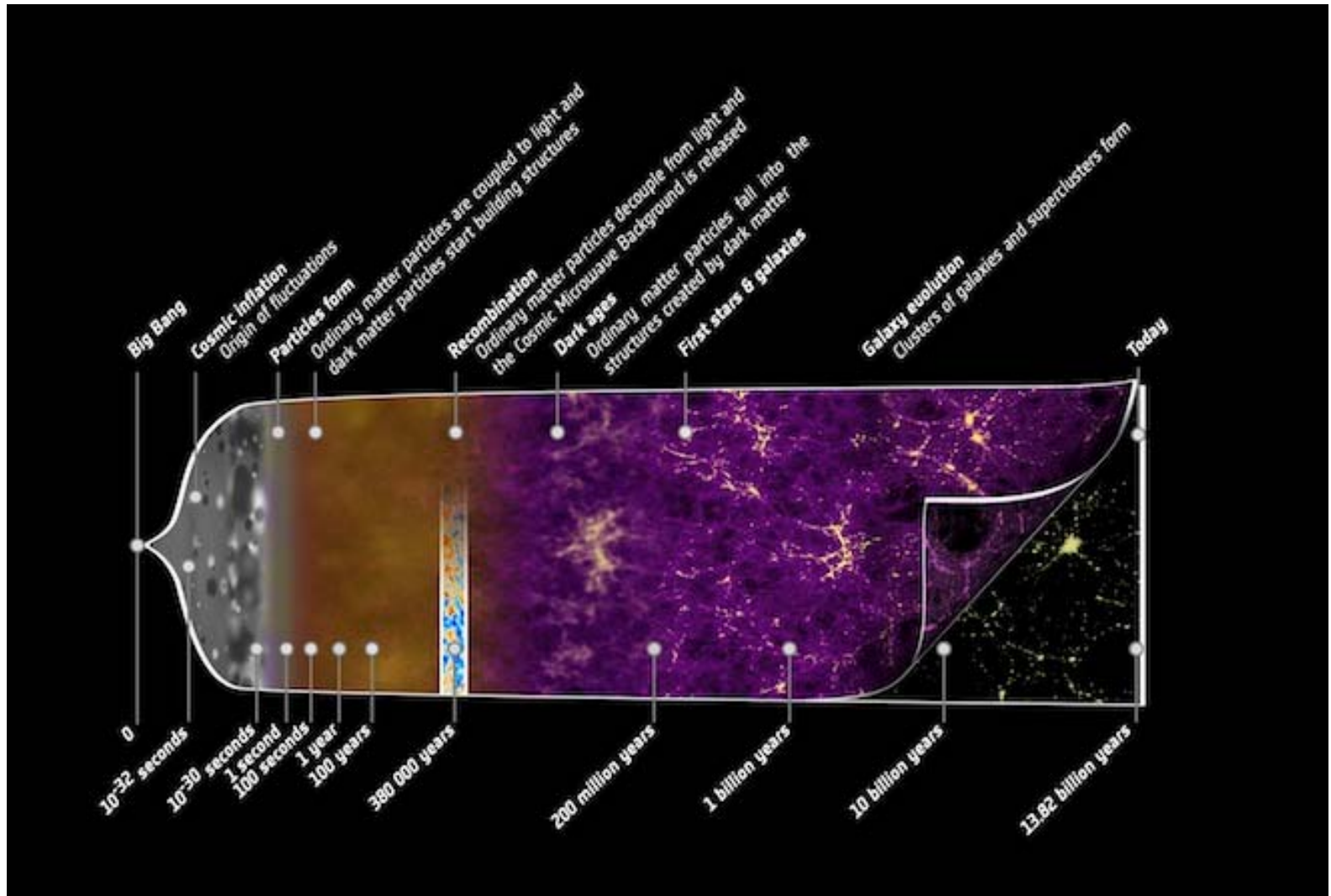
Andreas Albrecht; UC Davis  
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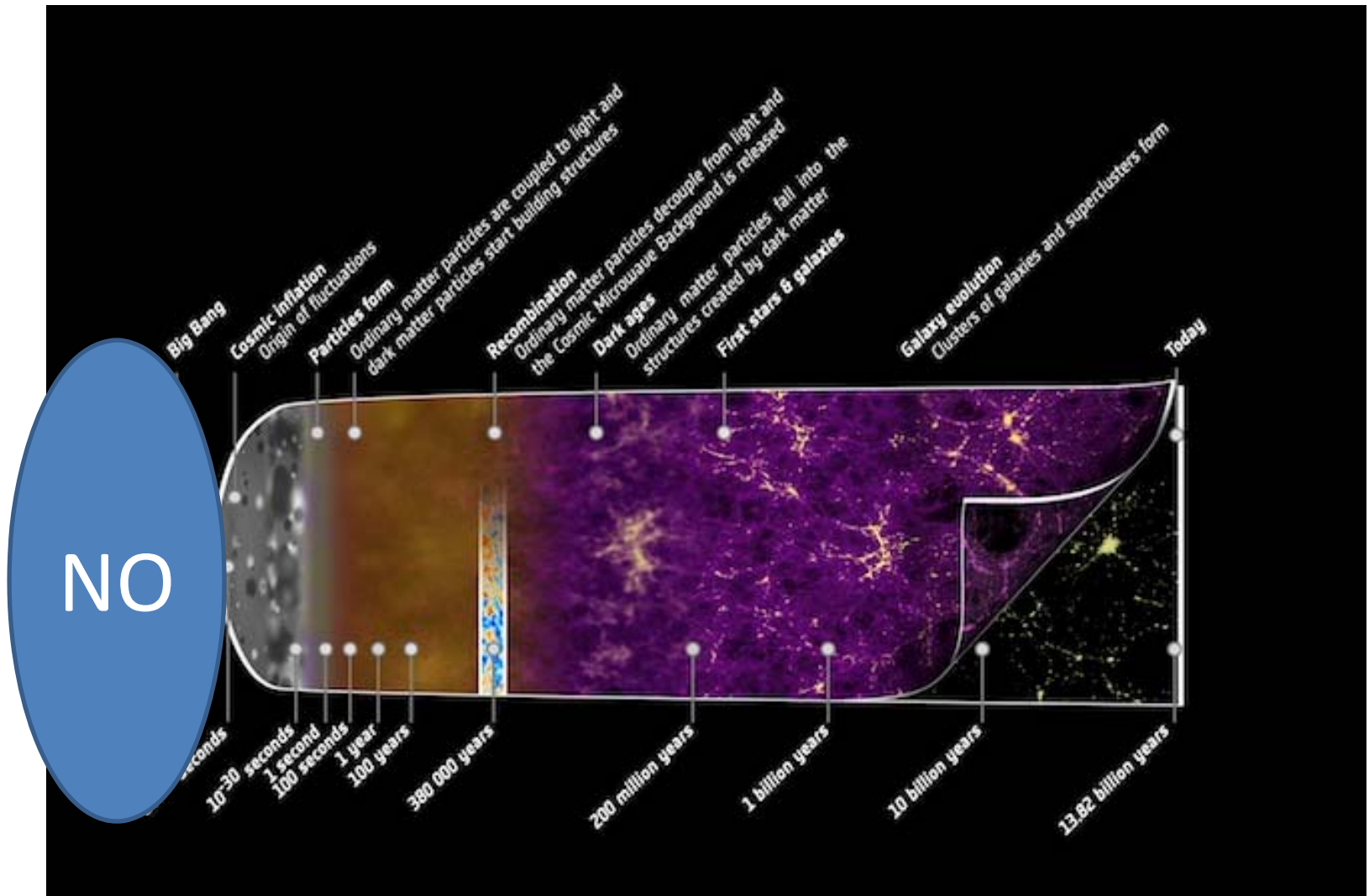
A complement to  
Alexei's talk

Andreas Albrecht; UC Davis  
Cosmocruise Sep 5 2015

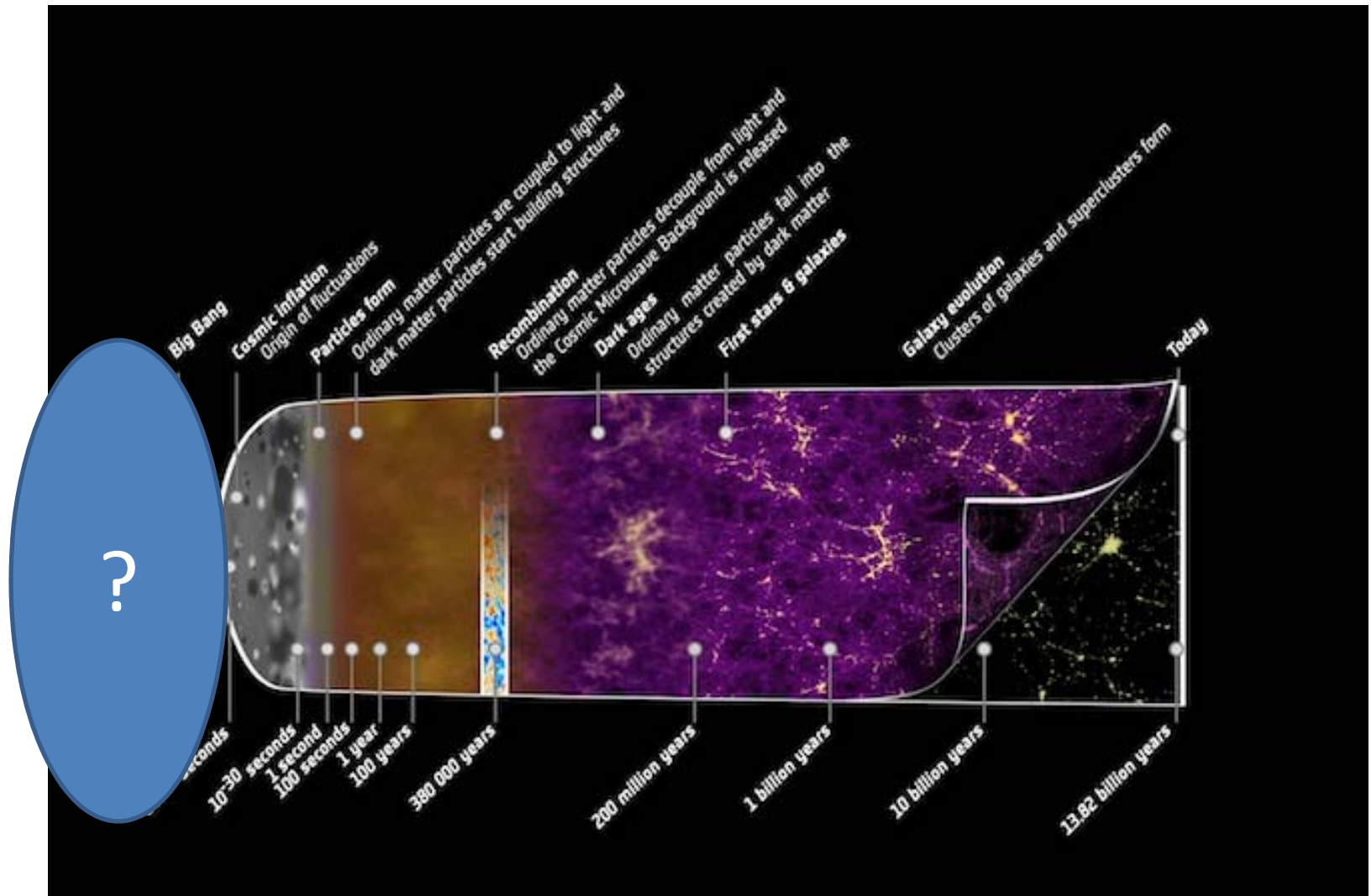
# The History of the Universe

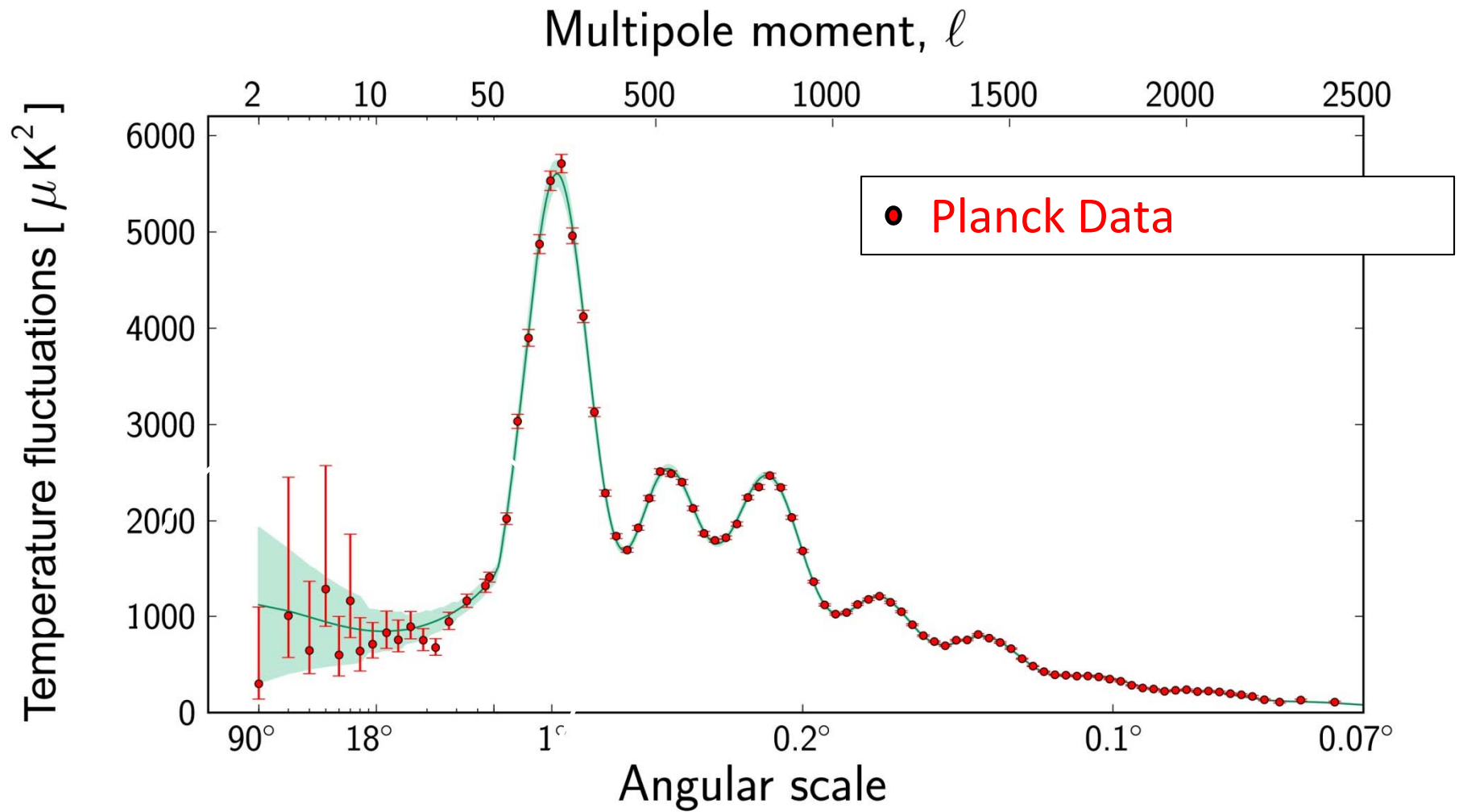


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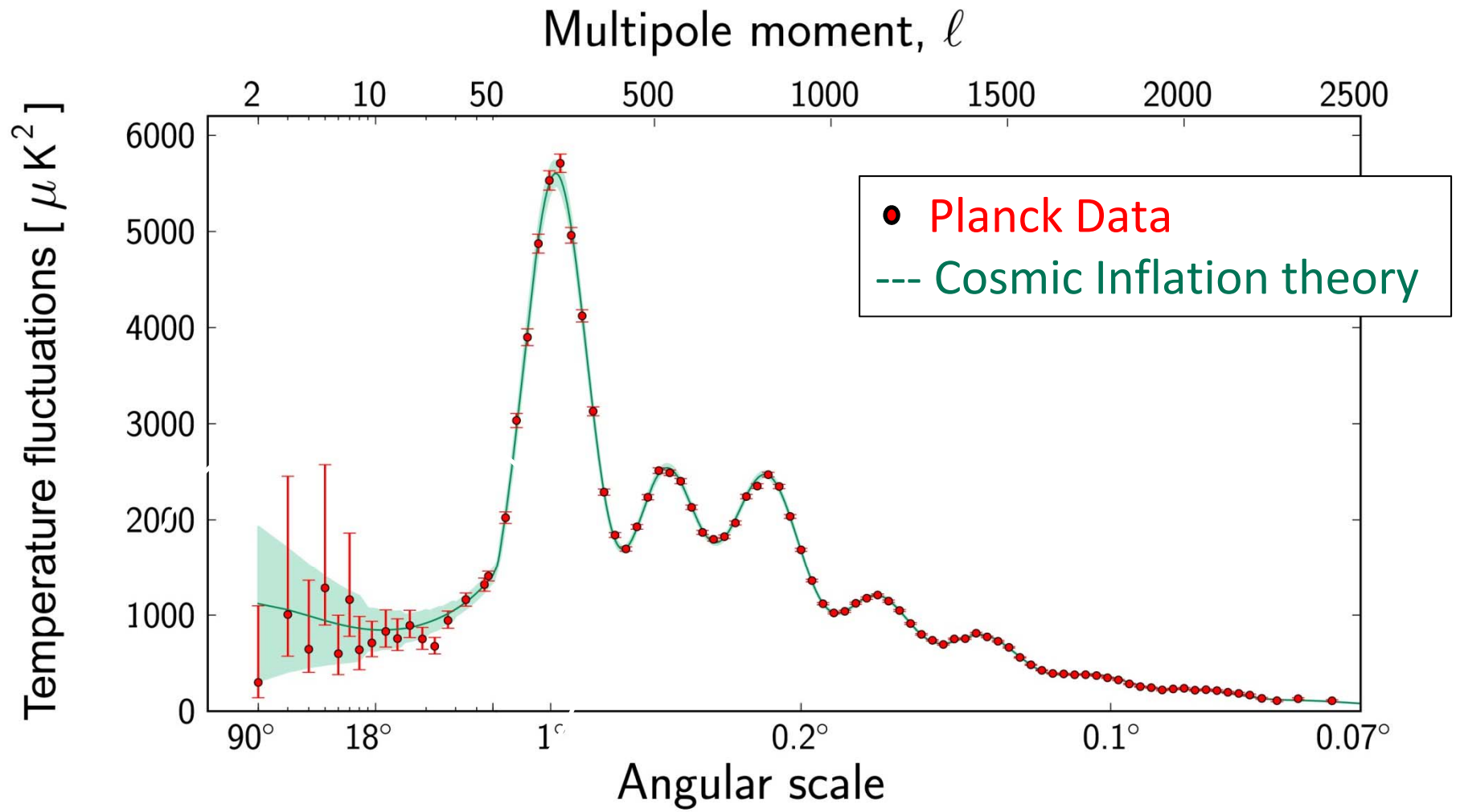


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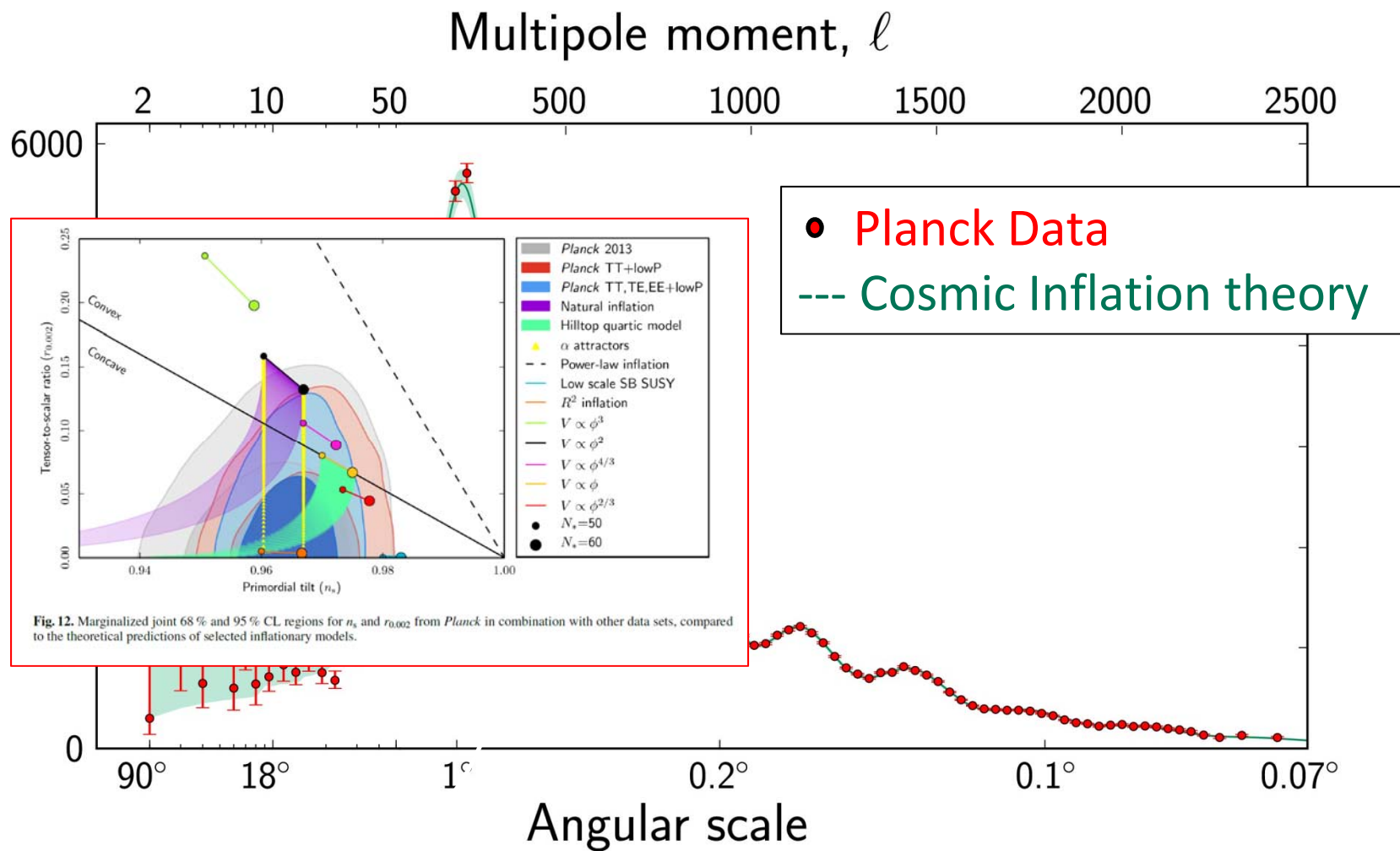




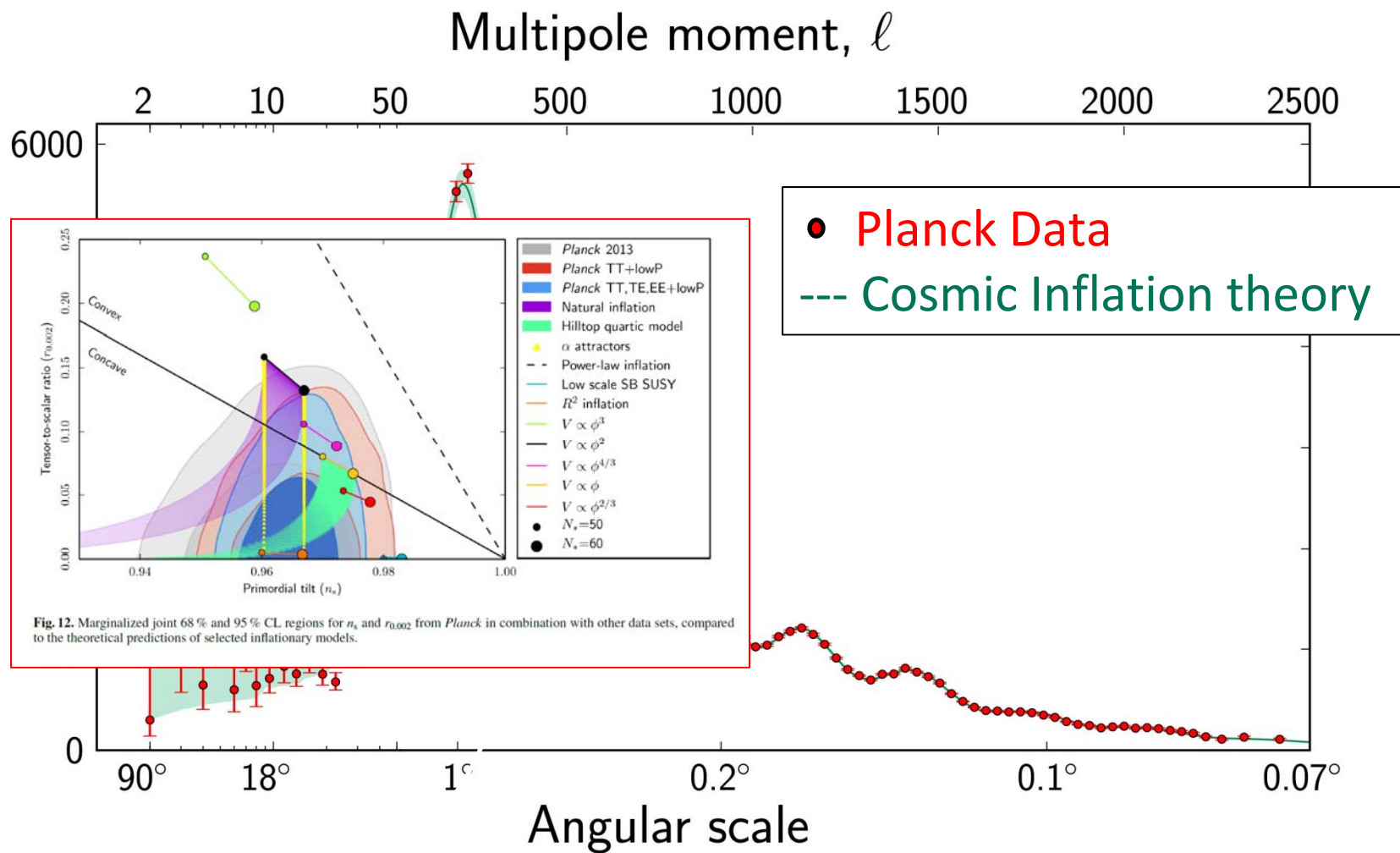




Temperature fluctuations [ $\mu K^2$ ]



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A recent application of inflation (IAU 2015)

## Cosmic Inflation:

→ Great phenomenology of cosmic structure, but:

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Unresolved  
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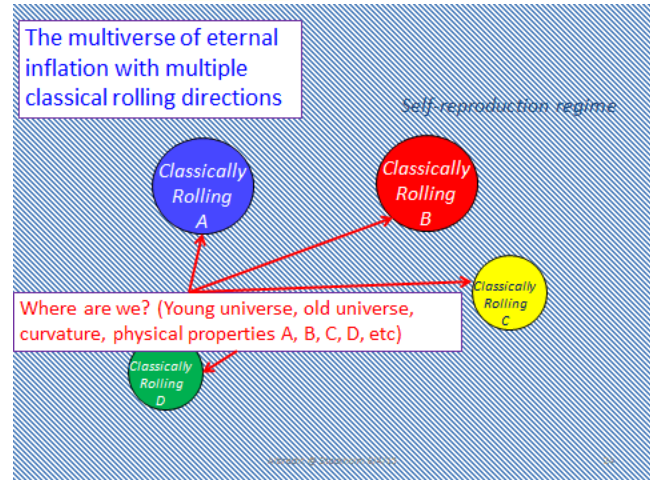
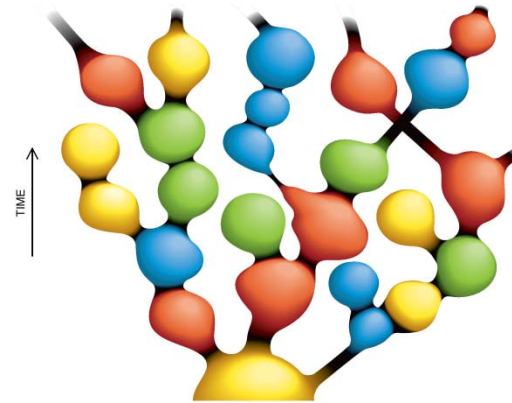
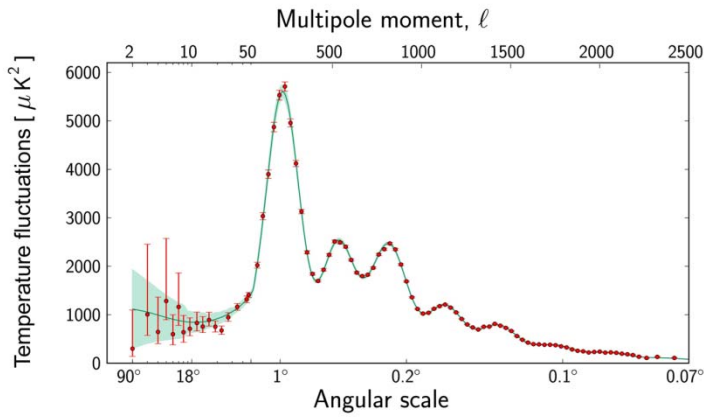
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# Cosmic Inflation:

Consumers

&

Producers

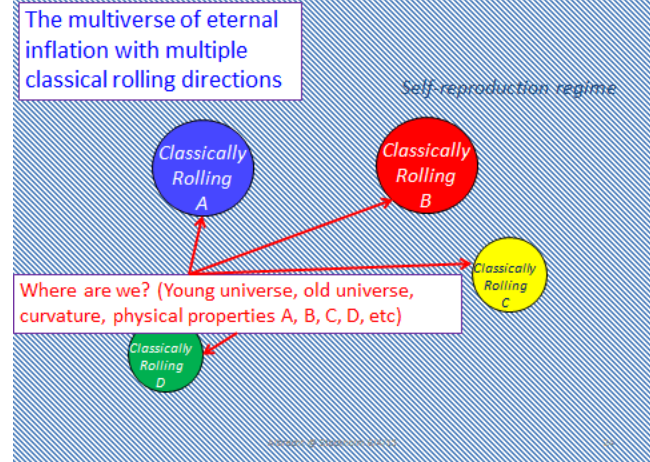
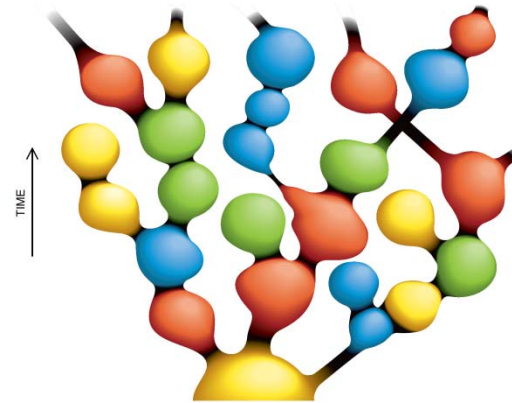
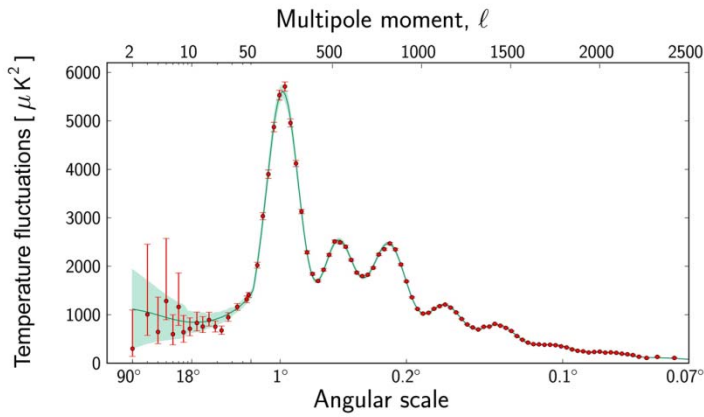


# Cosmic Inflation:

Consumers

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Goal of resolving tuning  
inspired by Guth's paper:

PHYSICAL REVIEW D

VOLUME 23, NUMBER 2

15 JANUARY 1981

## **Inflationary universe: A possible solution to the horizon and flatness problems**

Alan H. Guth\*

*Stanford Linear Accelerator Center, Stanford University, Stanford, California 94305*

(Received 11 August 1980)

The standard model of hot big-bang cosmology requires initial conditions which are problematic in two ways: (1) The early universe is assumed to be highly homogeneous, in spite of the fact that separated regions were causally disconnected (horizon problem); and (2) the initial value of the Hubble constant must be fine tuned to extraordinary accuracy to produce a universe as flat (i.e., near critical mass density) as the one we see today (flatness problem). These problems would disappear if, in its early history, the universe supercooled to temperatures 28 or more orders of magnitude below the critical temperature for some phase transition. A huge expansion factor would then result from a period of exponential growth, and the entropy of the universe would be multiplied by a huge factor when the latent heat is released. Such a scenario is completely natural in the context of grand unified models of elementary-particle interactions. In such models, the supercooling is also relevant to the problem of monopole suppression. Unfortunately, the scenario seems to lead to some unacceptable consequences, so modifications must be sought.

**A NEW TYPE OF ISOTROPIC COSMOLOGICAL MODELS WITHOUT SINGULARITY**

A.A. STAROBINSKY

*Department of Applied Mathematics and Theoretical Physics, Cambridge University, Cambridge, England<sup>1</sup>  
and The Landau Institute for Theoretical Physics, The Academy of Sciences, Moscow, 117334, USSR<sup>2</sup>*

Received 11 January 1980

The Einstein equations with quantum one-loop contributions of conformally covariant matter fields are shown to admit a class of nonsingular isotropic homogeneous and most symmetric (de Sitter) state.

It is well known that many solutions of the Einstein equations, in particular, the Robertson–Walker isotropic homogeneous model, contain singularities which are not physically continued beyond them. So

An alternate perspective in Starobinsky's famous paper:

the above mentioned condition then we shall obtain one possible answer to the fundamental question stated in the first paragraph of this paper. It is worth noting that the evolution of the Universe need not follow a "generic" solution, it may well be described just by this unique one, at least initially.

Eqs. (2), (3) were first considered in ref. [1] and then investigated in detail in ref. [2] in the case  $K = 0$ . The conclusion was that they have no nonsingular solutions. We shall show that the only reason for this result is that an additional term describing classical isotropic radiation (i.e. a certain number of initially

number of quantum fields is large. Let  $u = a^2 \dot{a}^2$ ,  $v = u + Ka^2$ . Then we have:

$$v = \frac{v^2}{H^2 a^4} - \frac{1}{M^2} \left( \frac{vv''}{a^2} - \frac{2vv'}{a^3} - \frac{v'}{4a} \right)$$

where a prime denotes a derivative. Another useful representation is obtained by letting  $f = u^{3/4}$ ,  $\xi = (12\pi^2 / M^2) \int d^2 f / d\xi^2 + M^2 \xi^{-2/3} f^{-1/3} - M^2 f$

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vs "normal" physics theory (e.g. Starobinsky's talk)

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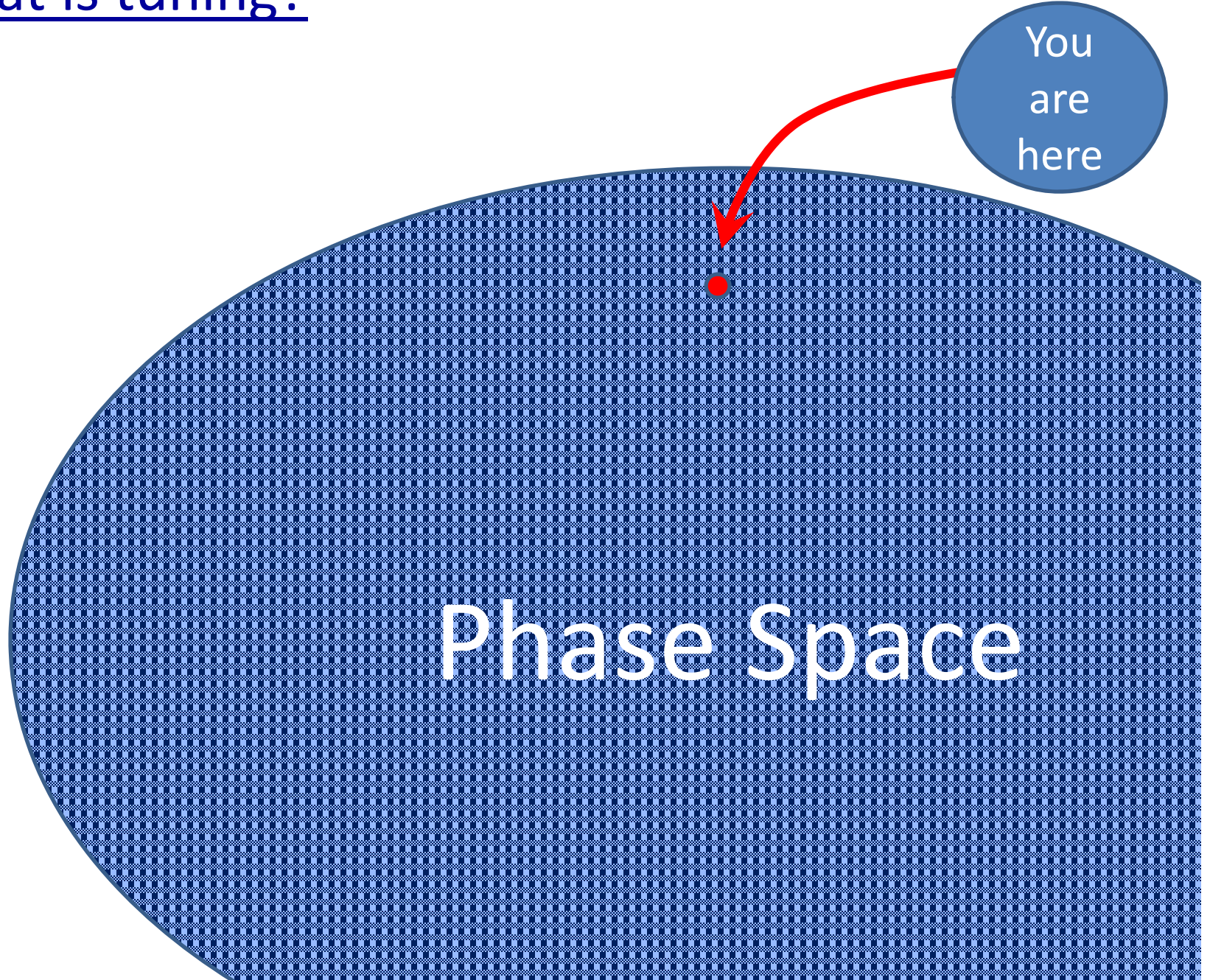
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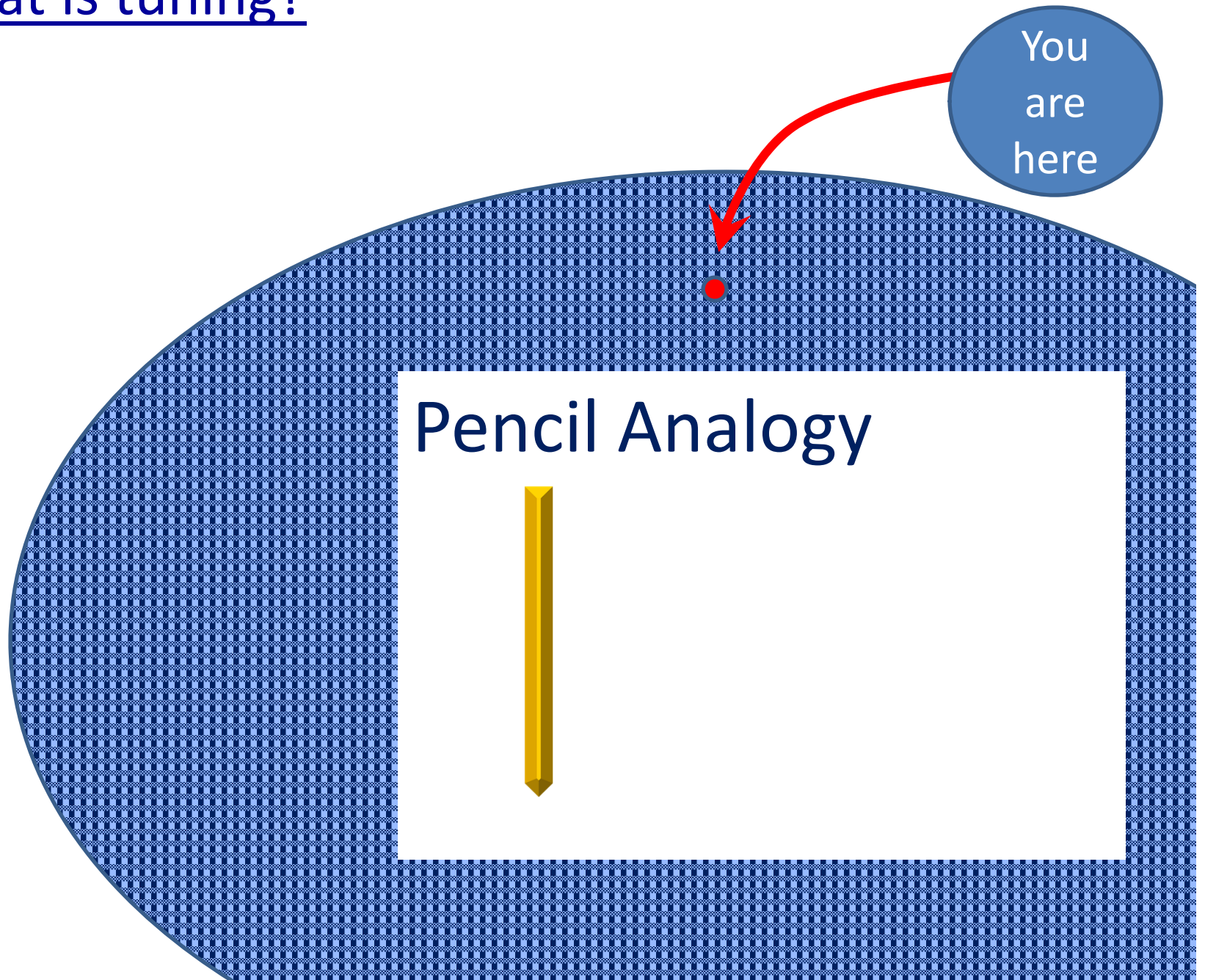
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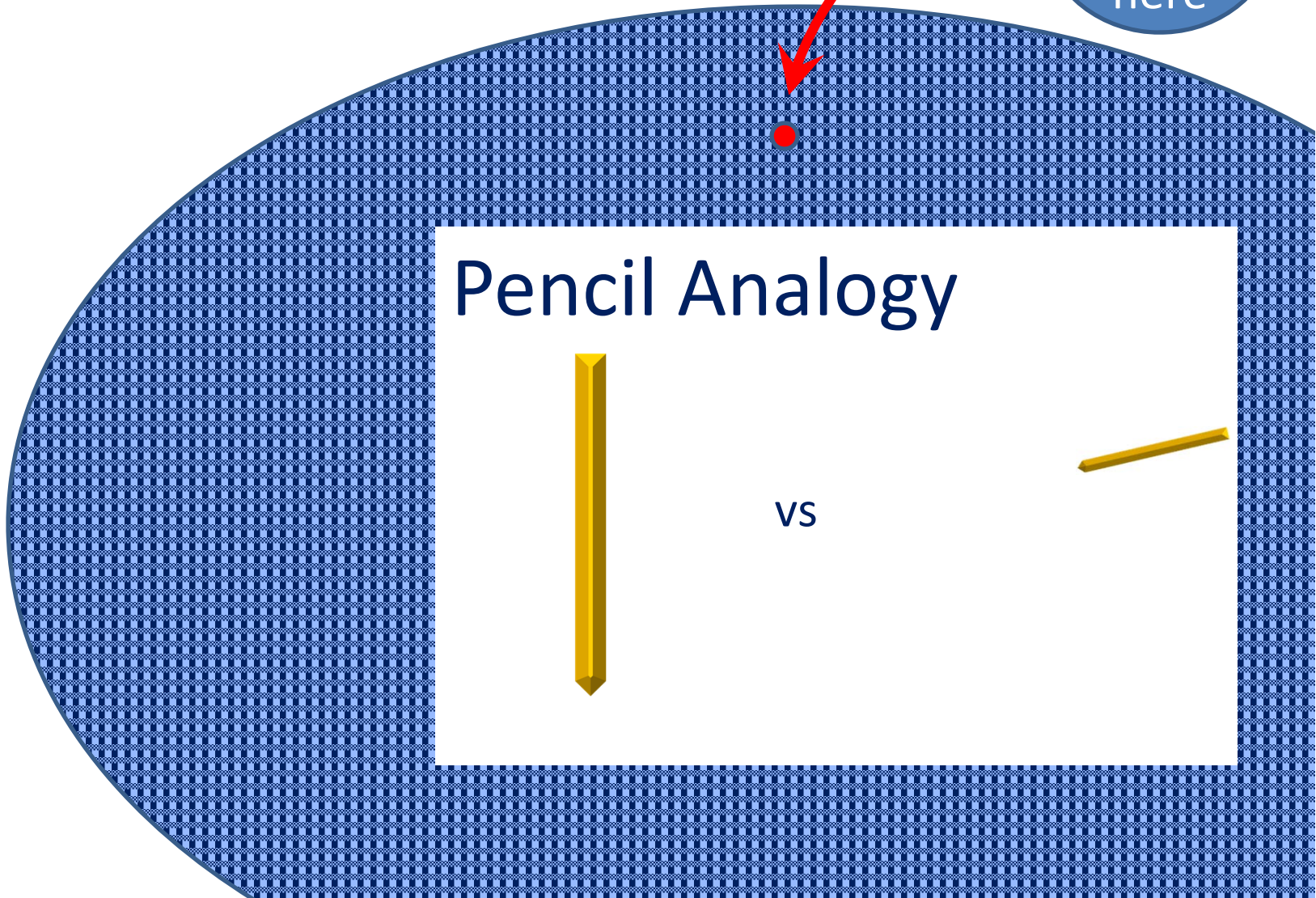
# What is tuning?





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You  
are  
here



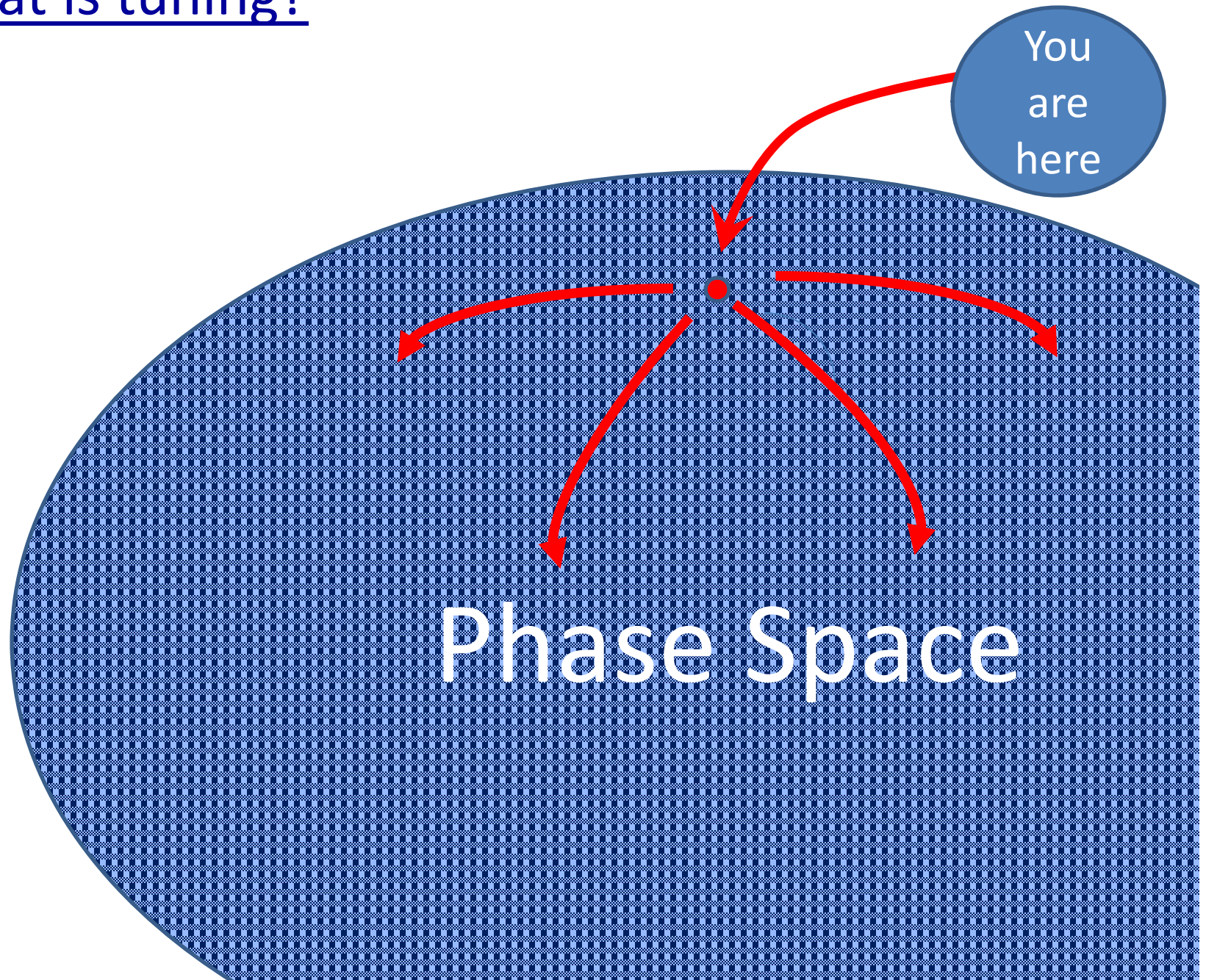
## Pencil Analogy



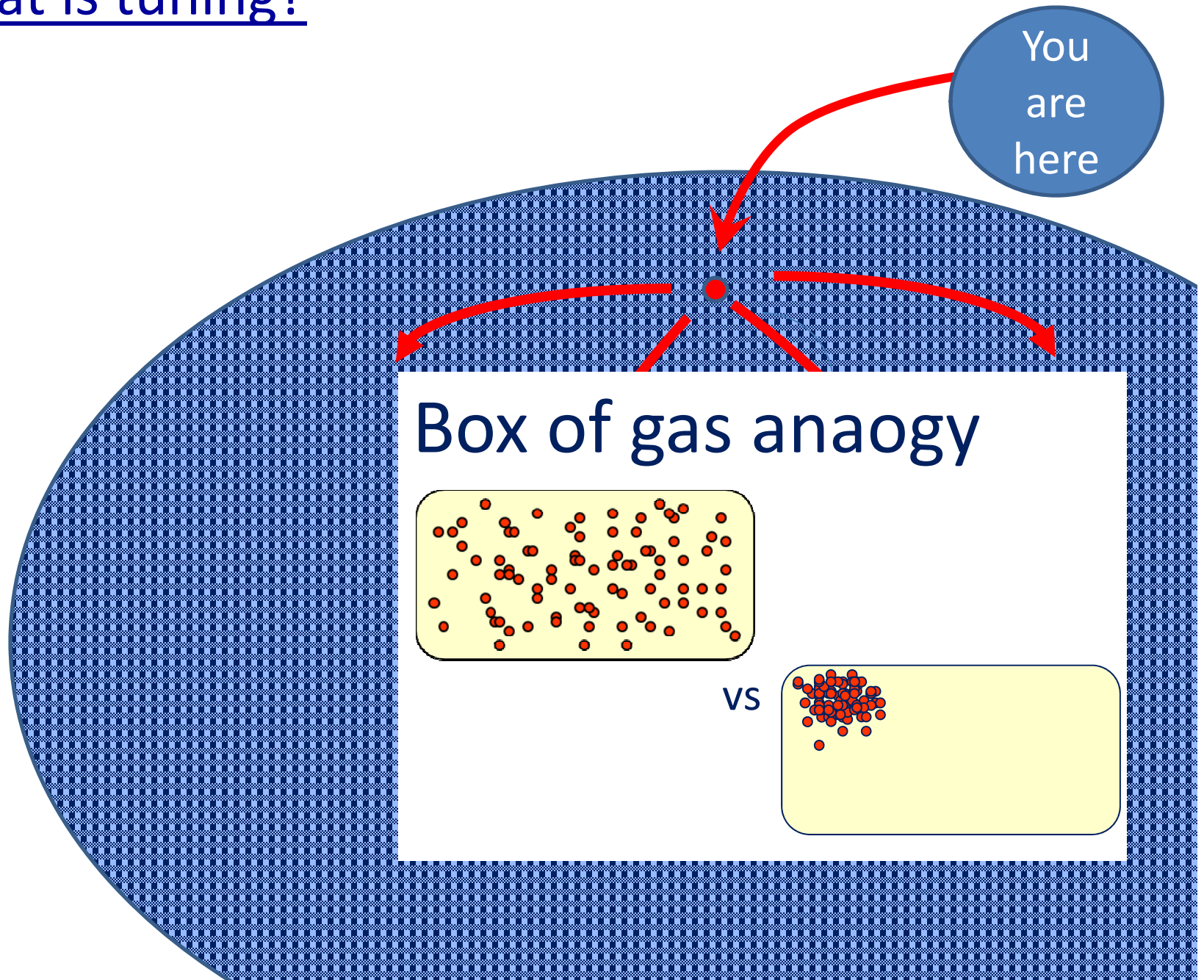
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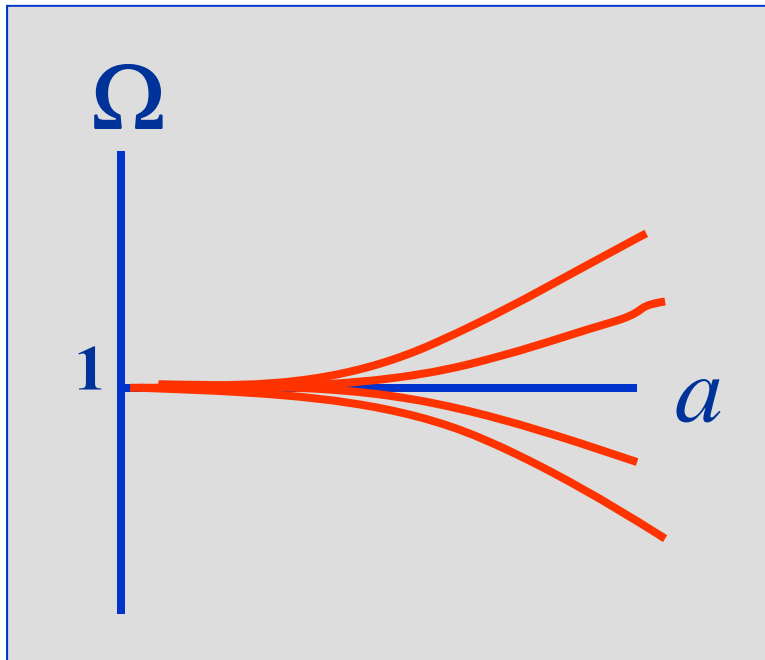
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In the SBB, flatness & homogeneity are "unstable fixed points":



$$\Omega \equiv \frac{\rho}{\rho_c}$$

$$\rho_c \equiv \frac{3H^2}{8\pi}$$

$$\left(\frac{\dot{a}}{a}\right)^2 \equiv H^2 = \frac{8\pi}{3}\rho - \frac{k}{a^2}$$

$$\propto a^{-3}, a^{-4}$$

Dominates with time

At  $T = 10^{16} \text{ GeV}$

or  $\frac{a}{a_0} = 10^{-28}$

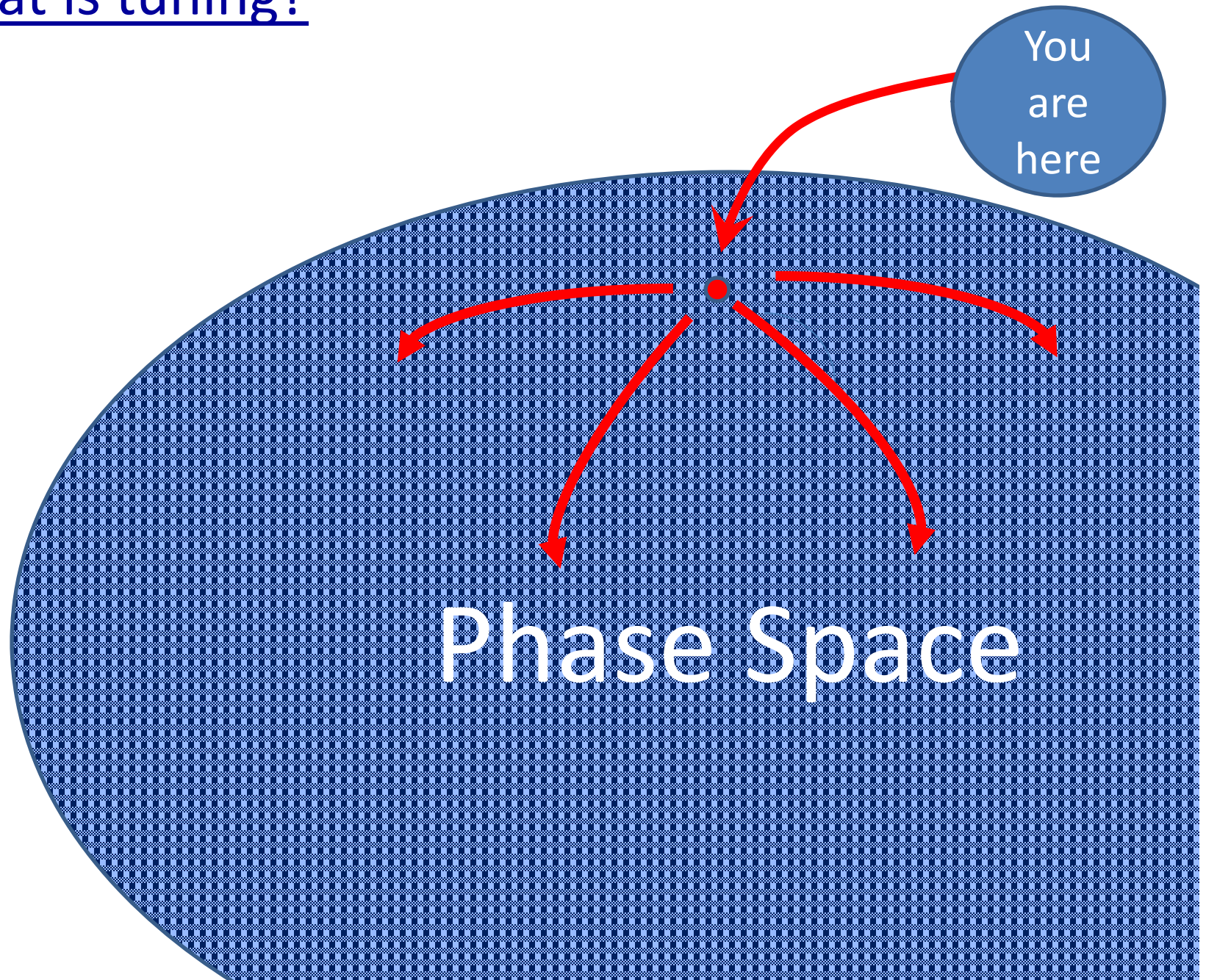
The "GUT scale"

Require  $\rho = \rho_c$  to 55 decimal places to get

$$\rho \approx \rho_c$$

today 36

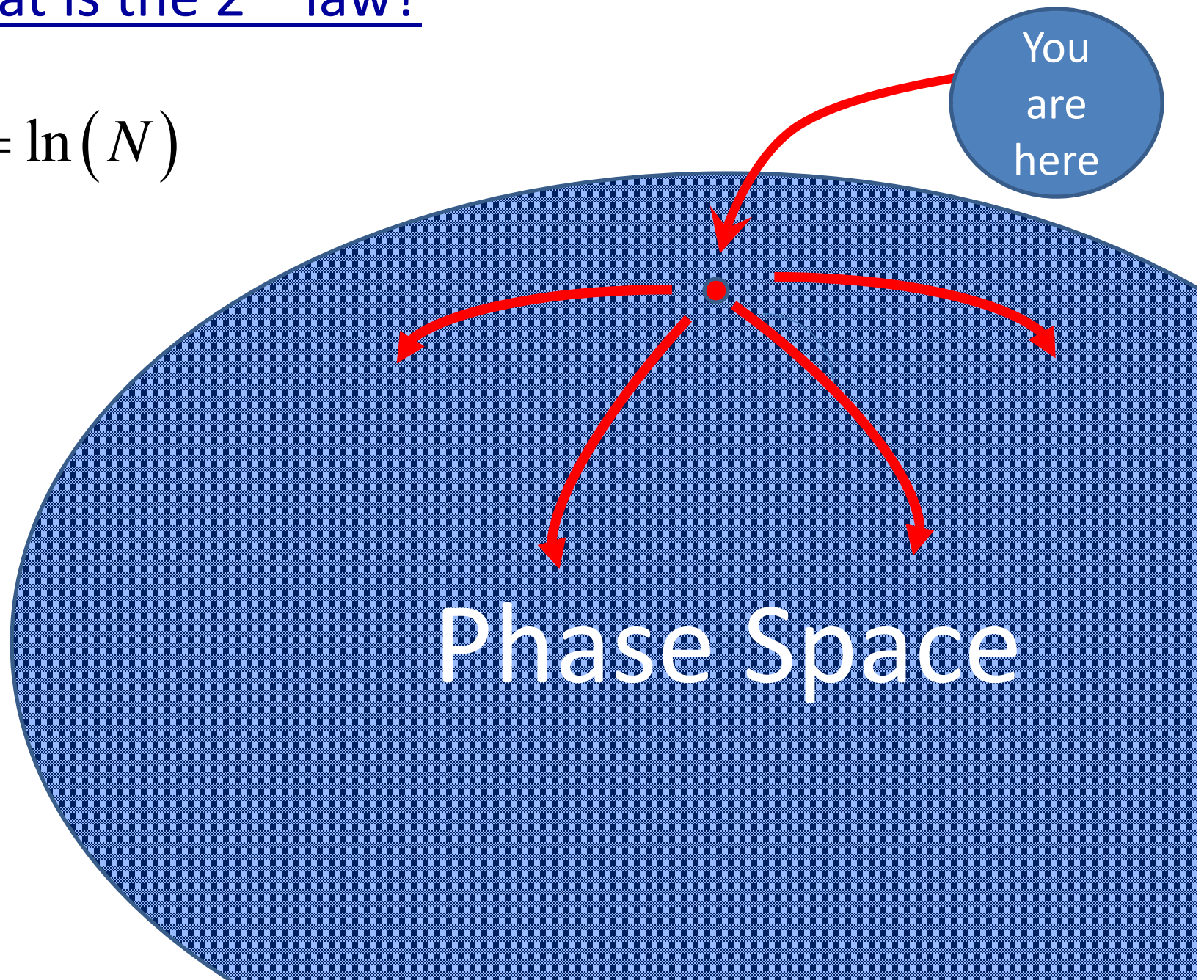
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$$S = \ln(N)$$



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2<sup>nd</sup> law  $\equiv$  tuning?



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Is the only way to avoid tuning  
to abandon the 2<sup>nd</sup> law?

$S$

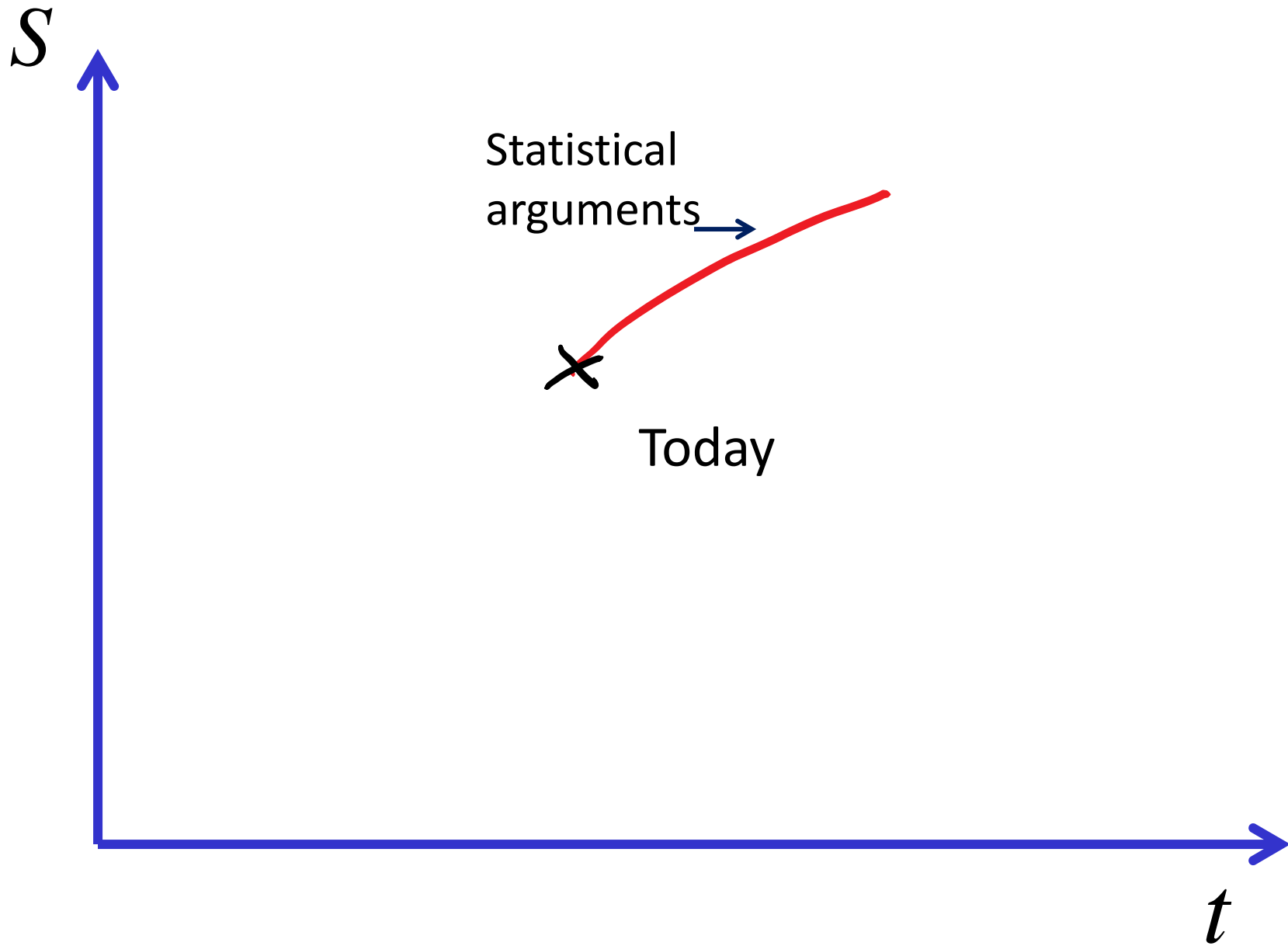


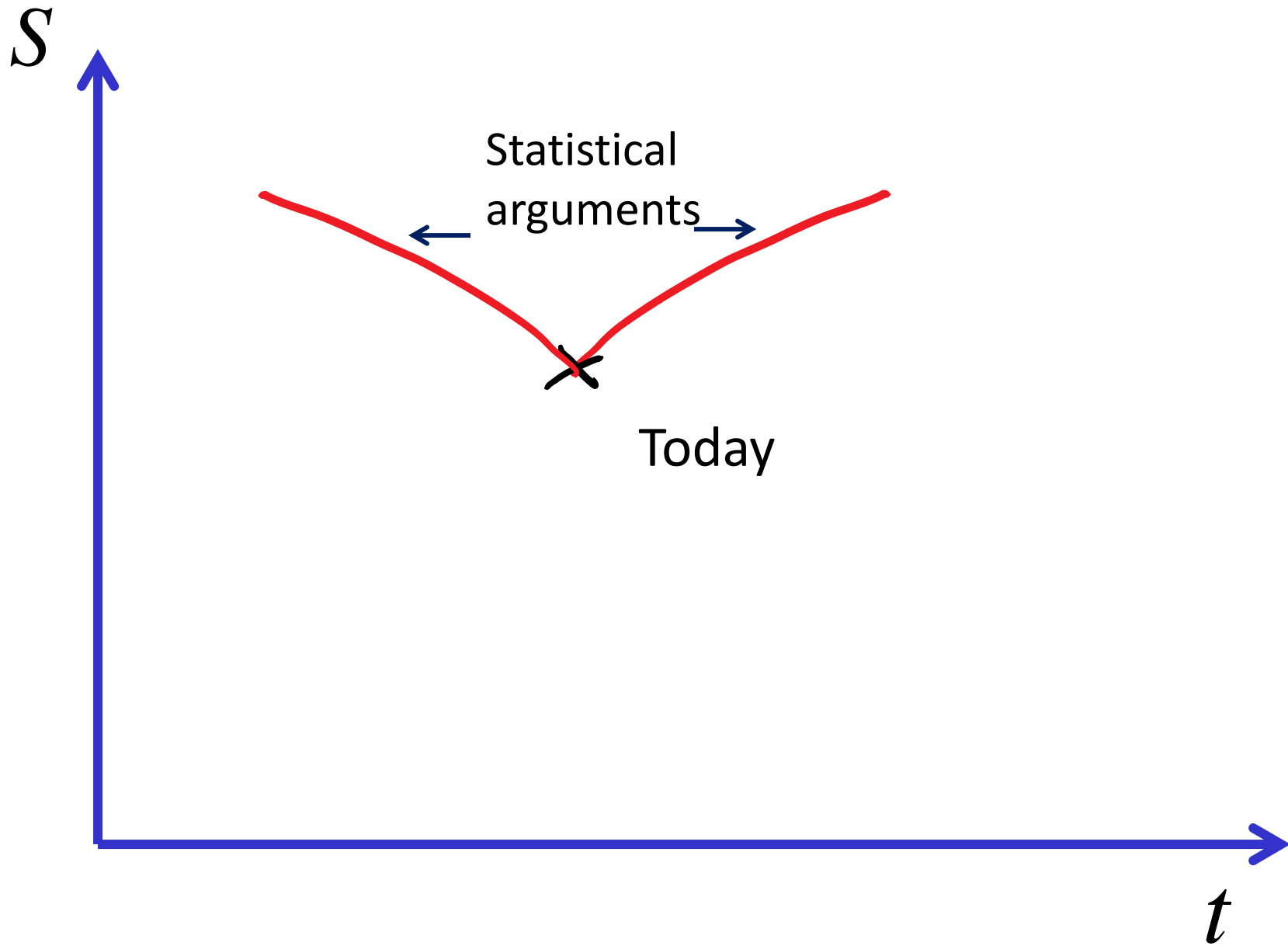
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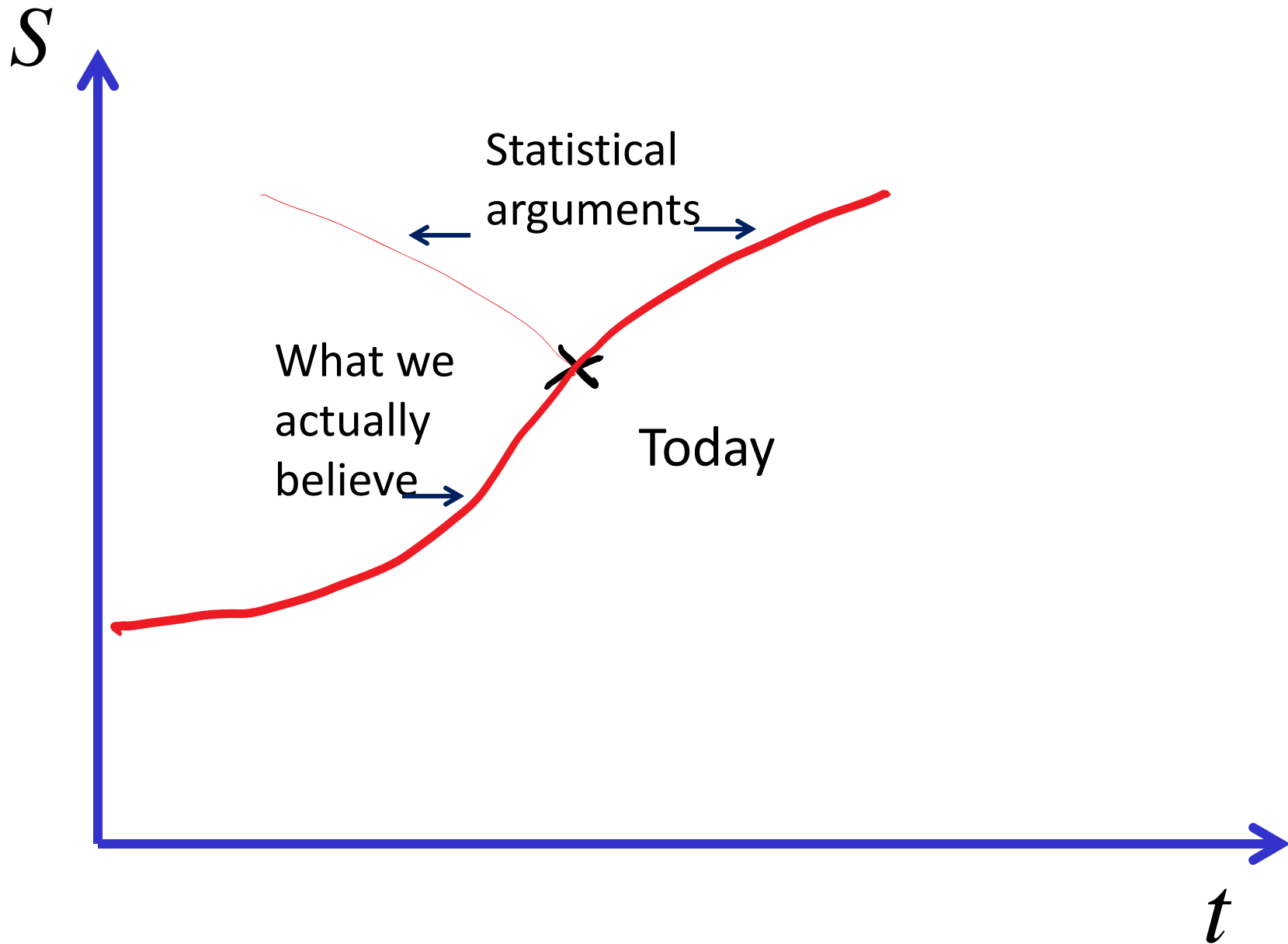
Today

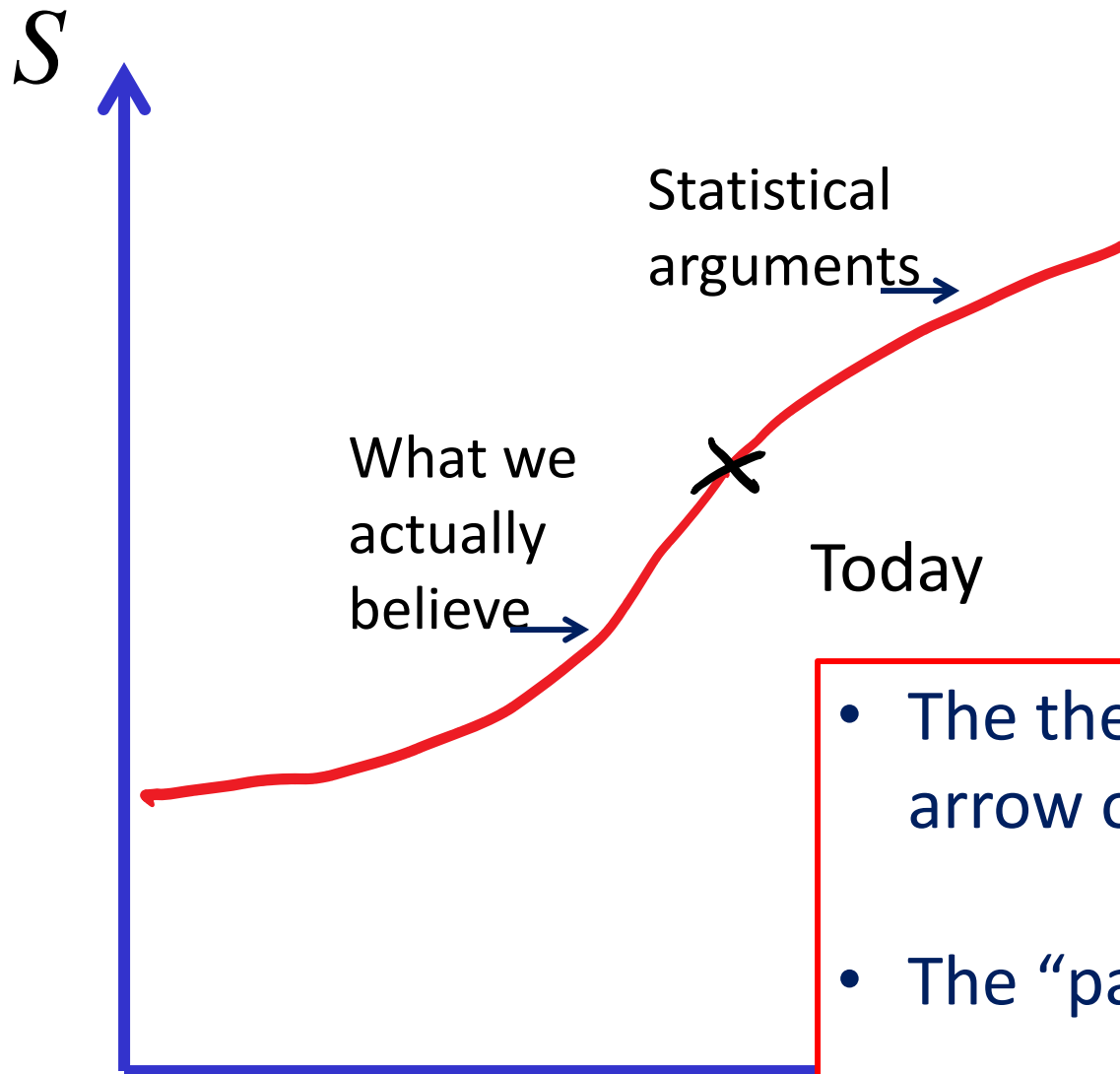
$t$



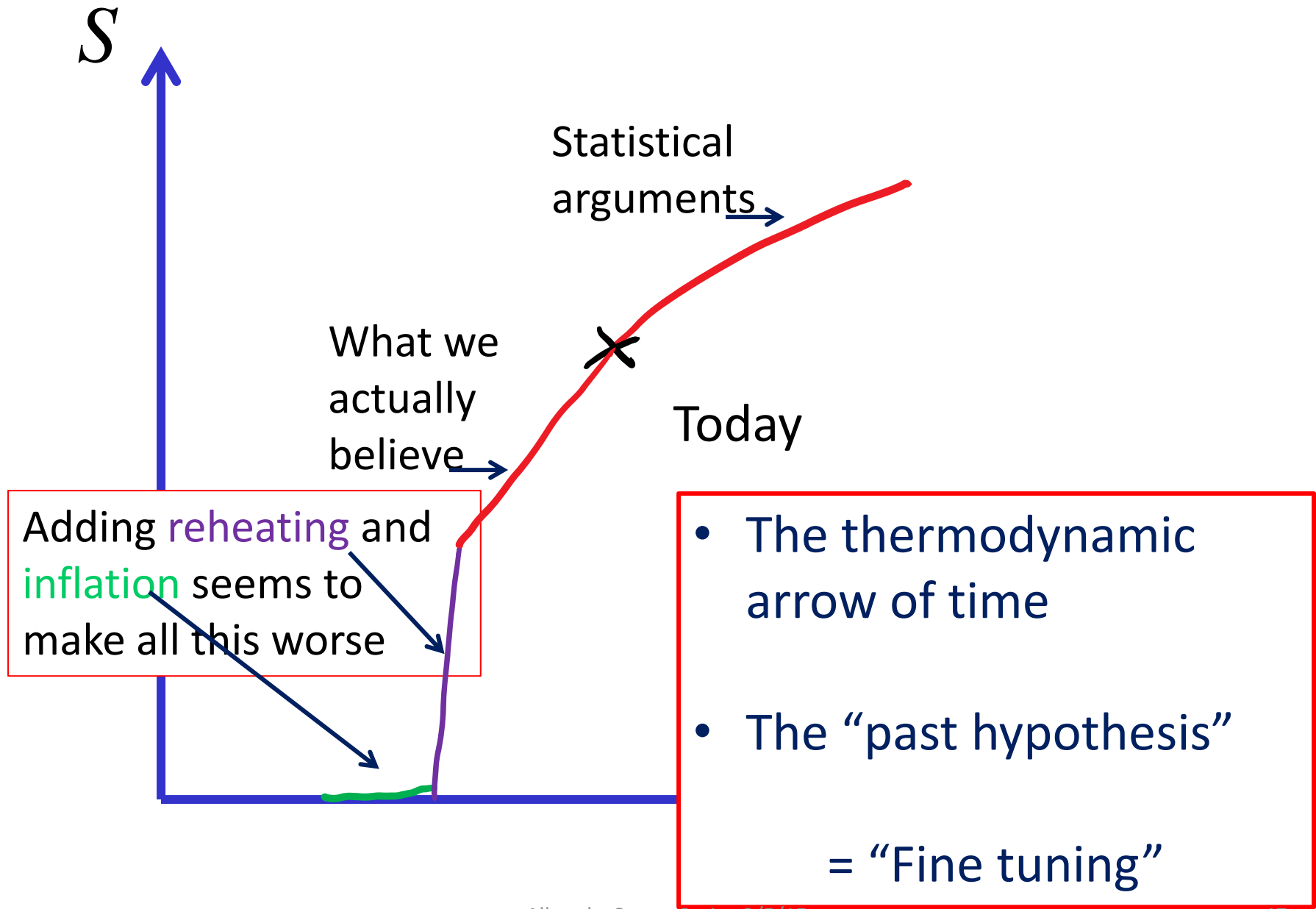


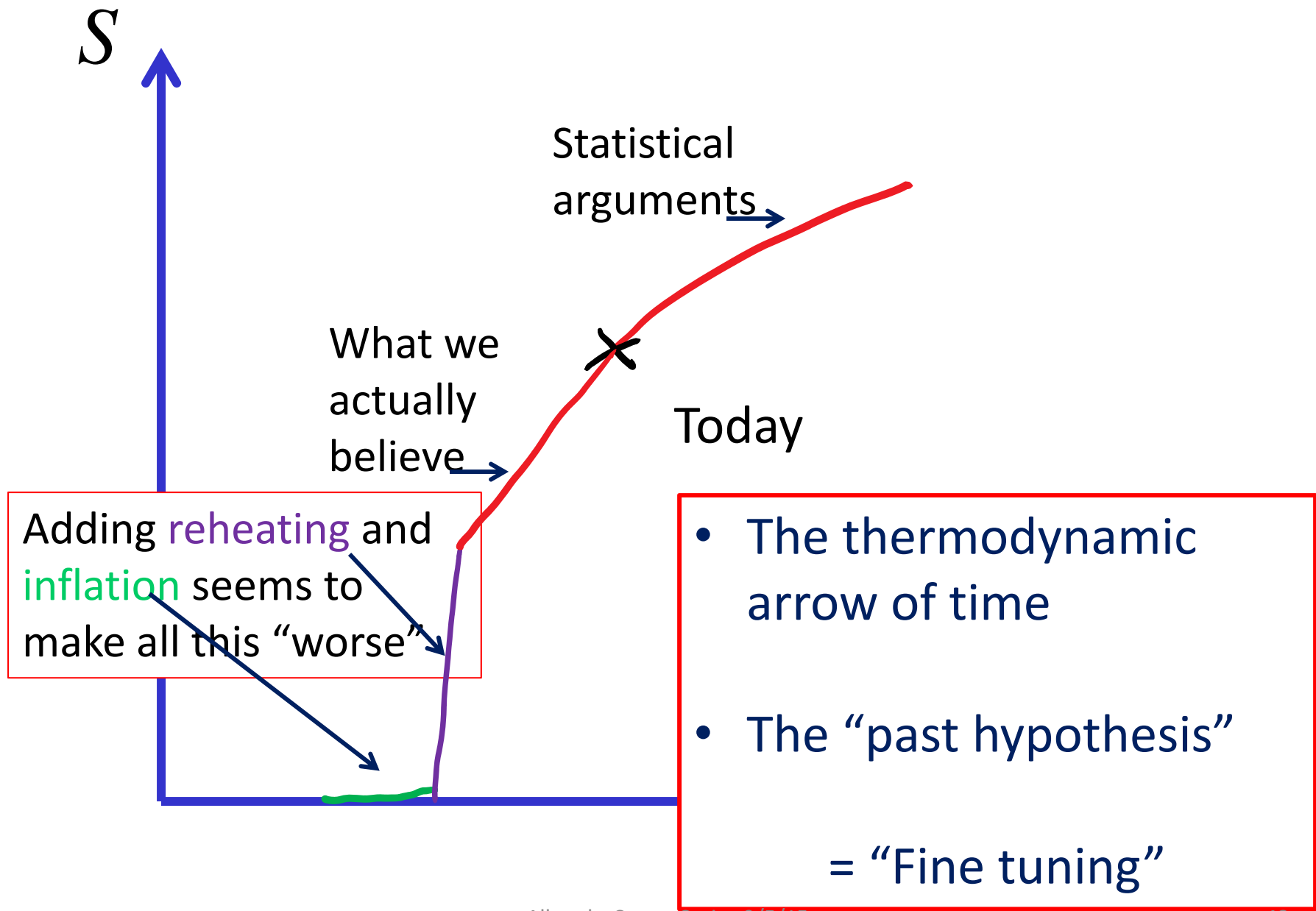






- The thermodynamic arrow of time
- The “past hypothesis”  
= “Fine tuning”







$S$

Statistical arguments →

What  
ac  
b

Low entropy of early universe  
(SBB) = low \*gravitational\*  
entropy = FRW (Penrose)

Adding reheating and  
inflation seems to  
make all this "worse"

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Related to Starobinsky  
comment about  
finding a black hole

= Fine tuning

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The tendency to slip in assumptions about  $\dot{S} > 0$   
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Stoltenberg & AA 2015

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Hernley, AA & Dray  
2013

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NB Same  
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“but it’s  
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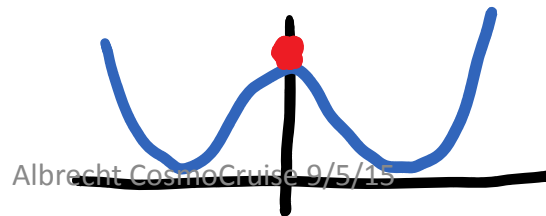
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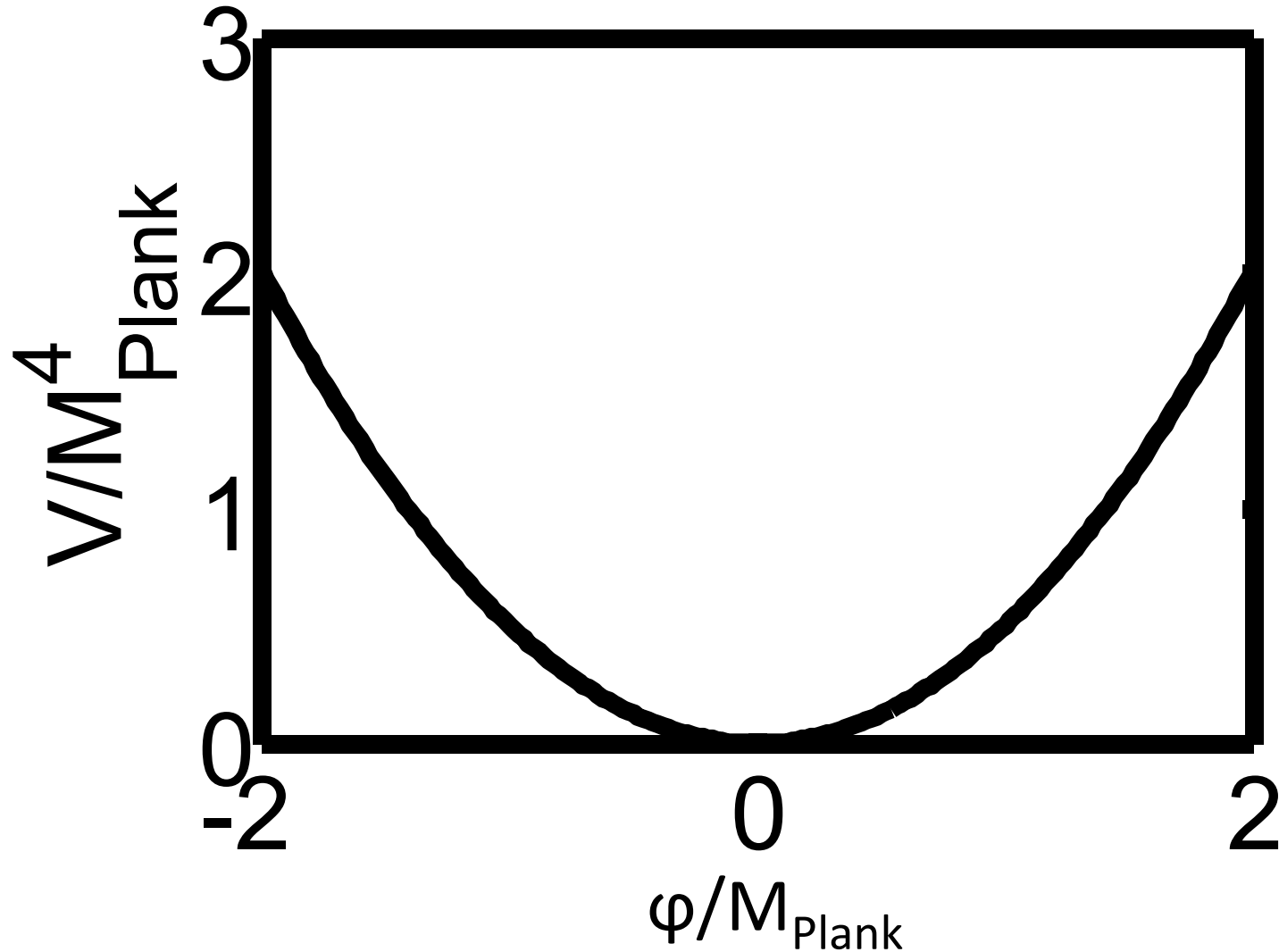
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- Belief in “naturalness” of high energy density starts



- “Std inflation”
- Landscape

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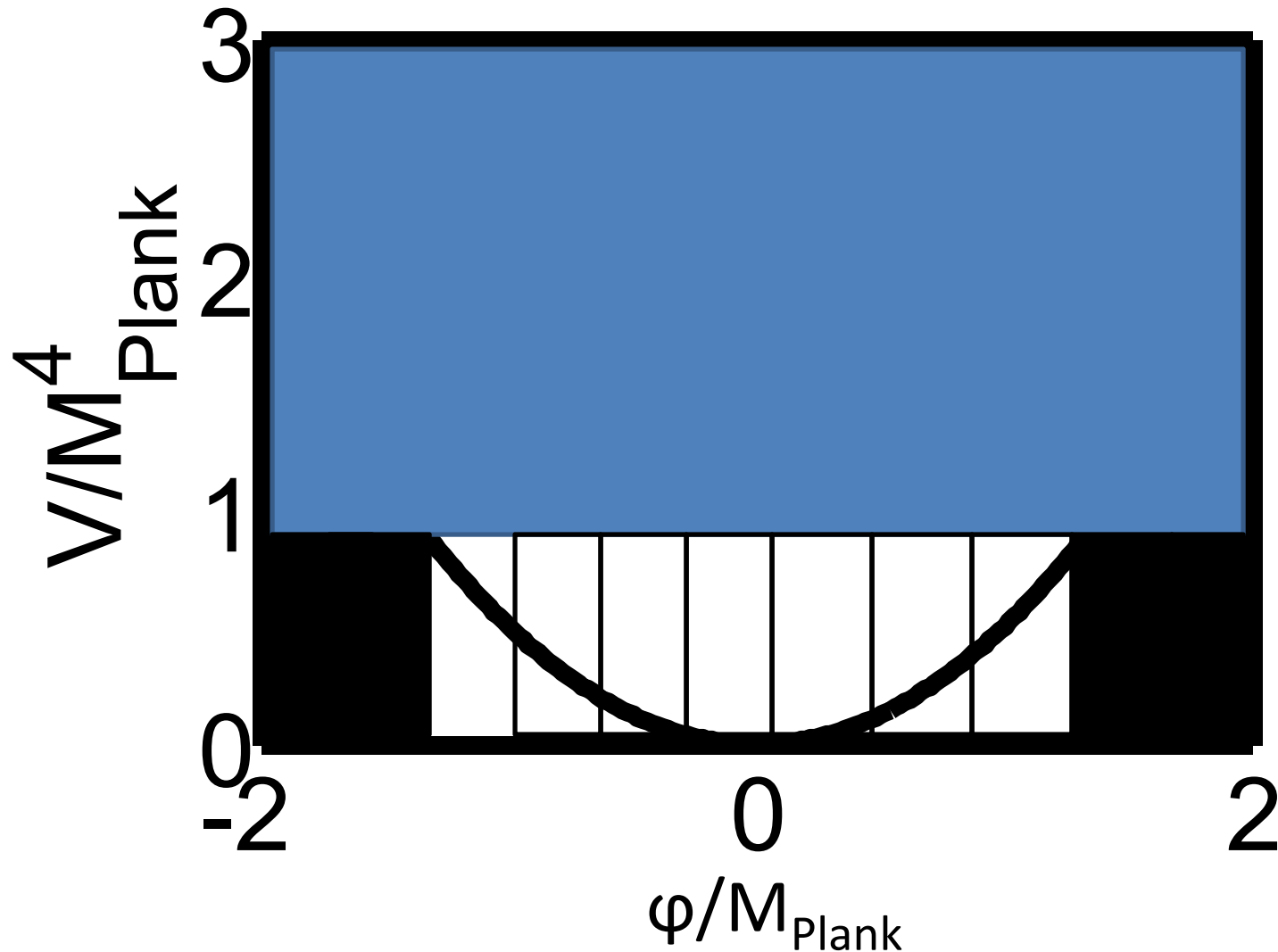
Equipartition argument  
(equally likely anywhere on potential)





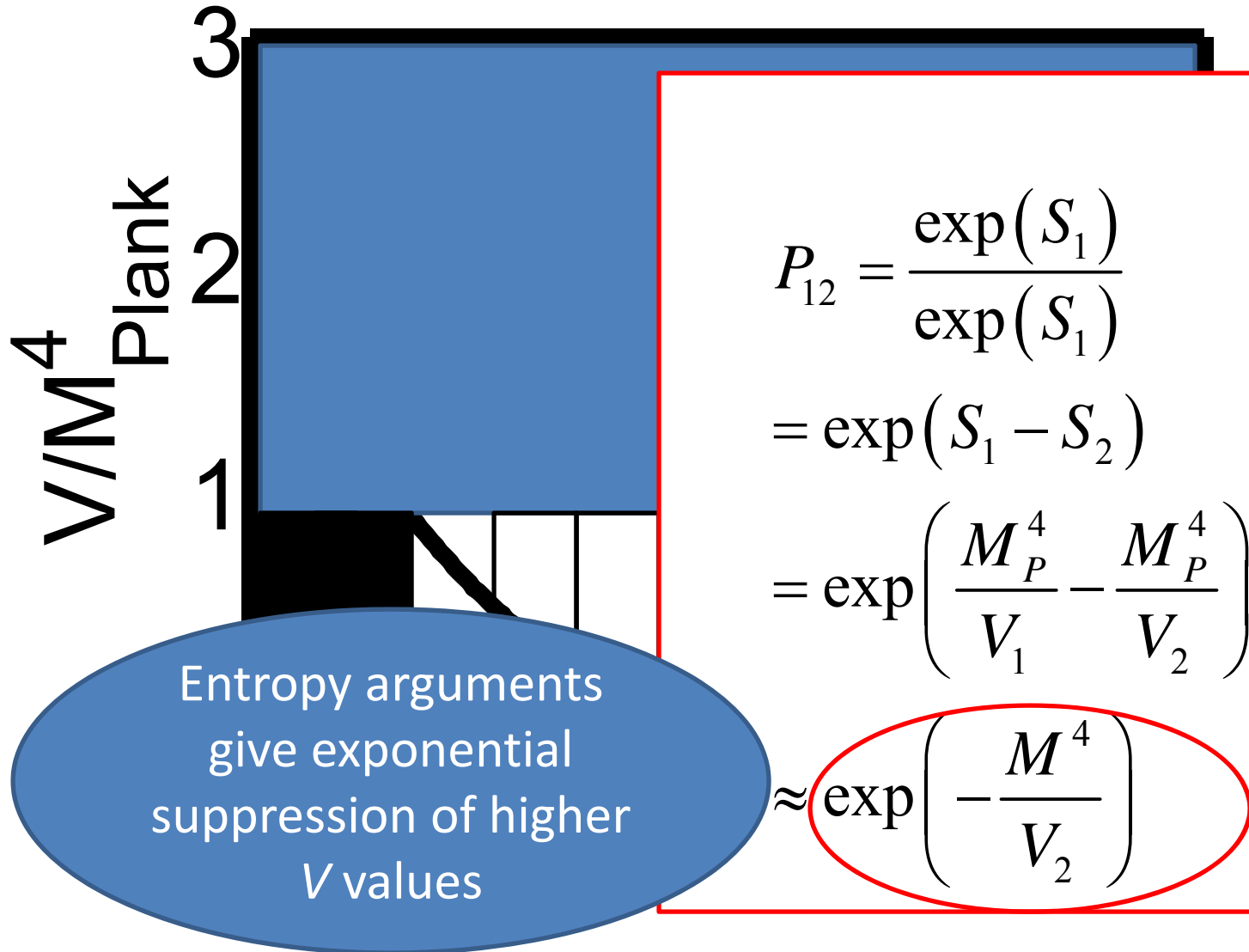
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“Why would you want to start with high entropy? You should end with that”

Entropy arguments give exponential suppression of higher  $V$  values

$$\begin{aligned} P_{12} &= \frac{\exp(S_1)}{\exp(S_1)} \\ &= \exp(S_1 - S_2) \\ &= \exp\left(\frac{M_P^4}{V_1} - \frac{M_P^4}{V_2}\right) \\ &\approx \exp\left(-\frac{M^4}{V_2}\right) \end{aligned}$$

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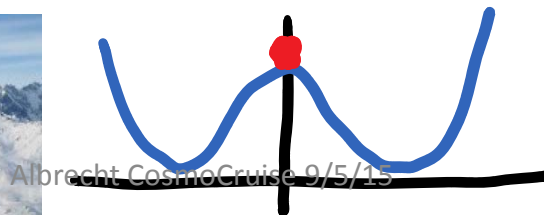
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“But if eternal inflation produces an infinite universe surely it does not matter if the start of inflation is very improbable”

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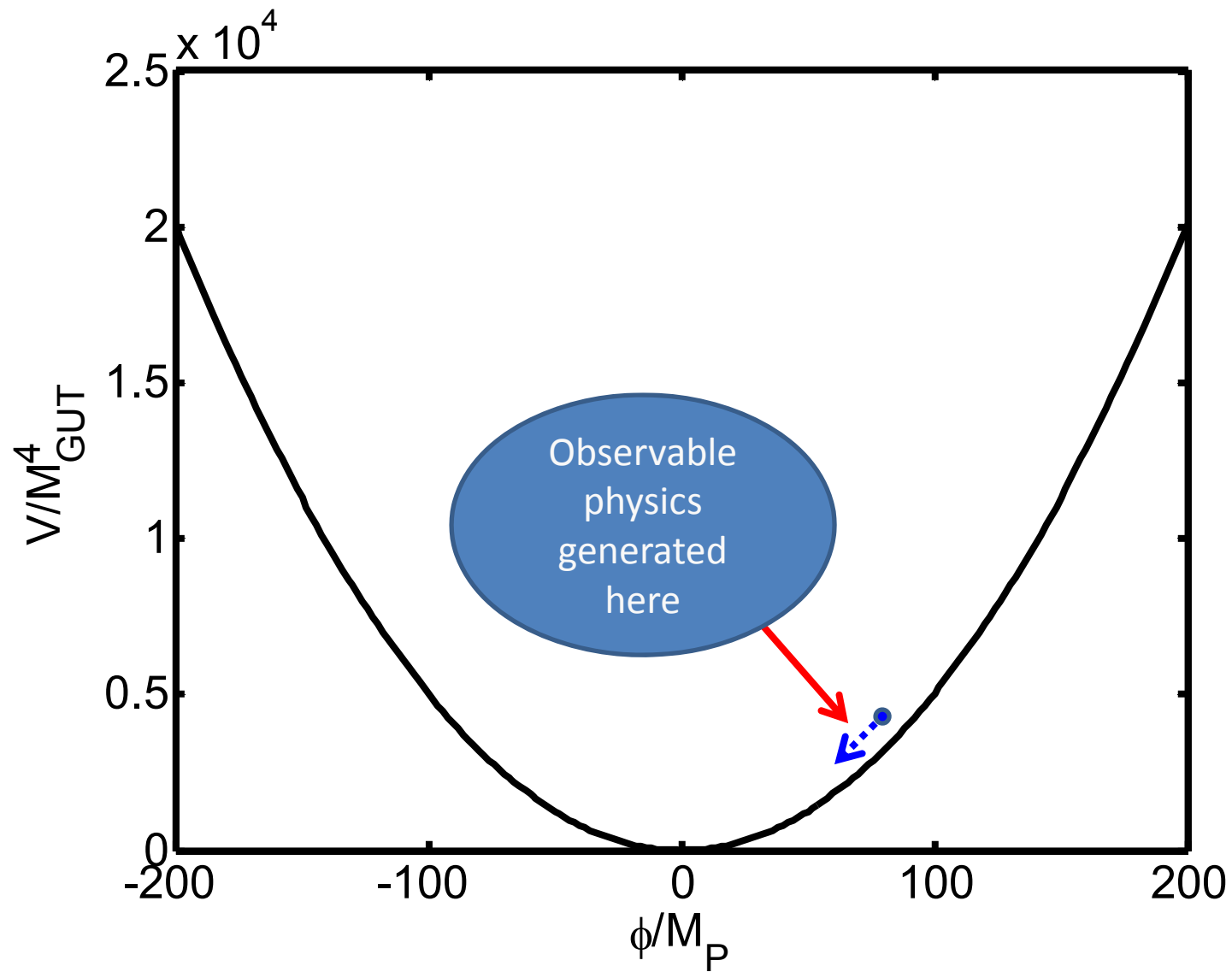
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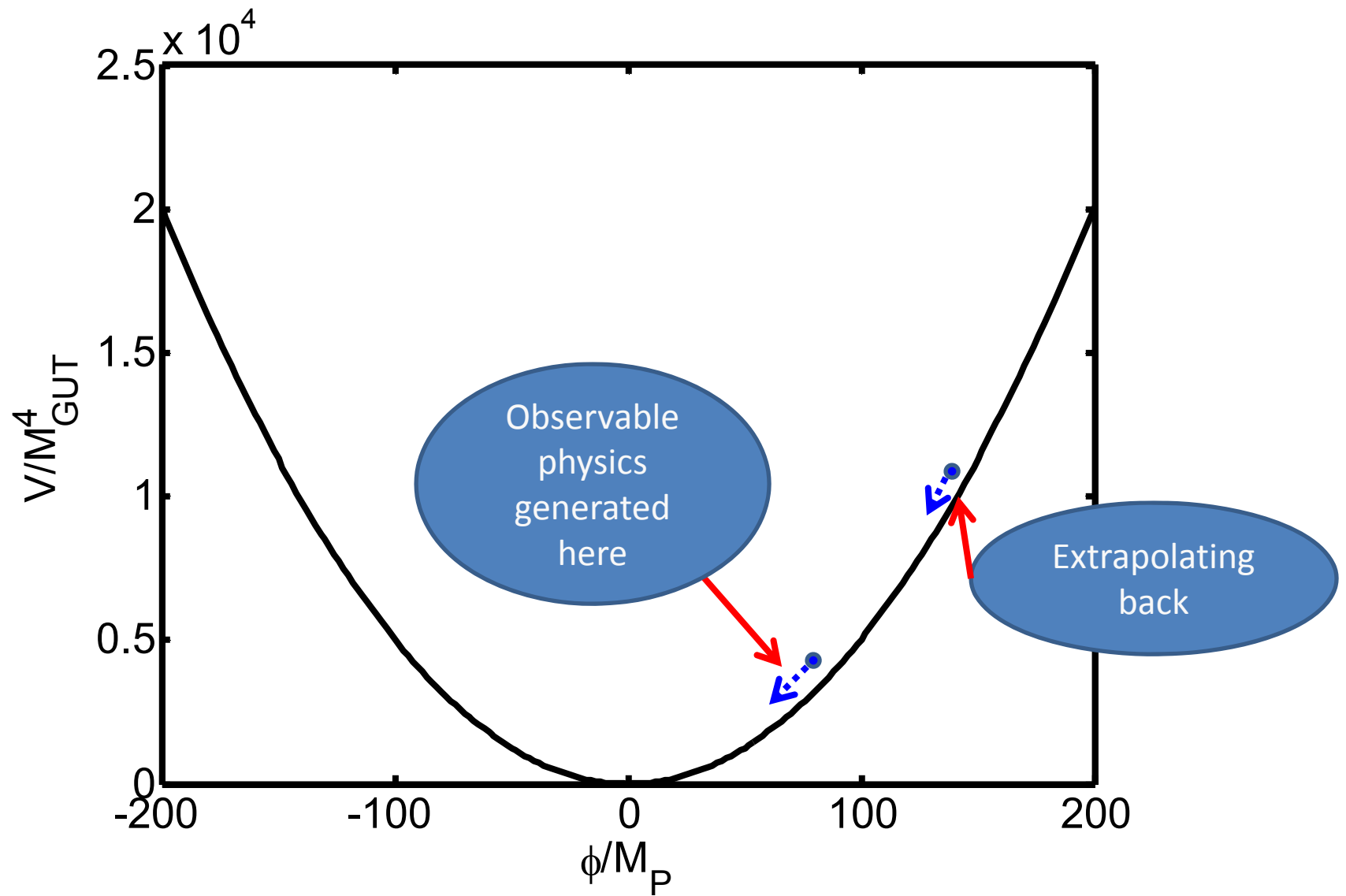
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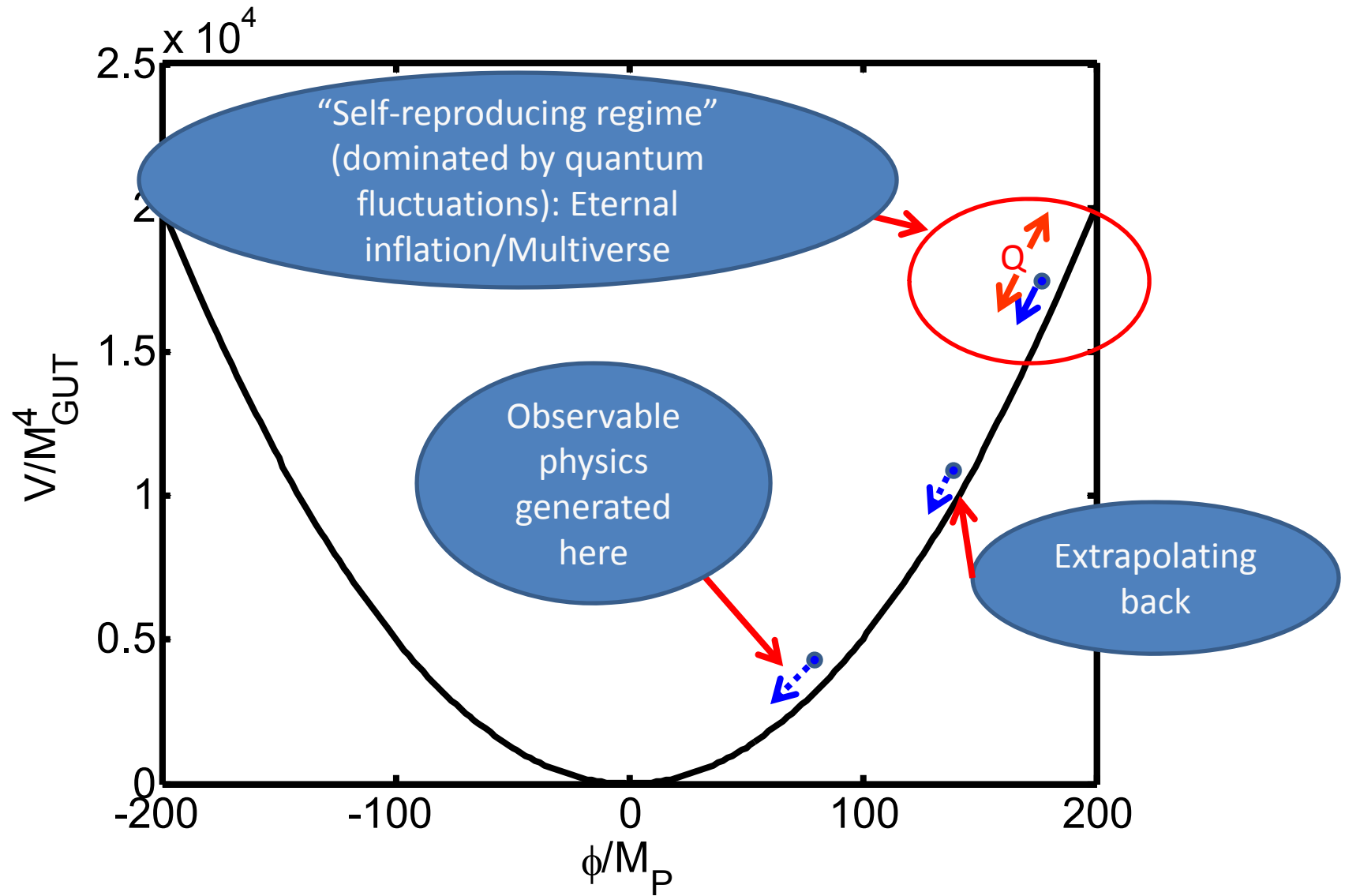
# Slow rolling of inflaton



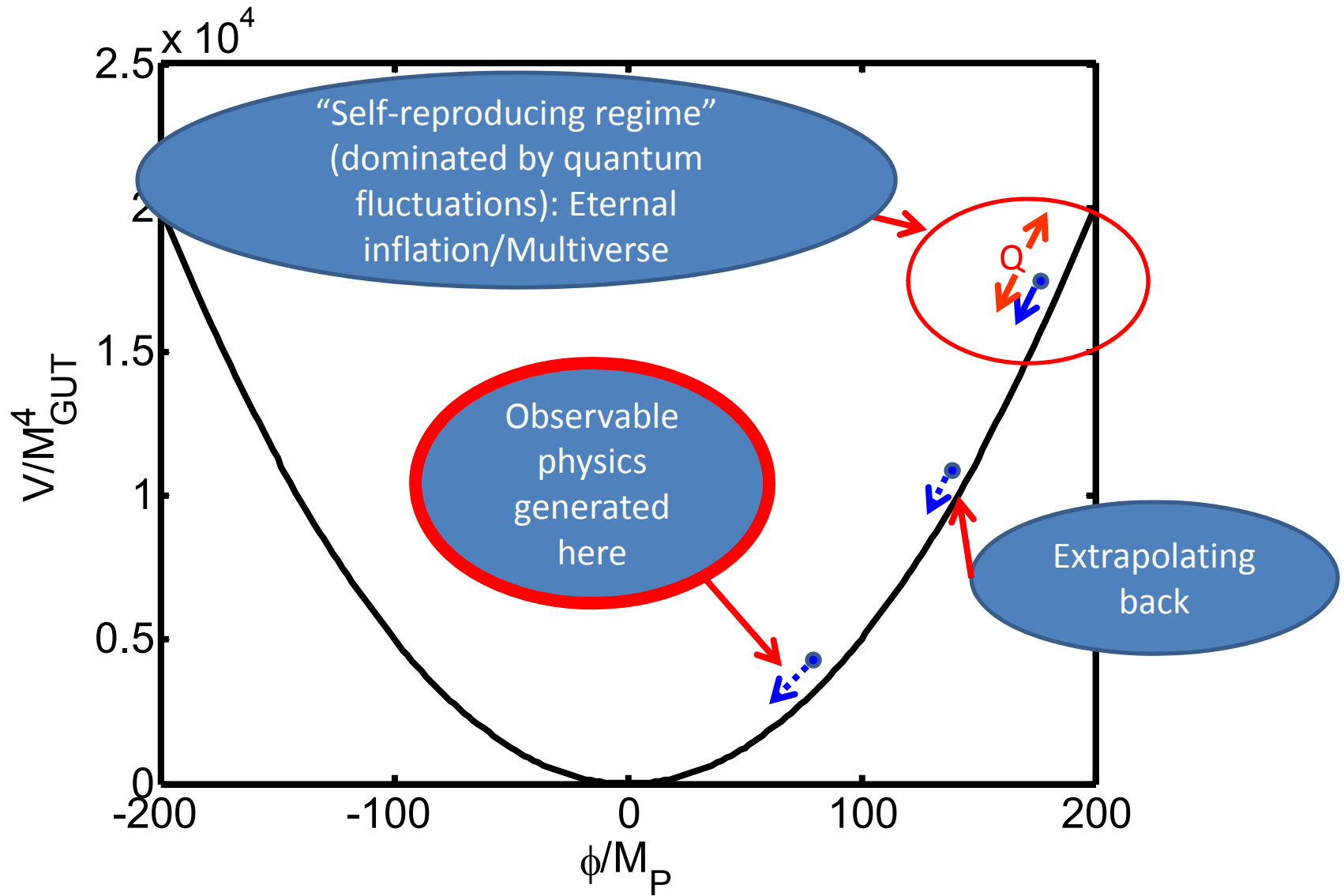
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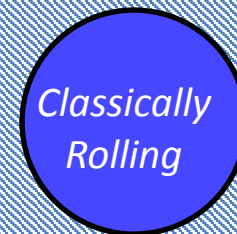


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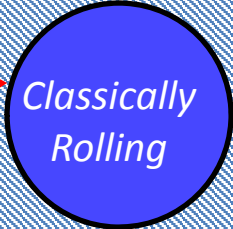
# The multiverse of eternal inflation

*Self-reproduction regime*



# The multiverse of eternal inflation

*Self-reproduction regime*



Where are we? (Young universe,  
old universe, curvature etc)

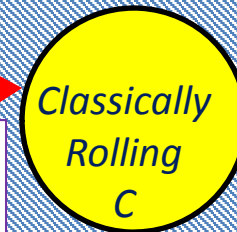
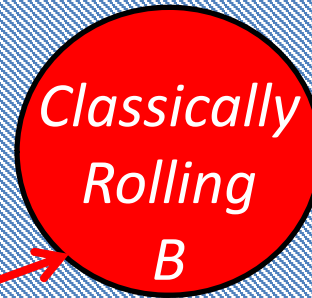
The multiverse of eternal inflation with multiple classical rolling directions

*Self-reproduction regime*



The multiverse of eternal inflation with multiple classical rolling directions

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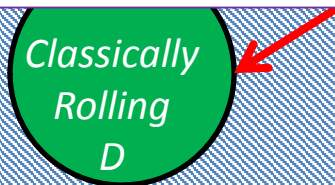
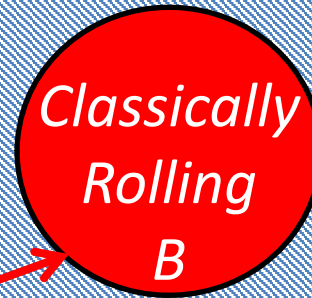


Where are we? (Young universe, old universe, curvature, physical properties A, B, C, D, etc)



The multiverse of eternal inflation with multiple classical rolling directions

*Self-reproduction regime*



Where are we? (Young universe, old universe, curvature, physical properties A, B, C, D, e...)

“Where are we?” →  
Expect the theory to give you a probability distribution in this space... hopefully with some sharp predictions

The multiverse of eternal inflation with multiple classical rolling

String theory landscape even more complicated (e.g. many types of eternal inflation)

Classically Rolling A

Rolling B

Where are we? (Young universe, old universe, curvature, physical properties A, B, C, D, e...)

Classically Rolling D

“Where are we?” →  
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# Challenges for eternal inflation

*“Anything that can happen will happen infinitely many times”*  
(A. Guth)

- 1) Measure Problems ( $\infty/\infty$ )
- 2) Problems defining probabilities
- 3) Problems/hidden assumptions re initial conditions
  - problem claiming generic predictions about state
  - cannot claim “solution to cosmological problems”
  - Related to 2<sup>nd</sup> law, low  $S$  start

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Inflation  $\neq$  Eternal  
Inflation

2<sup>nd</sup> law, low S start

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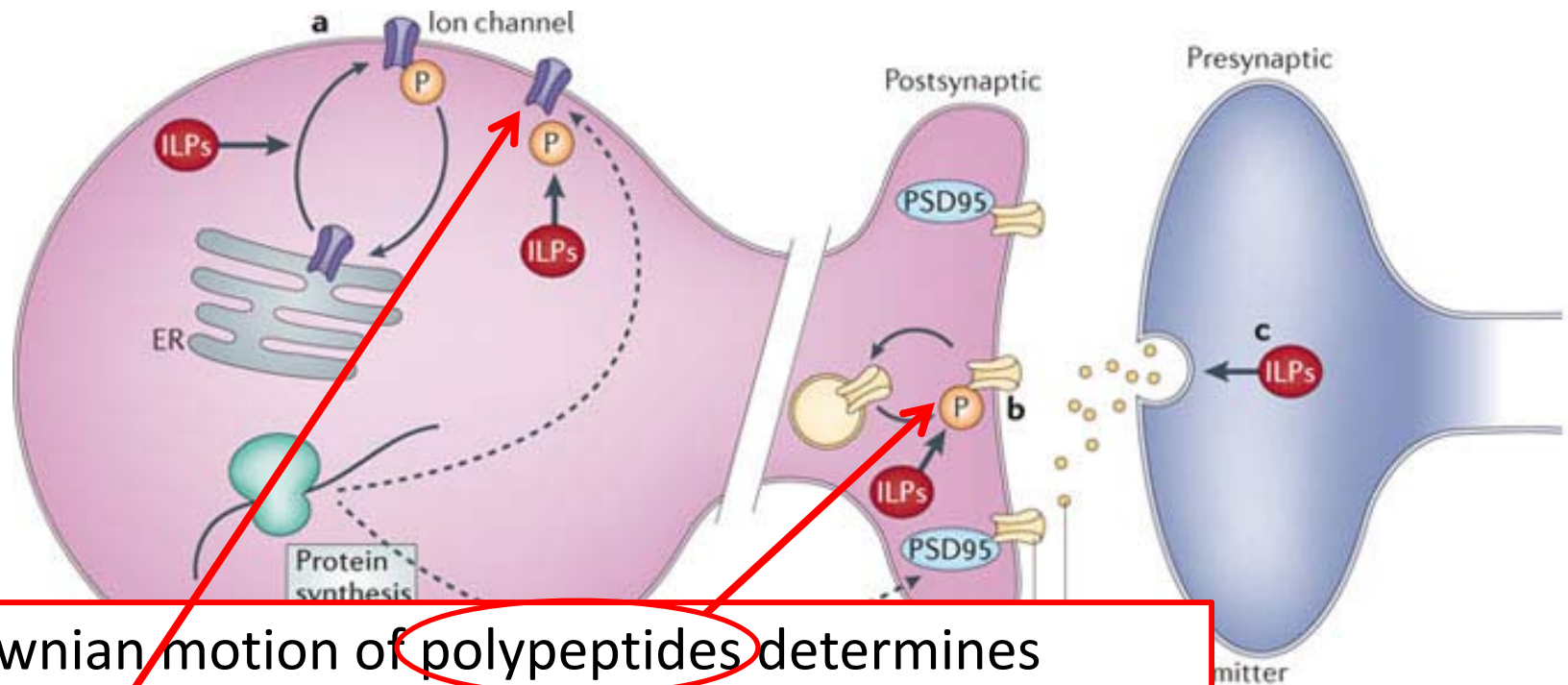
3) Problems/hidden assumptions  
→ problem

Albrecht and Phillips 2014:

- 1) All probabilities are quantum.
- 2) Must expunge purely classical probabilities from discussion of eternal inflation

An important role for Brownian motion  
Uncertainty in neuron transmission times

QUANTUM



Brownian motion of polypeptides determines exactly how many of them are blocking ion channels in neurons at any given time. This is believed to be the dominant source of neuron transmission time uncertainties  $\delta t_n \approx 1ms$

# Analysis of coin flip

$$\delta t_f = \delta t_n \times \left( \frac{v_h}{v_h + v_f} \right)$$

$$\delta t_t = \sqrt{2} \delta t_f$$

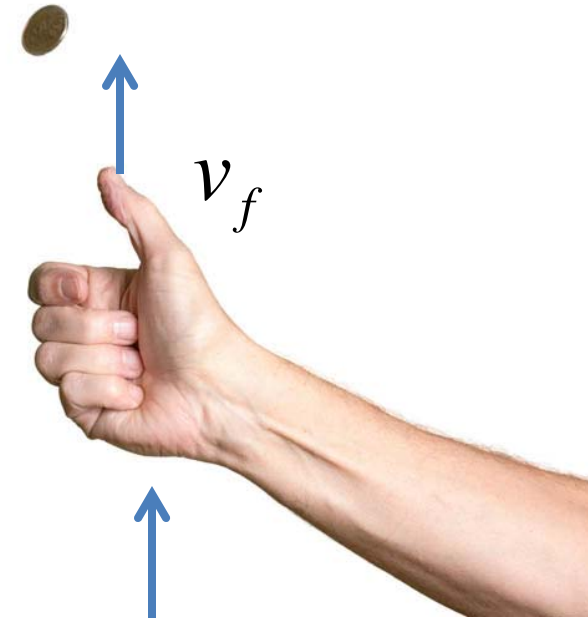
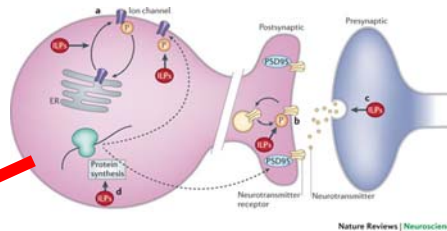
$$f = \frac{4v_f}{\pi d}$$

$$\delta N = f \delta t_t = 0.5$$

Using:

$$\delta t_n \approx 1ms \quad v_h = v_f = 5m/s$$

$$d = 0.01m$$



Coin diameter =  $d$

No "Principle of indifference"



# Challenges for eternal inflation

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→ problem

Possible  
discussion/surprise  
talk topic

Albrecht and Phillips 2014:

- 1) All probabilities are quantum.
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→ problem claiming generic predictions about state

→ cannot claim “solution to cosmological problems”

→ Related to 2<sup>nd</sup> law, low  $S$  start


“But if eternal inflation produces an infinite universe surely it does not matter if the start of inflation is very improbable”

NO


Hernley, AA & Dray  
2013

AA & Sorbo 2004

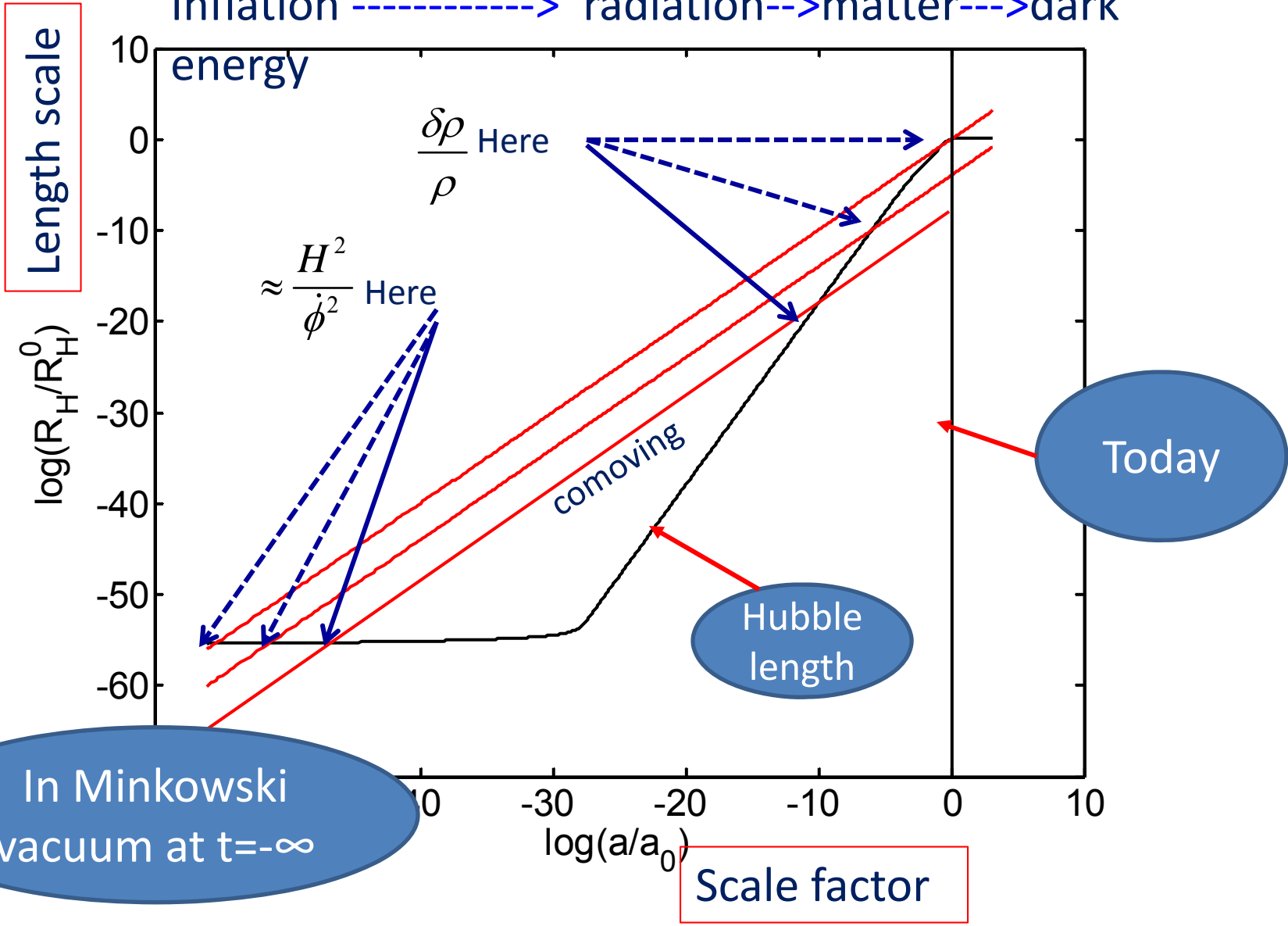
## Outline

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2. Tuning & Entropy
3. Temporal Provincialism
4. Eternal Inflation, measures and probabilities 
5. The Bunch Davies vacuum
6. de Sitter equilibrium cosmology
7. Conclusions

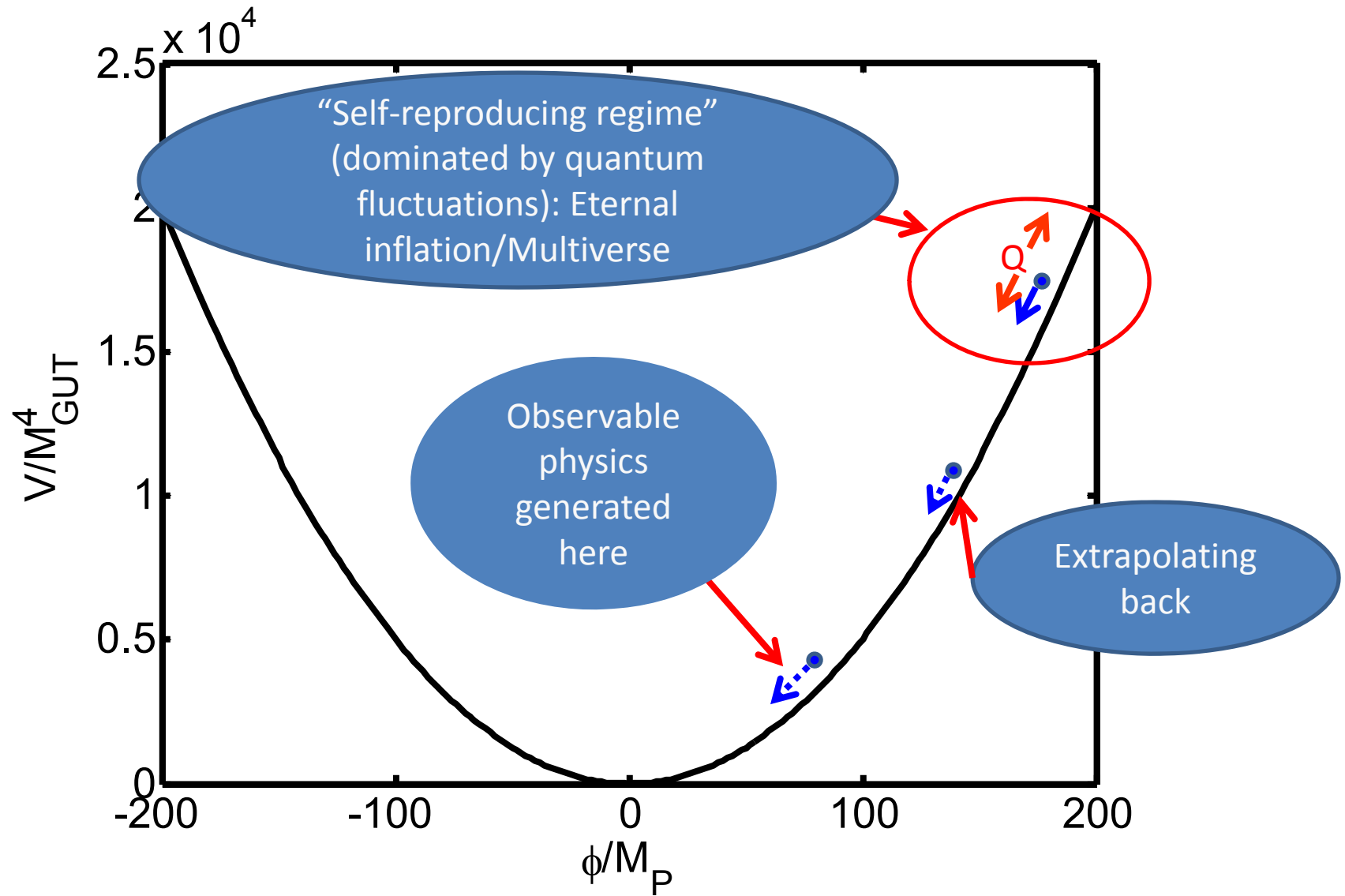
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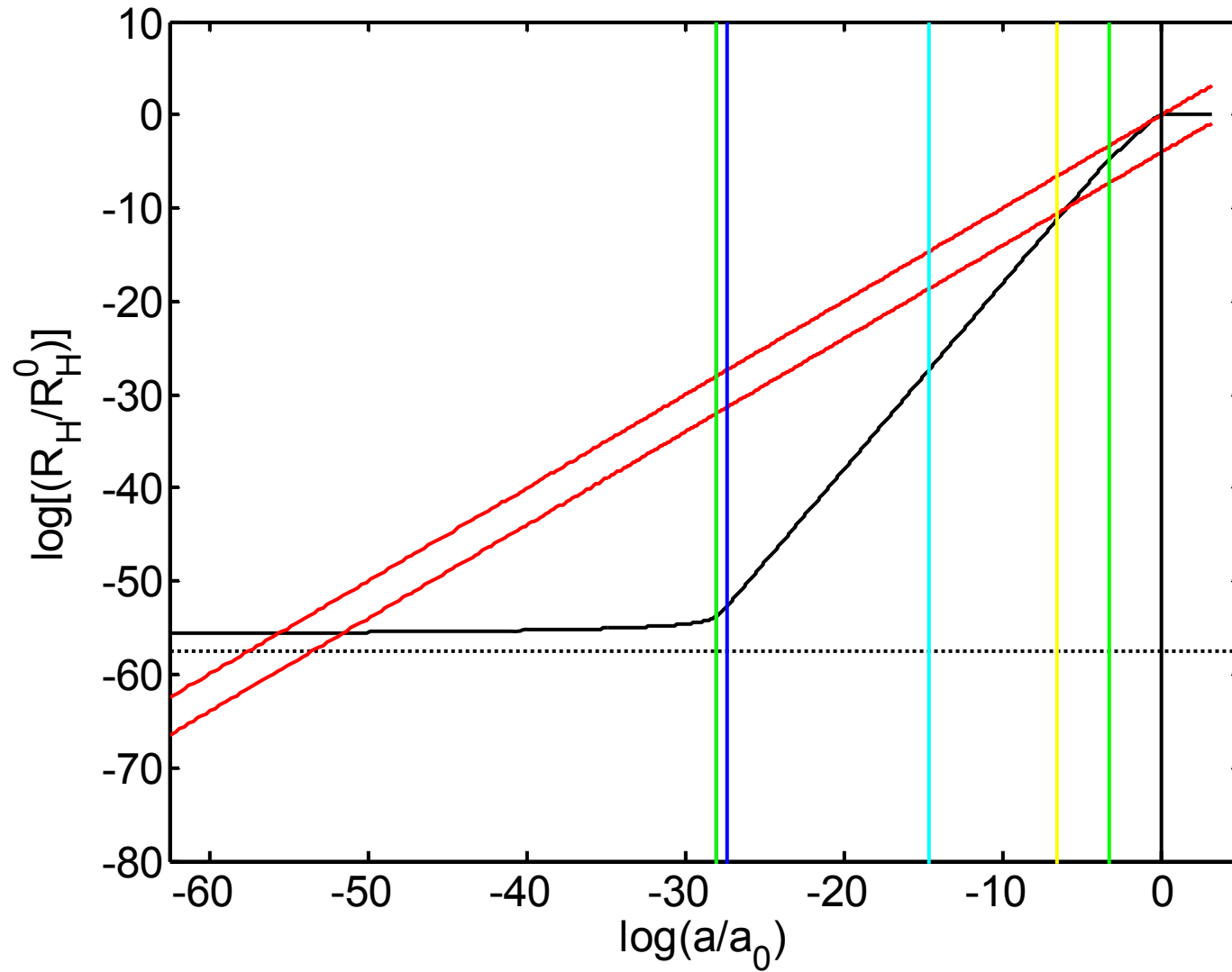
Inflation -----> radiation-->matter--->dark



# Slow rolling of inflaton

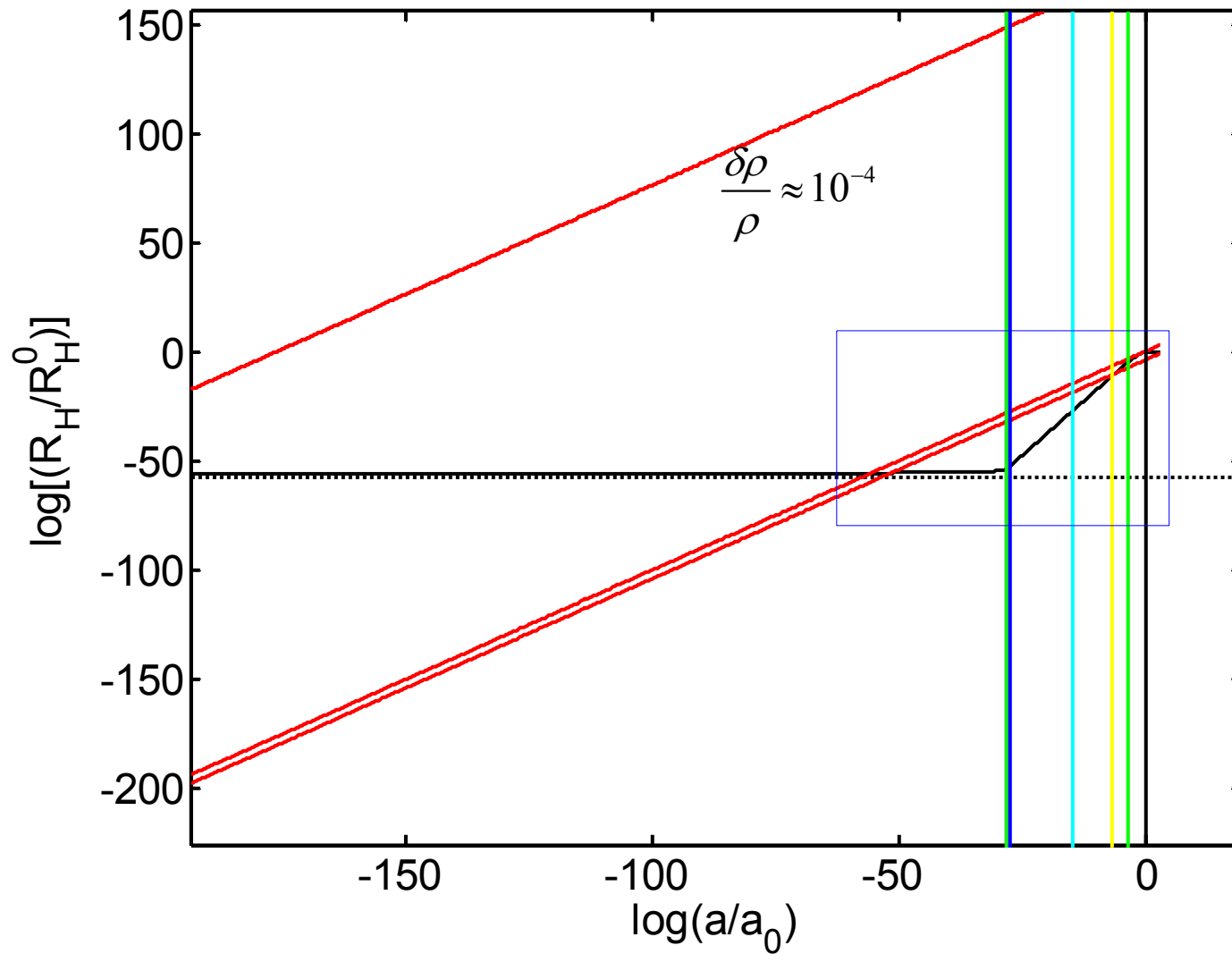


# Evolution of Cosmic Length

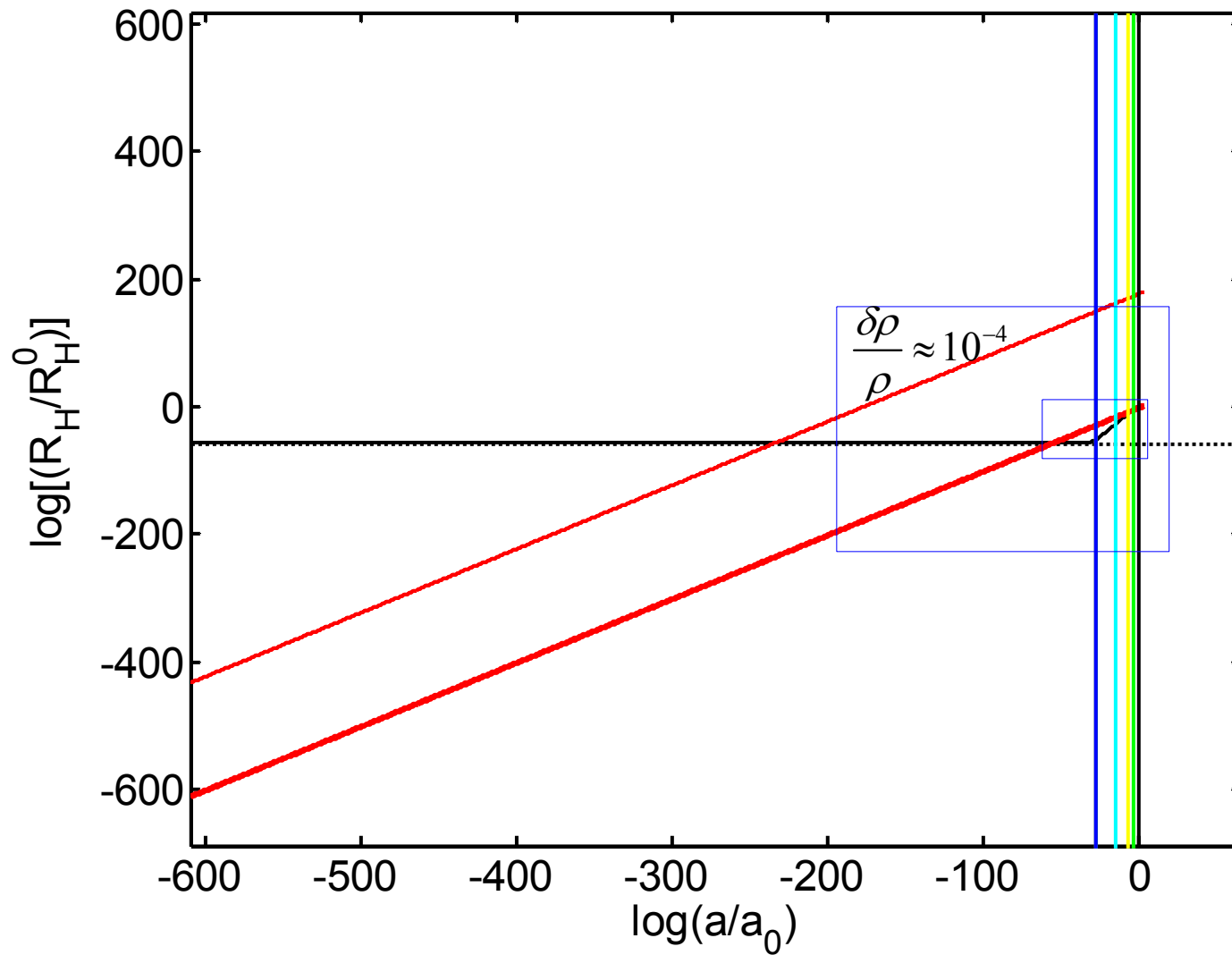




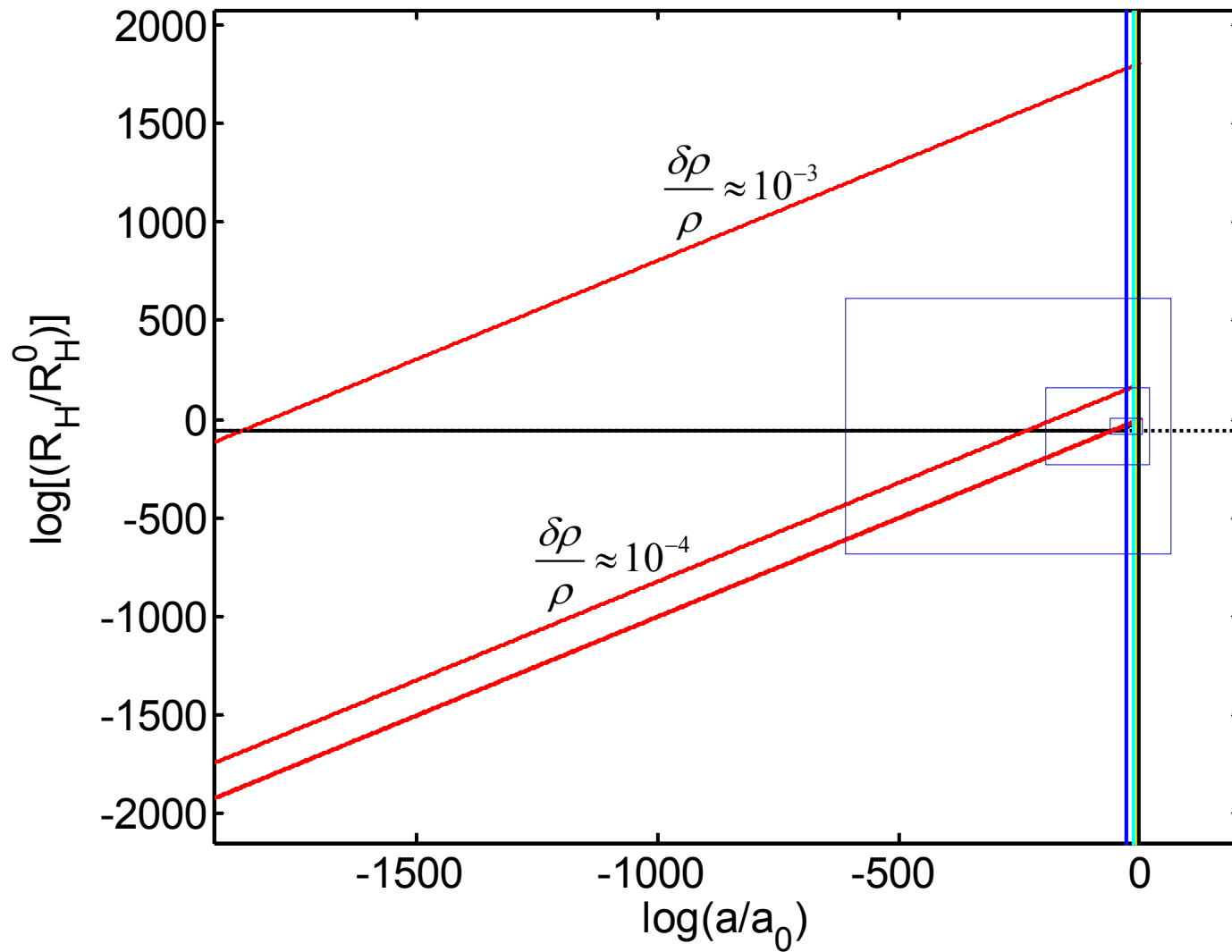
# Evolution of Cosmic Length (zooming out)



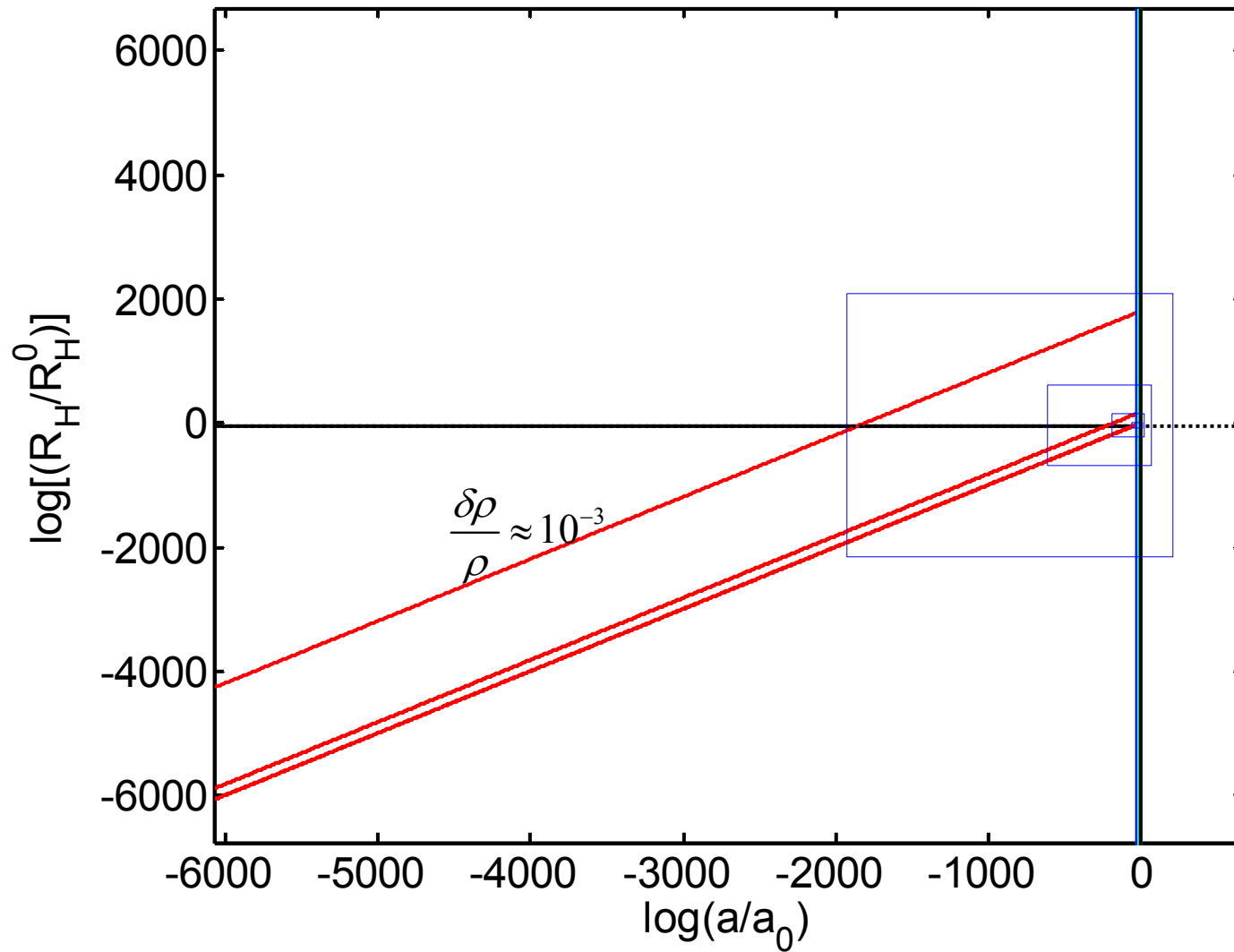
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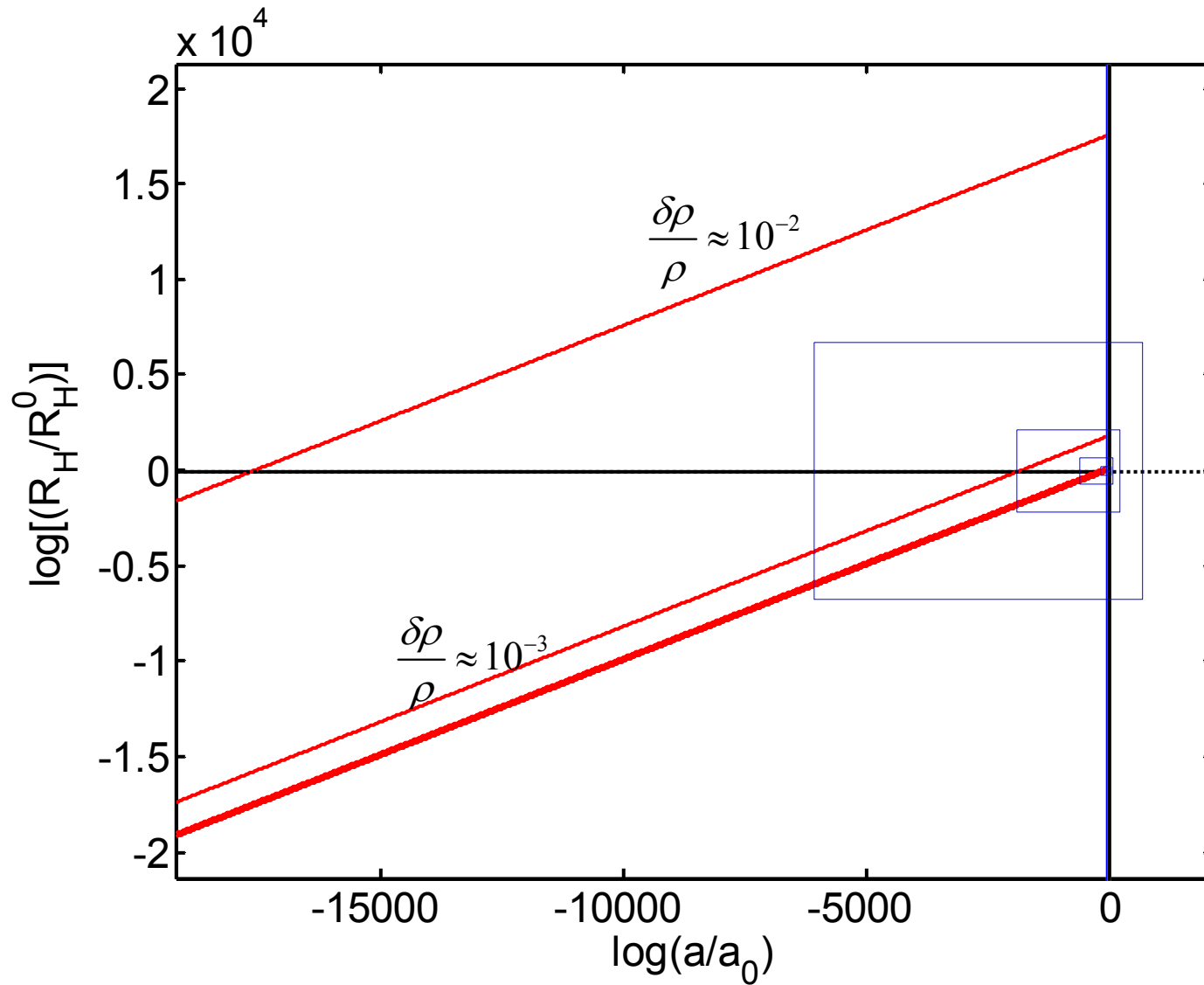
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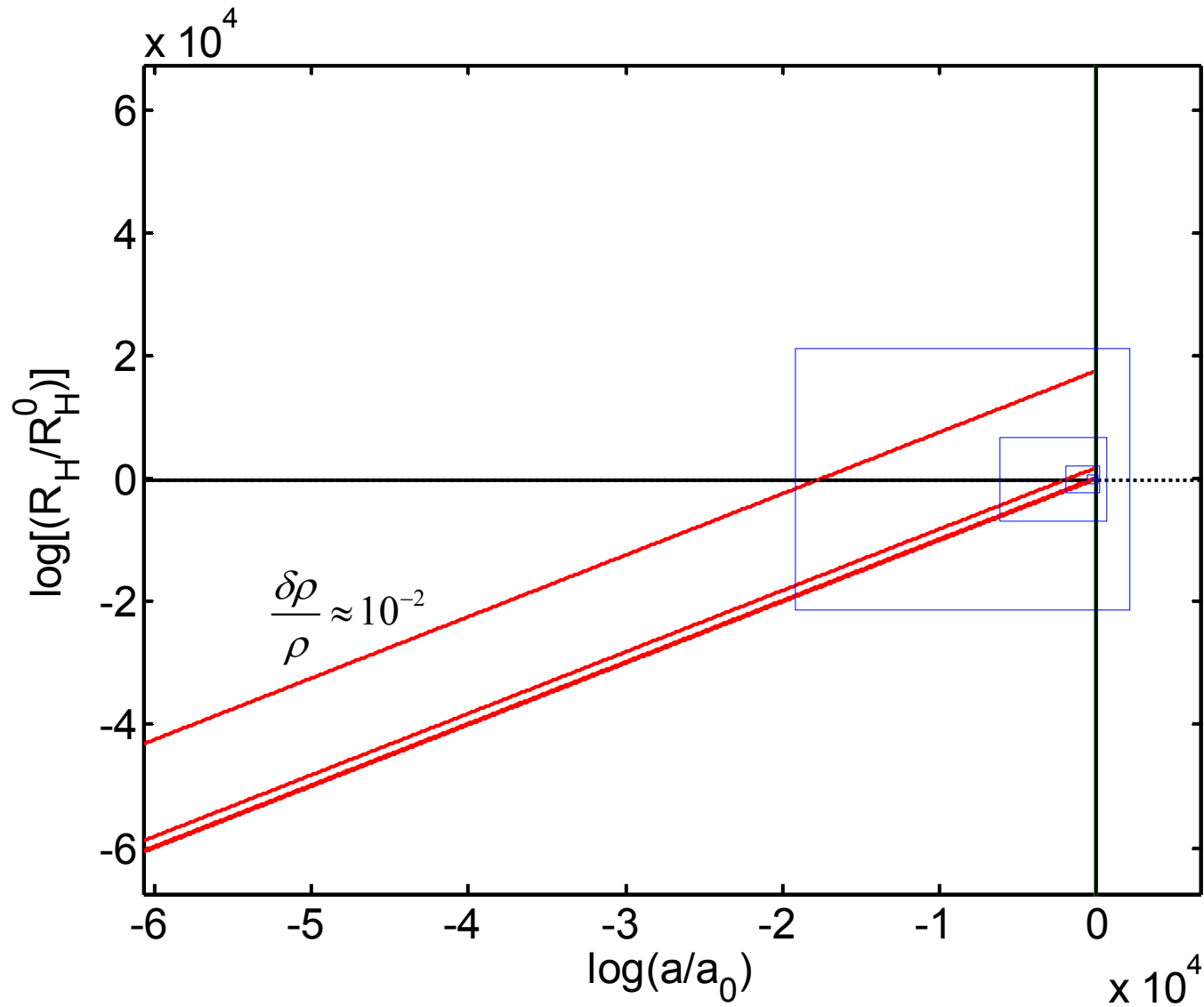
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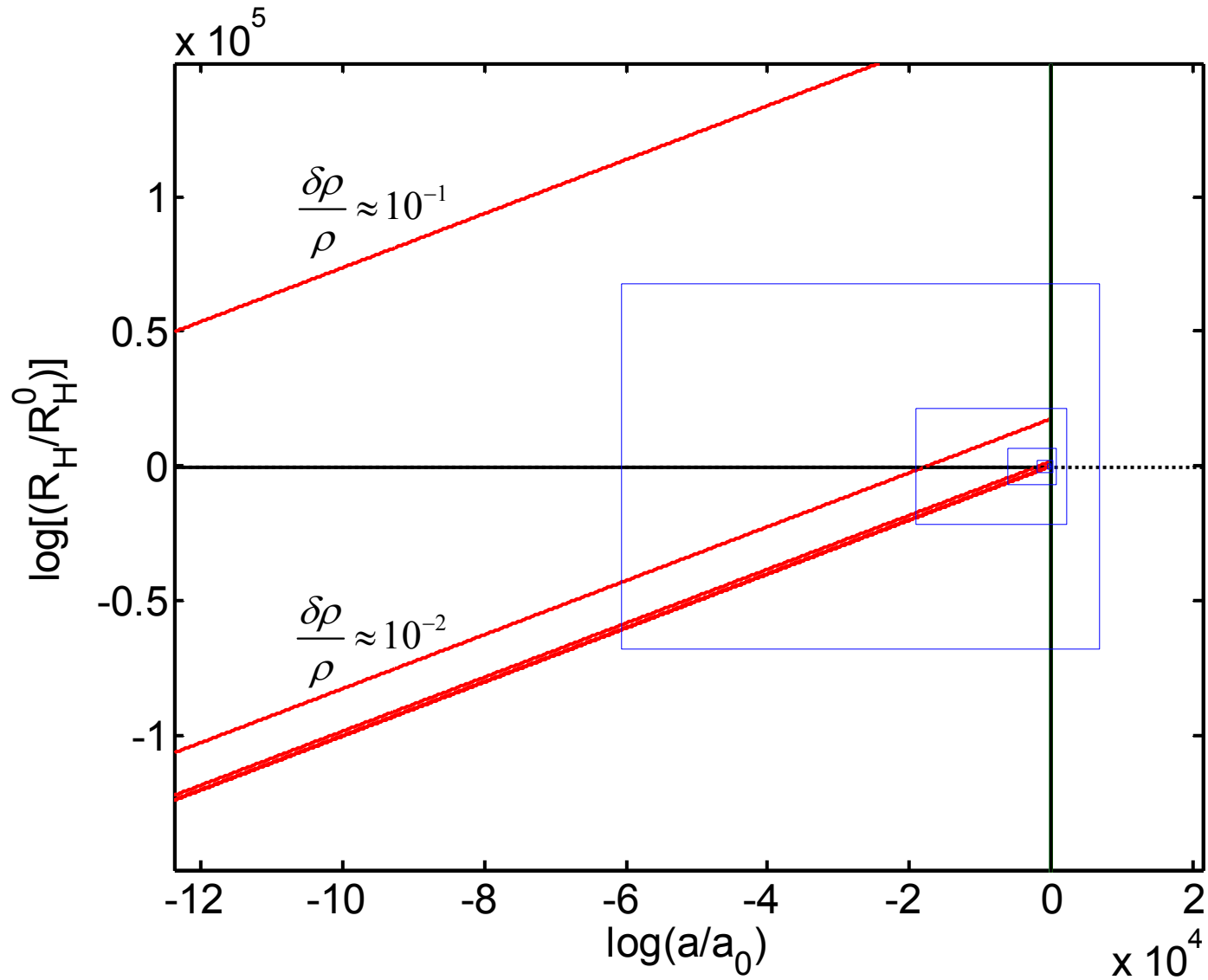
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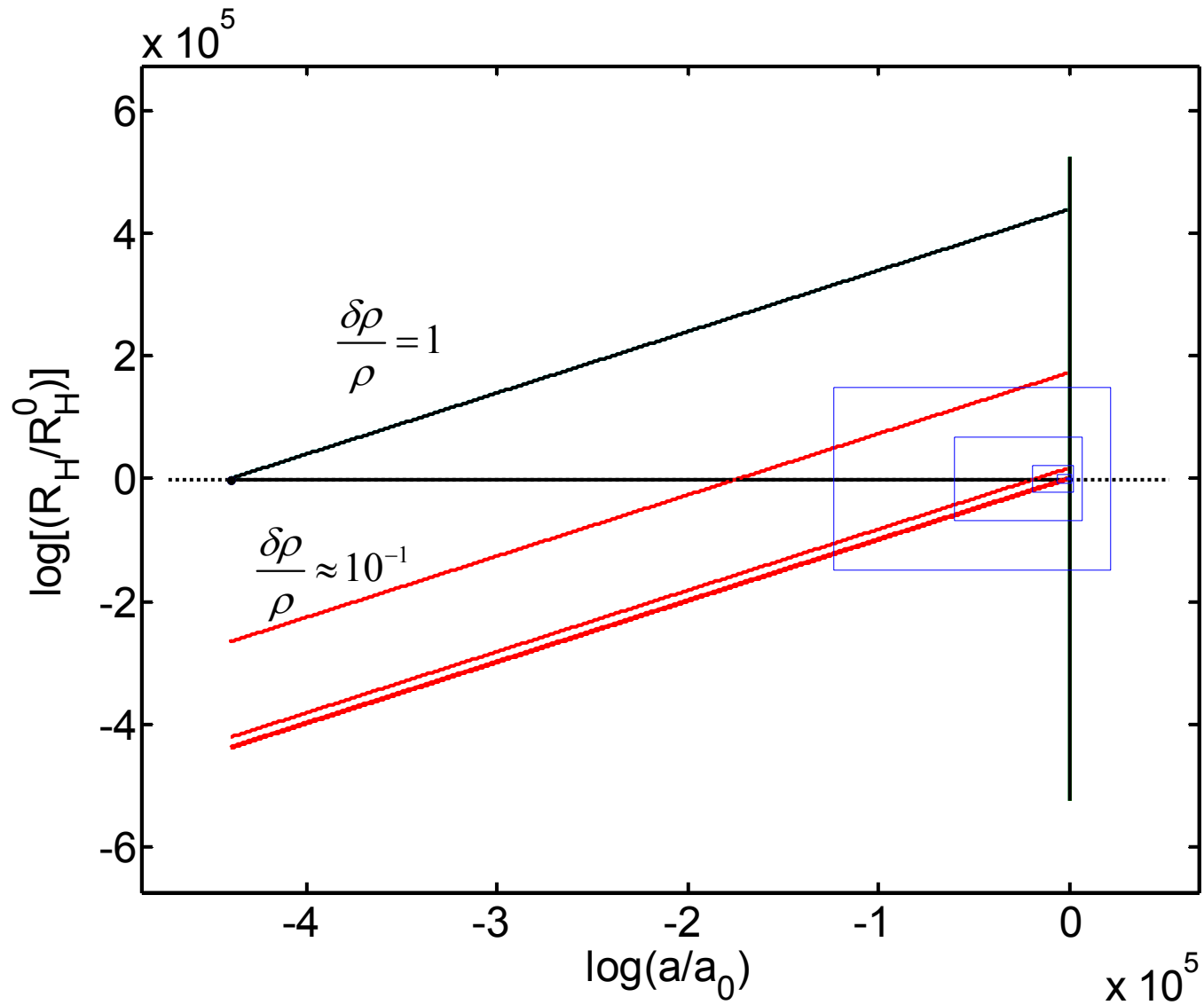
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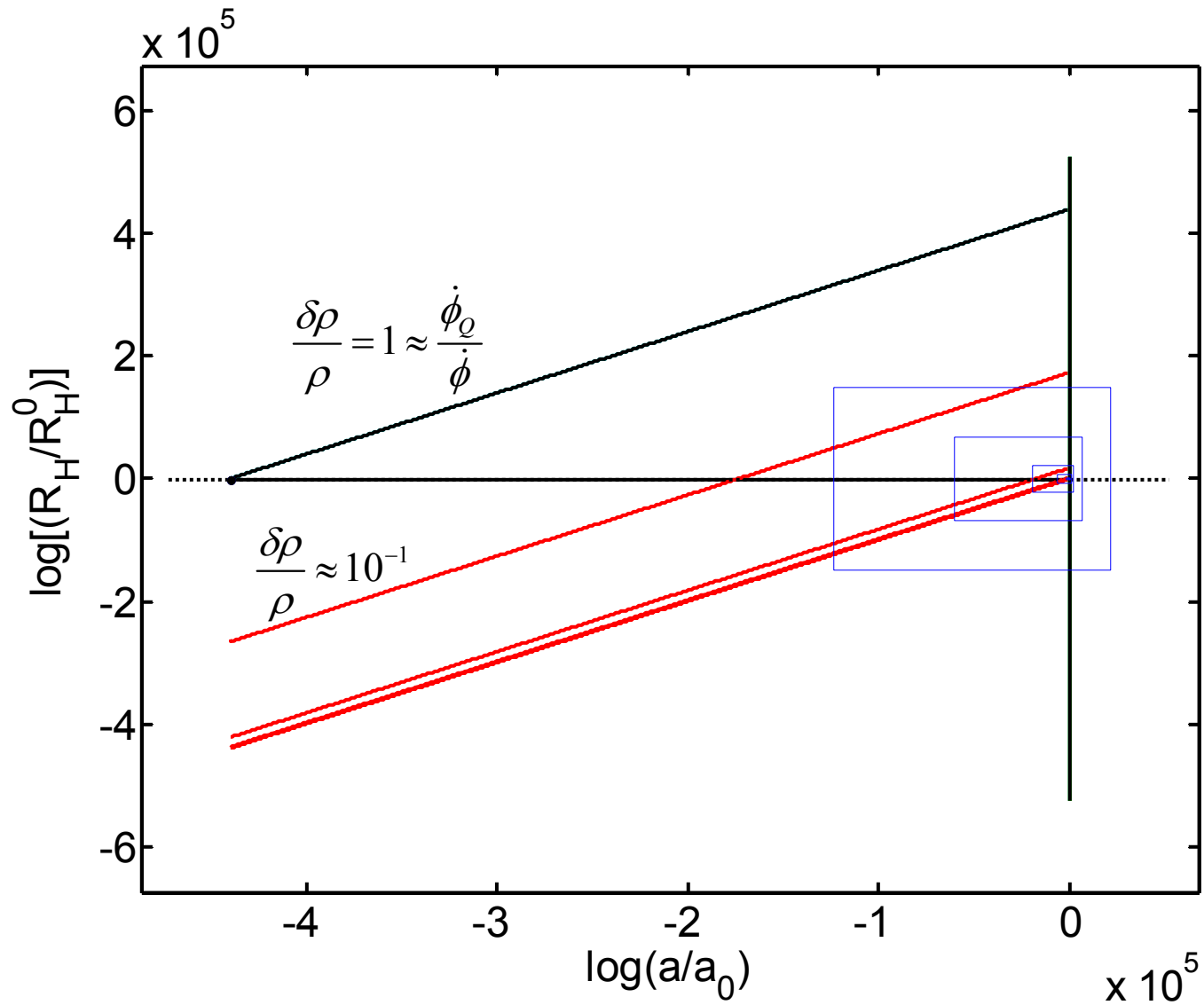


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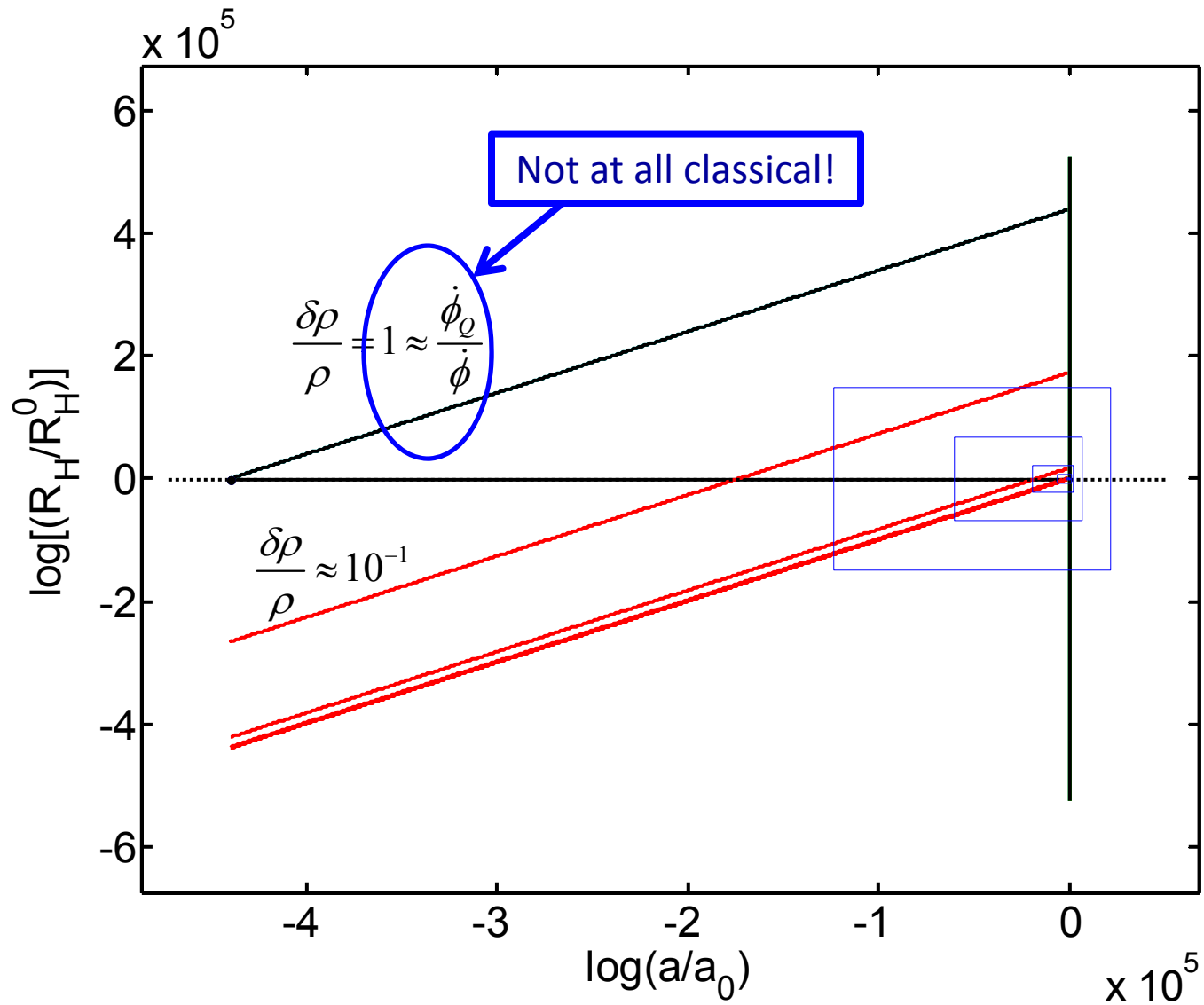


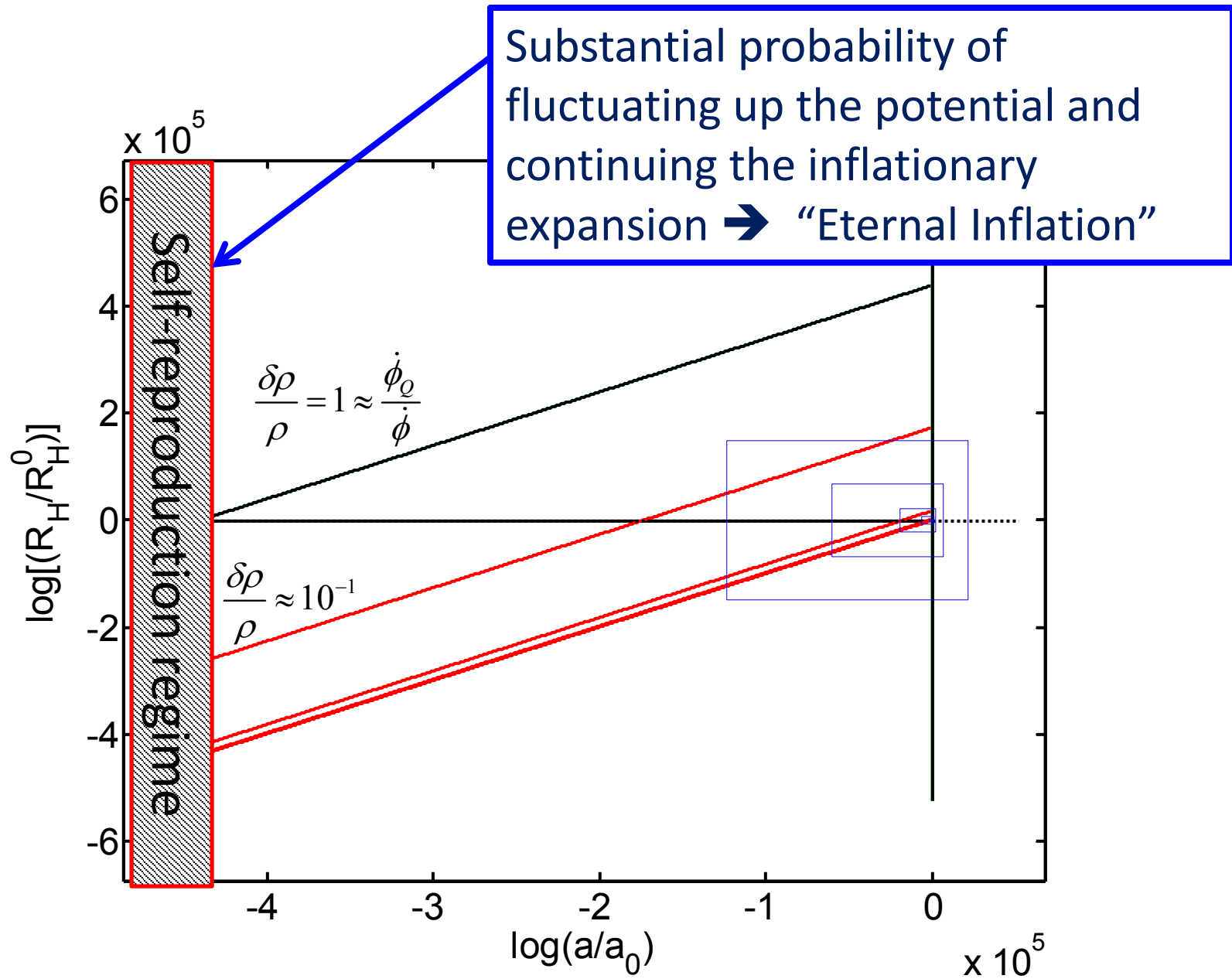


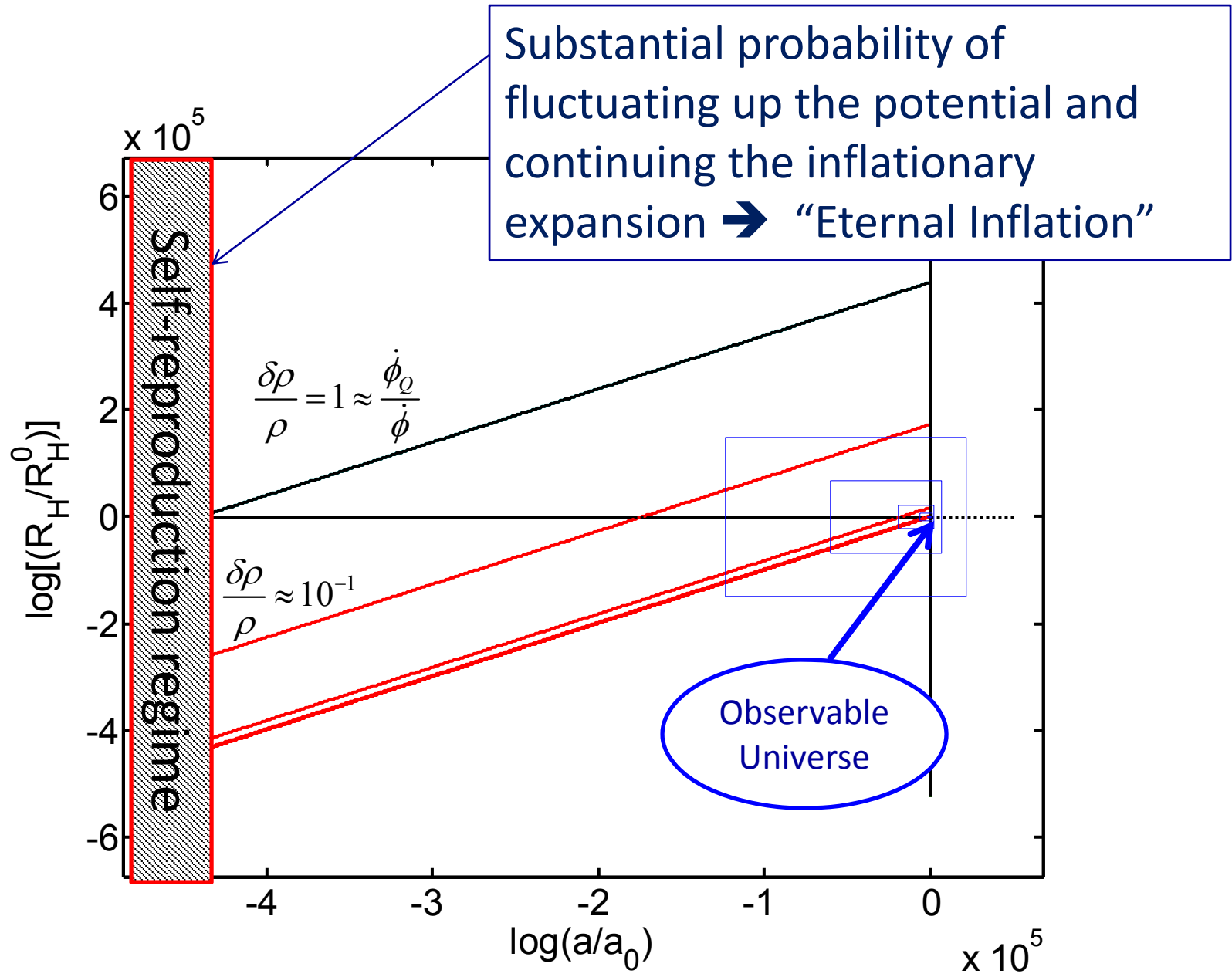
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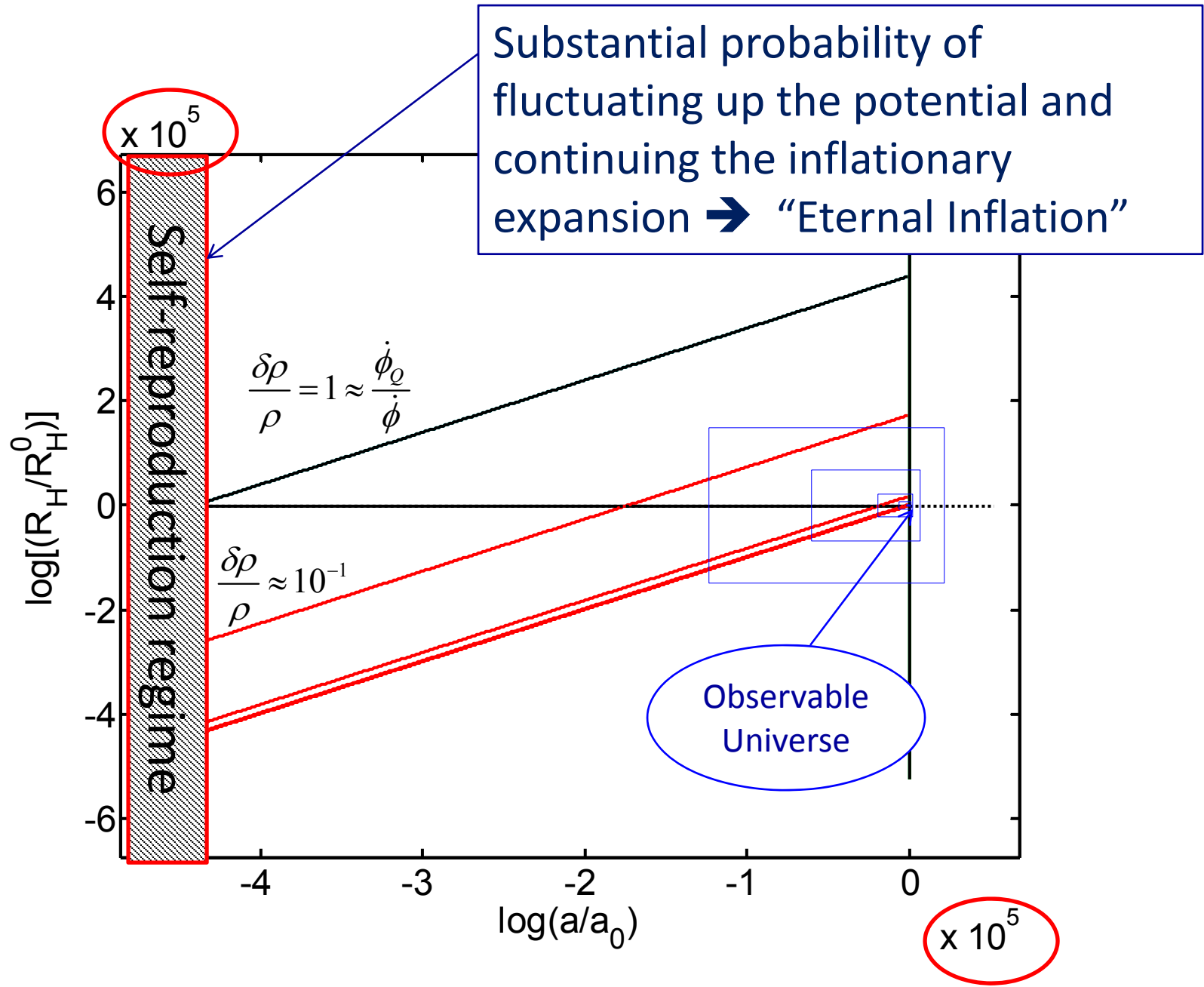


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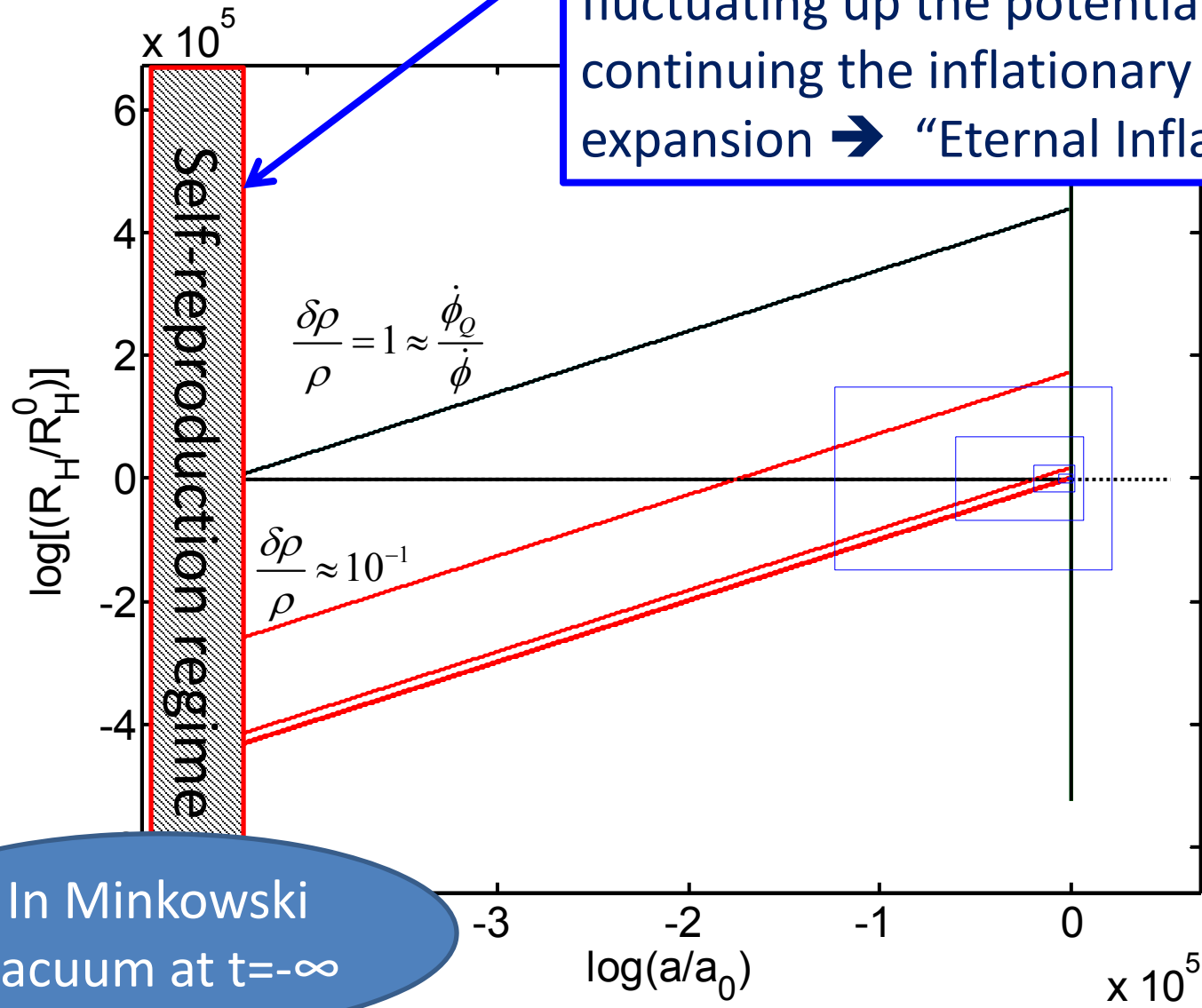




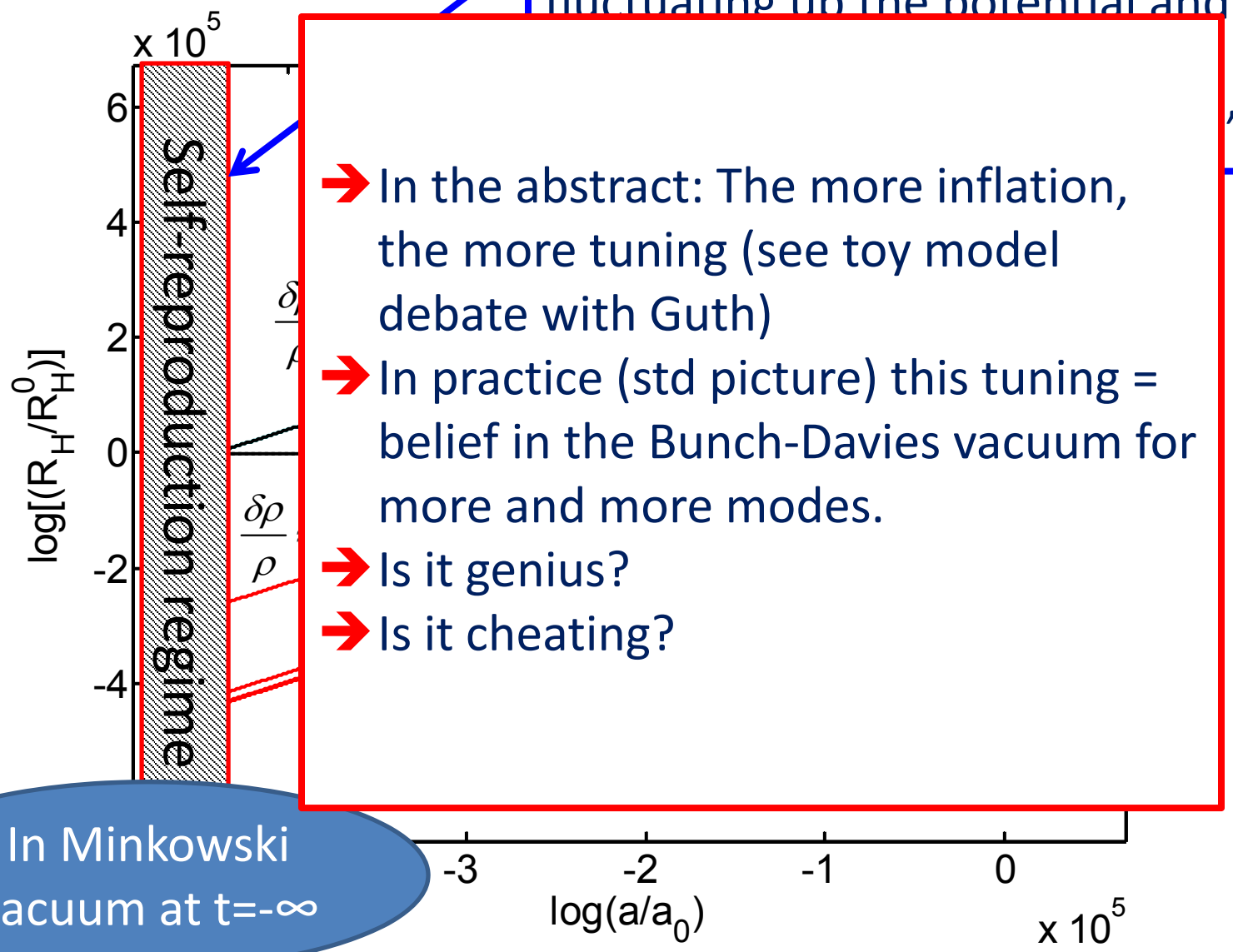




Substantial probability of fluctuating up the potential and continuing the inflationary expansion → “Eternal Inflation”



In Minkowski vacuum at  $t=-\infty$

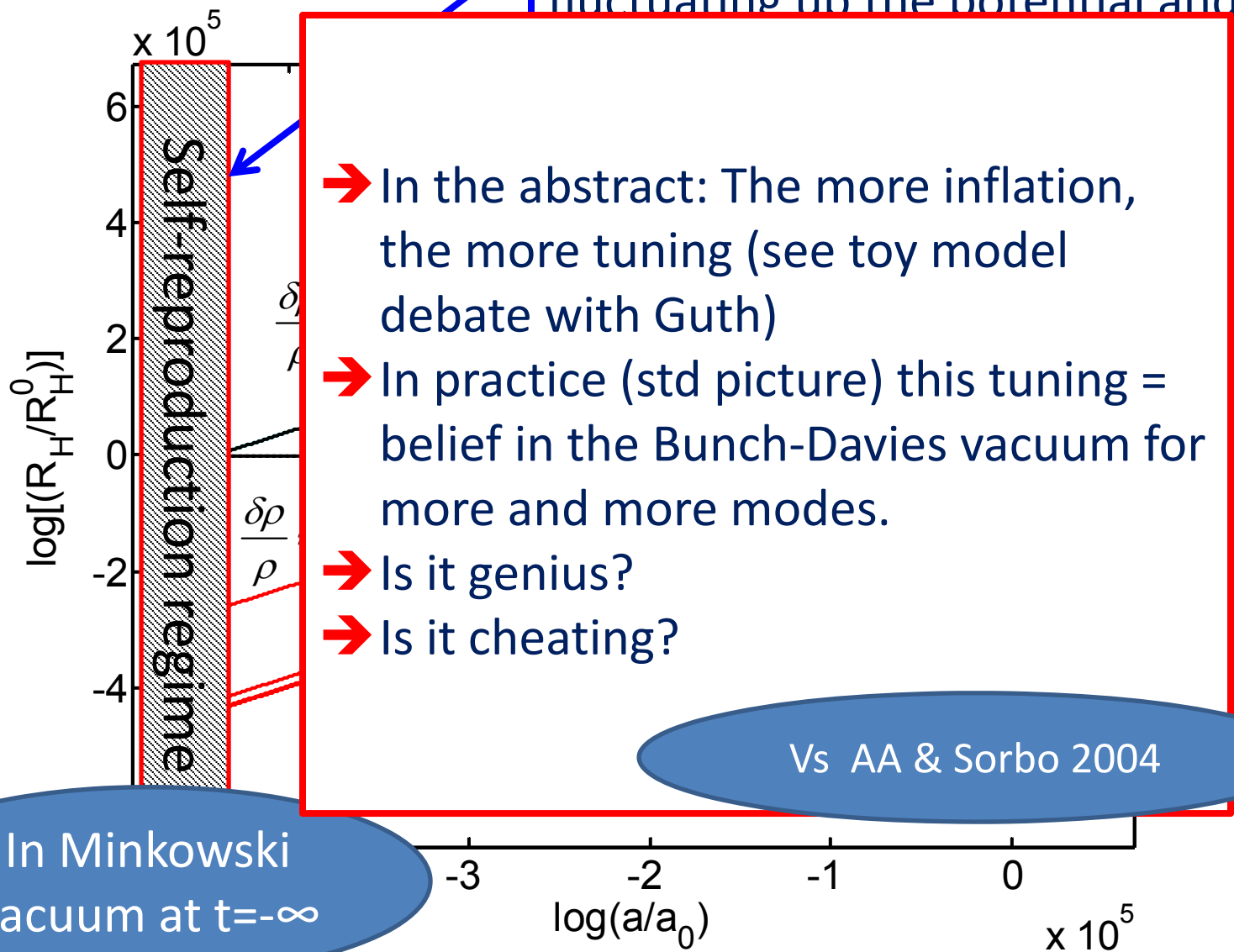


Substantial probability of fluctuating up the potential and

- In the abstract: The more inflation, the more tuning (see toy model debate with Guth)
- In practice (std picture) this tuning = belief in the Bunch-Davies vacuum for more and more modes.
- Is it genius?
- Is it cheating?


In Minkowski vacuum at  $t=-\infty$

Substantial probability of fluctuating up the potential and





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## de Sitter Equilibrium (dSE) cosmology

- Take ideas from Holography,  $\Lambda$  to construct a finite cosmology (beyond EFT)

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In our view, cosmologists should heed mathematician David Hilbert’s warning: although infinity is needed to complete mathematics, it occurs nowhere in the physical Universe.

*J Silk & J. Ellis Nature (2014)*



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AA: *arXiv:1401.7309*

AA: *arXiv:1104.3315*

AA: *arXiv:0906.1047*

AA & Sorbo: *hep-th/0405270* Albrecht CosmoCruise 9/5/15

## Implications of the de Sitter horizon

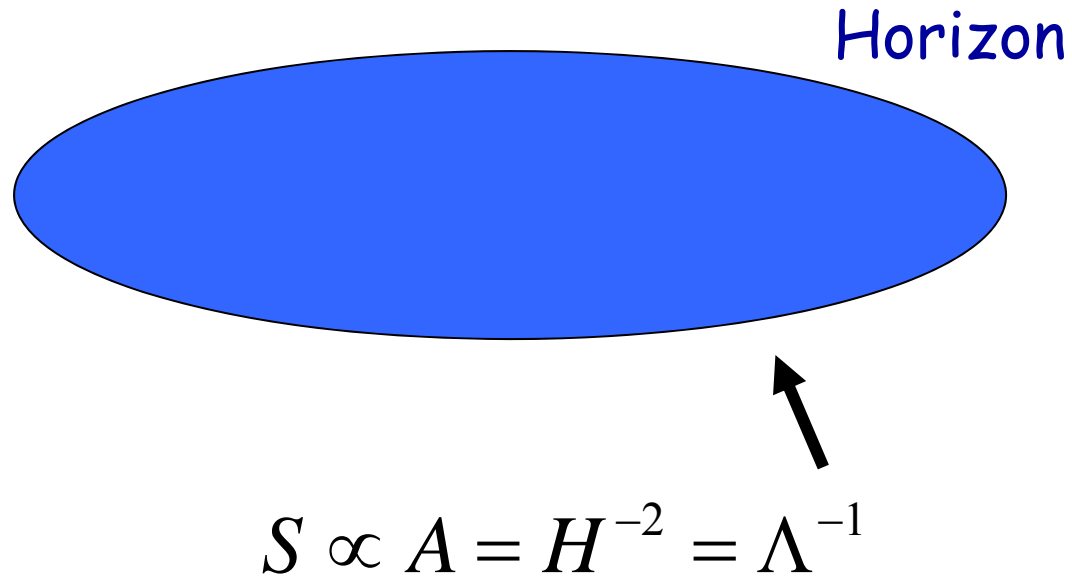
- Maximum entropy

$$S_{\Lambda} \propto A = H_{\Lambda}^{-2} = \left(\frac{\Lambda}{3}\right)^{-1}$$

- Gibbons-Hawking Temperature

$$T_{GH} = H_{\Lambda} = \sqrt{\frac{8\pi G}{3}\rho_{\Lambda}}$$

“De Sitter Space: The ultimate equilibrium for the universe?”



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- Only a finite volume ever observed
- If  $\Lambda$  is truly constant: Cosmology as fluctuating Eqm.
- Maximum entropy  $\longrightarrow$  finite Hilbert space of dimension  $N = e^{S_\Lambda}$  *Banks & Fischler & Dyson et al.*

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dSE cosmology

# Equilibrium Cosmology

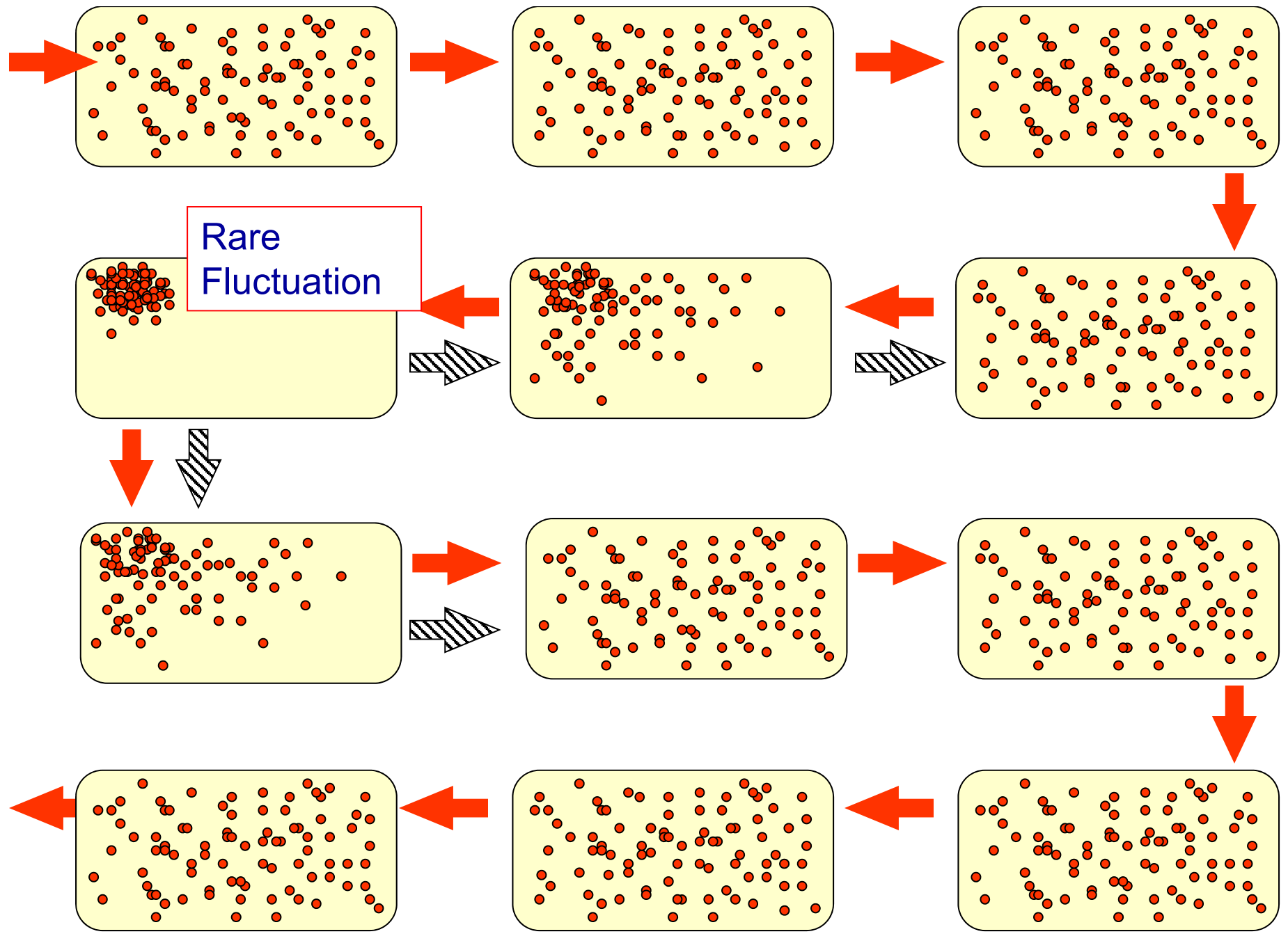
## Equilibrium Cosmology

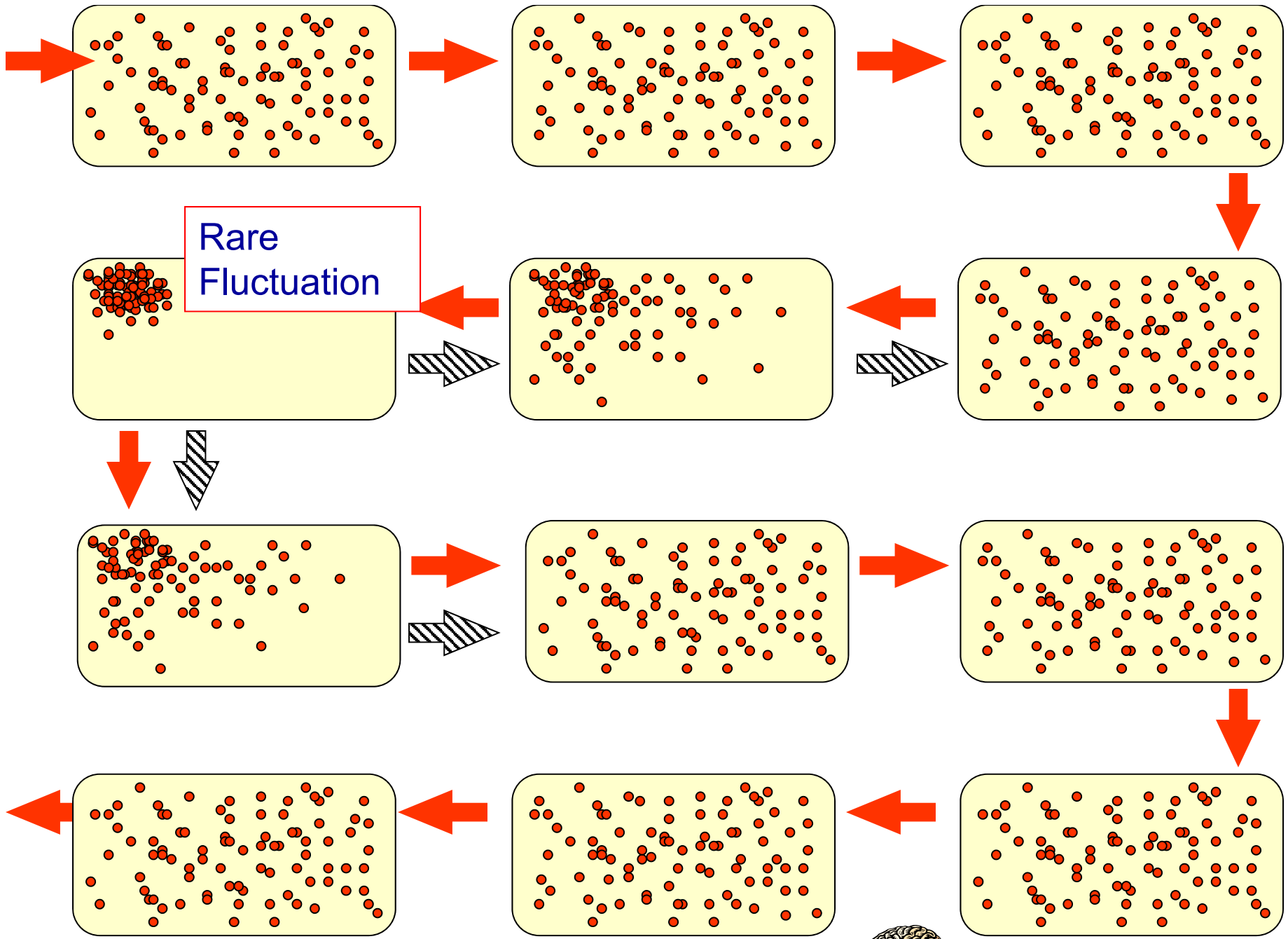
An eqm. theory does not require any theory of initial conditions. The probability of appearing in a given state is given entirely by stat mech, and is thus “given by the dynamics”.

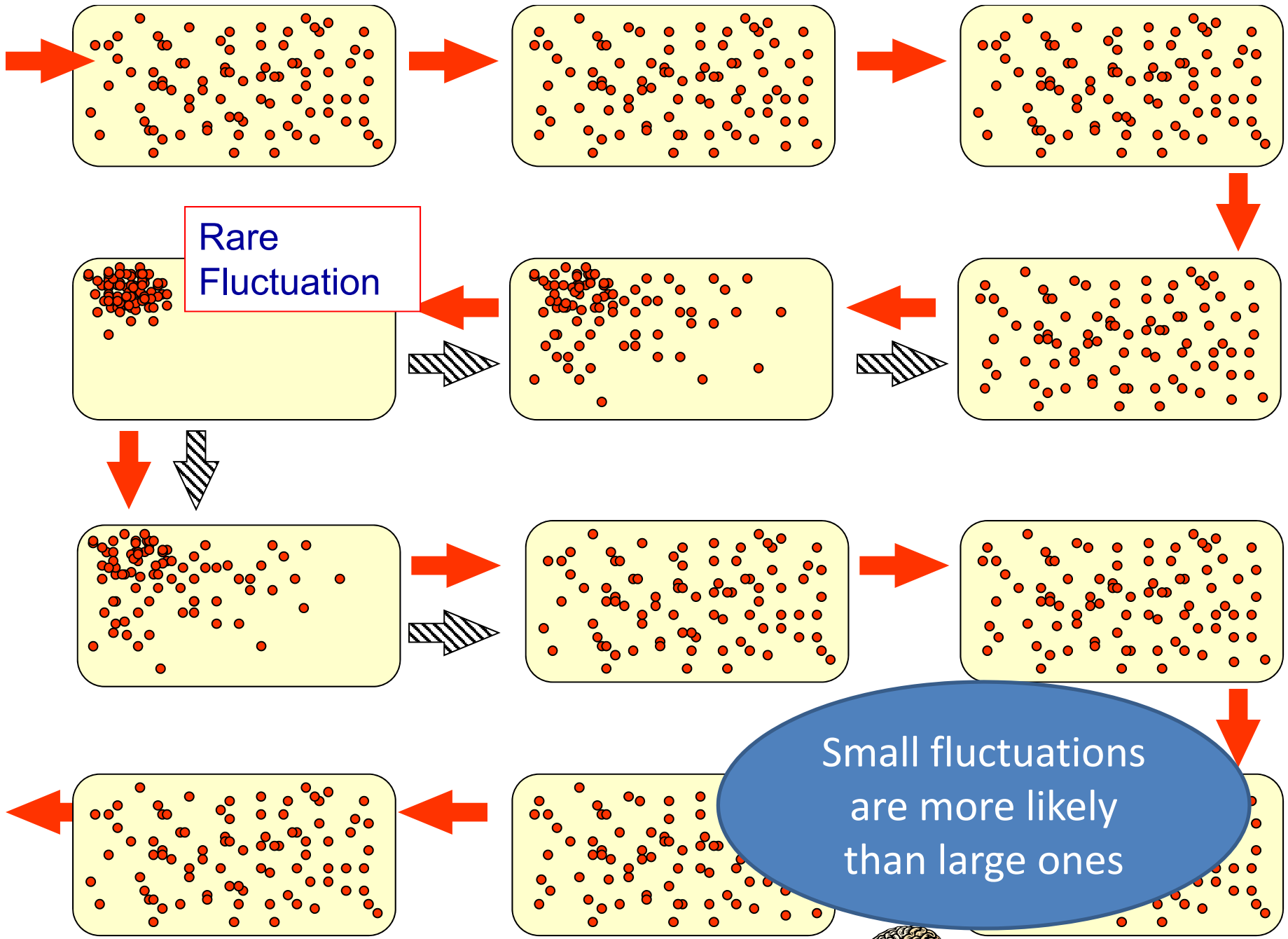
If you know the Hamiltonian you know how to assign probabilities to different states without any special theory of initial conditions.

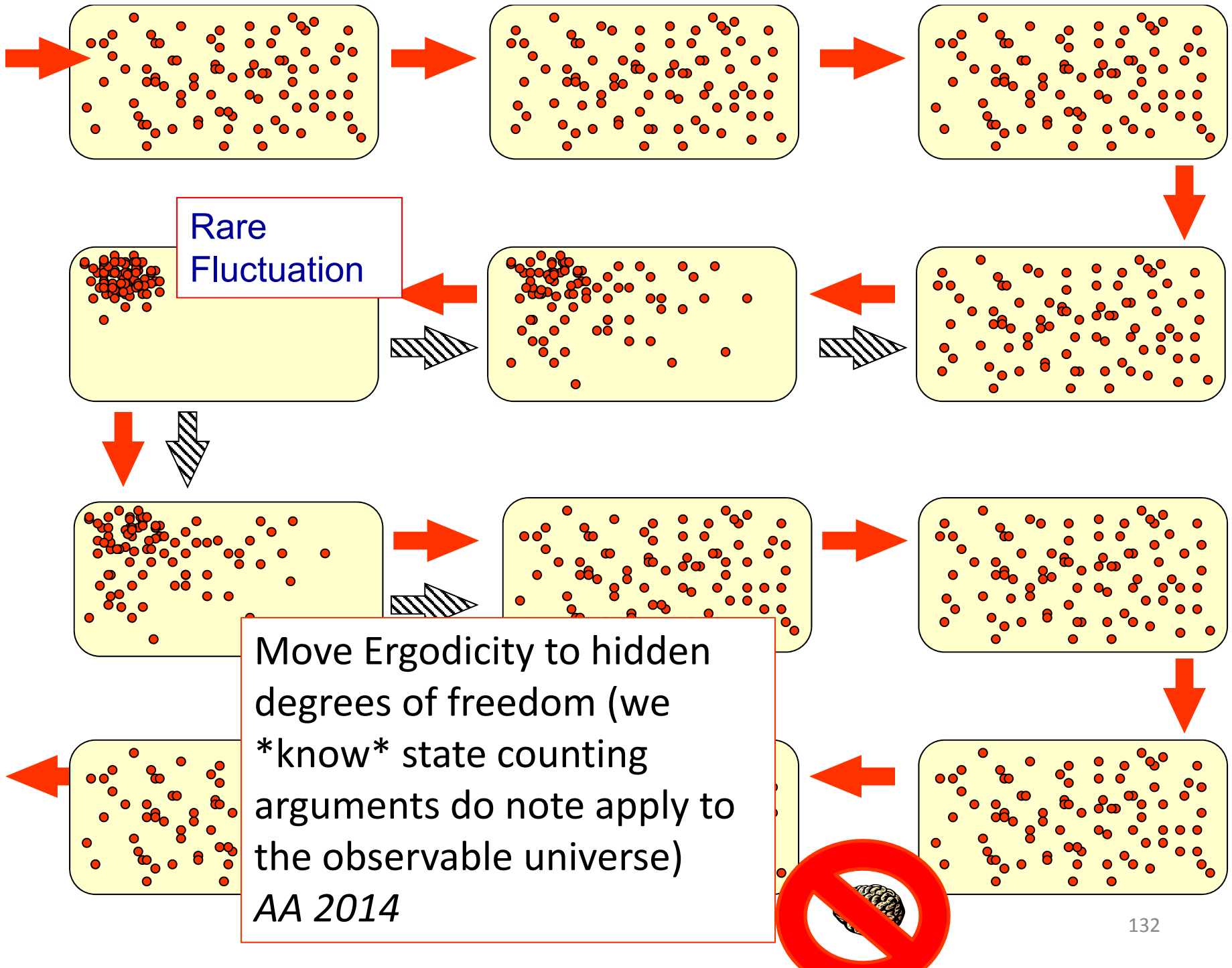
Dyson et al 2002

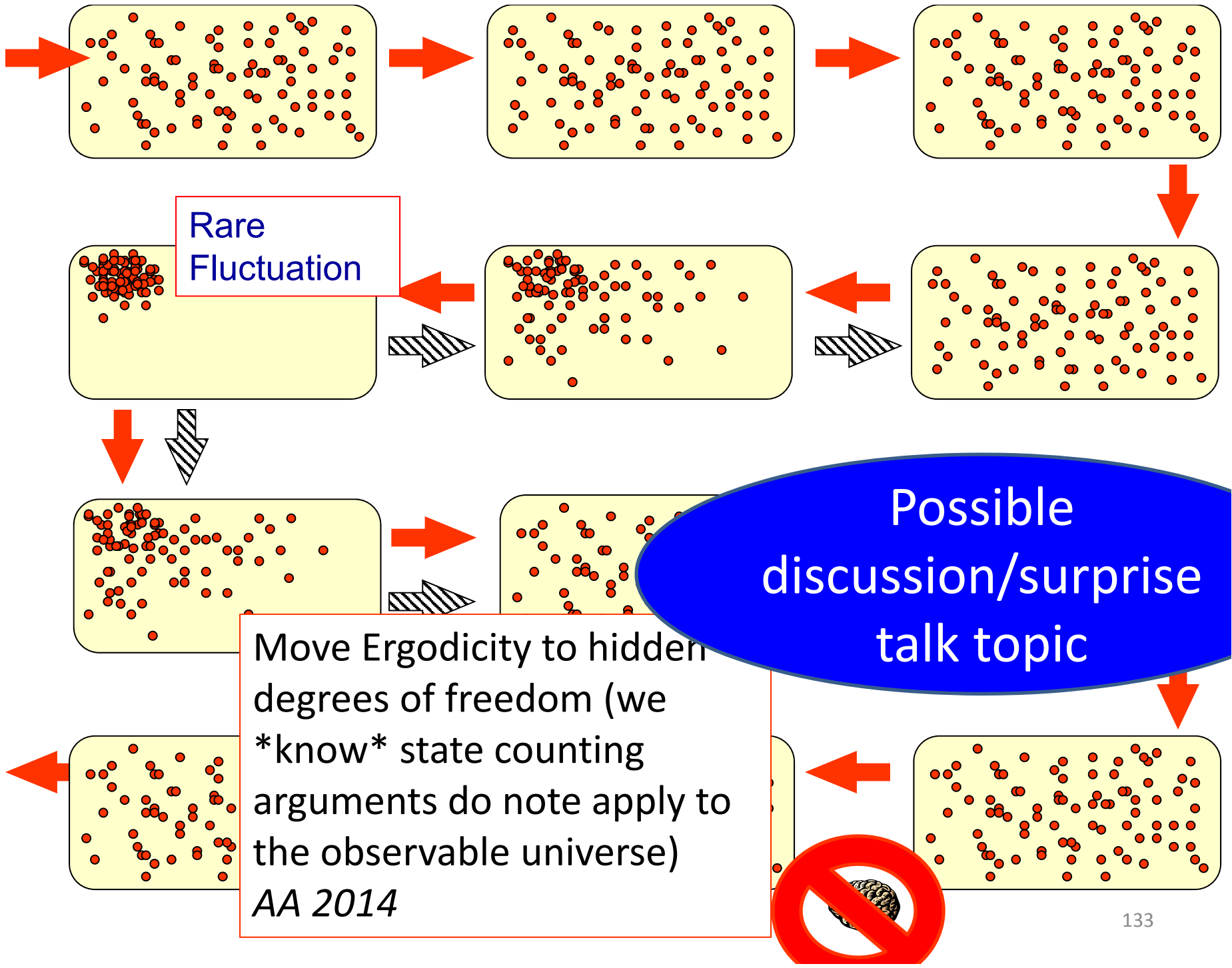




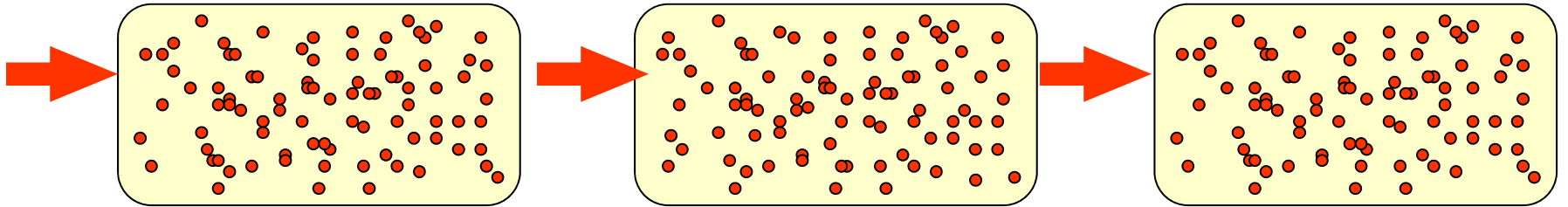




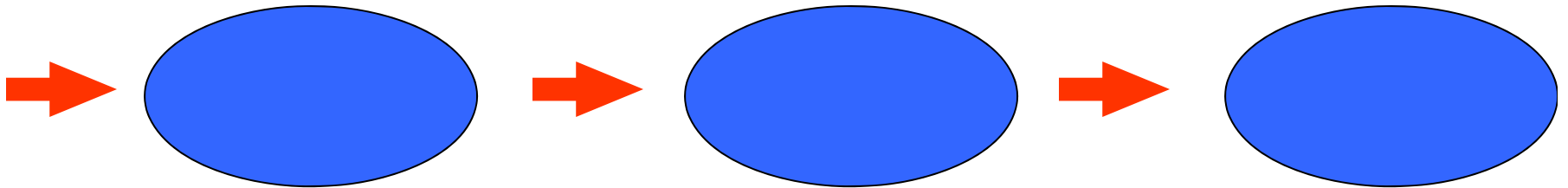




Concept:



Realization:



“de Sitter Space”



## Fluctuating from dSE to inflation:

- The process of an inflaton fluctuating from late time de Sitter to an inflating state is dominated by the “Farhi-Guth Guven” (FGG) process
- A “seed” is formed from the Gibbons-Hawking radiation that can then tunnel via the Guth-Farhi instanton.
- Rate is well approximated by the rate of seed formation:

$$\propto e^{-\frac{m_s}{T_{GH}}} = e^{-\frac{m_s}{H_\Lambda}}$$

- Seed mass:

$$m_s = \rho_I (cH_I^{-1})^3 = 0.0013kg \left( \frac{(10^{16} GeV)^4}{\rho_I} \right)^{1/2}$$



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Small seed can produce an entire universe →  
Evade “Boltzmann Brain” problem

Albrecht CosmoCruise 9/5/15



## Fluctuating from dSE to inflation:

- The process of an inflaton fluctuating from late time de Sitter to an inflationary state is dominated by the

“Farhi”

- A “Farhi” fluctuation plays the role we always thought it could play:

Makes a whole universe out of one easy to achieve fluctuation.

- Seed mass:

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## Fluctuating from dSE to inflation:

- The process of an inflaton fluctuating from late time de Sitter to an inflating state

“Farhi-Guth Guven” (FGG)

*M → 0 not a problem for G-F process (A. Ulvestad & AA 2012)*

- A “seed” is formed from the Gibbons-Hawking radiation that can then tunnel through an instanton.

*See also Freivogel et al 2006, Banks 2002*

- Rate is well approximated by the rate of seed formation:

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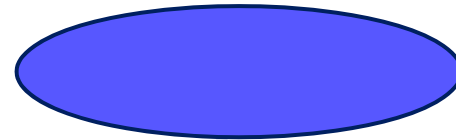
Time

Events

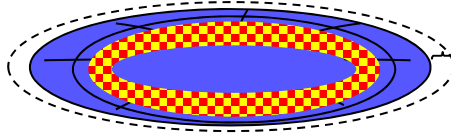
De Sitter-like spacetime

Baby Universe

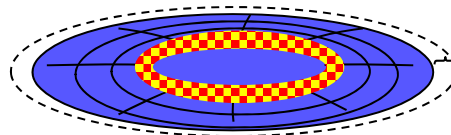
Eqm.



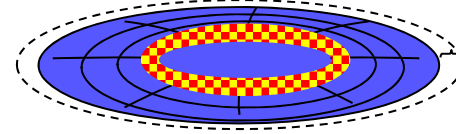
Seed  
Fluctuation



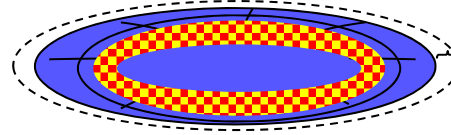
Tunneling



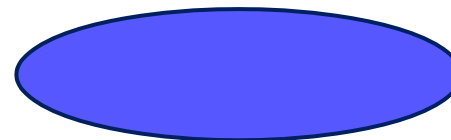
Evolution



Evolution



de Sitter  
&  
Recoupling &  
Equilibration



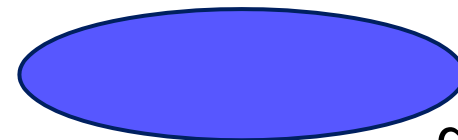
Inflation



Radiation

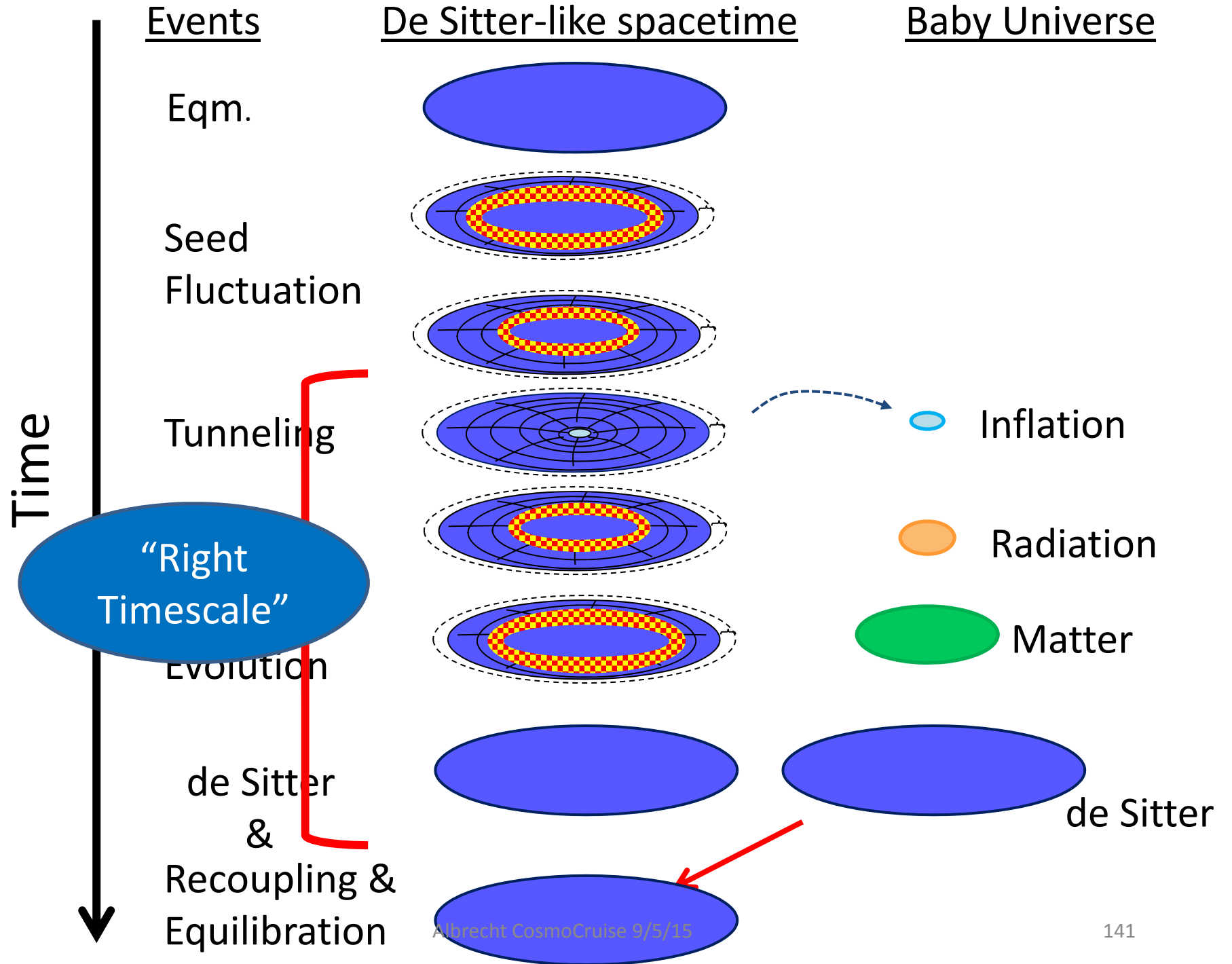


Matter



de Sitter






## Implications of finite Hilbert space $N = e^{S_\Lambda}$

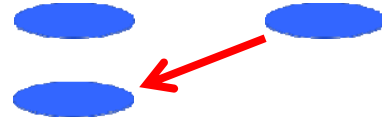
- Recurrences
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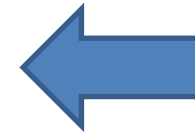
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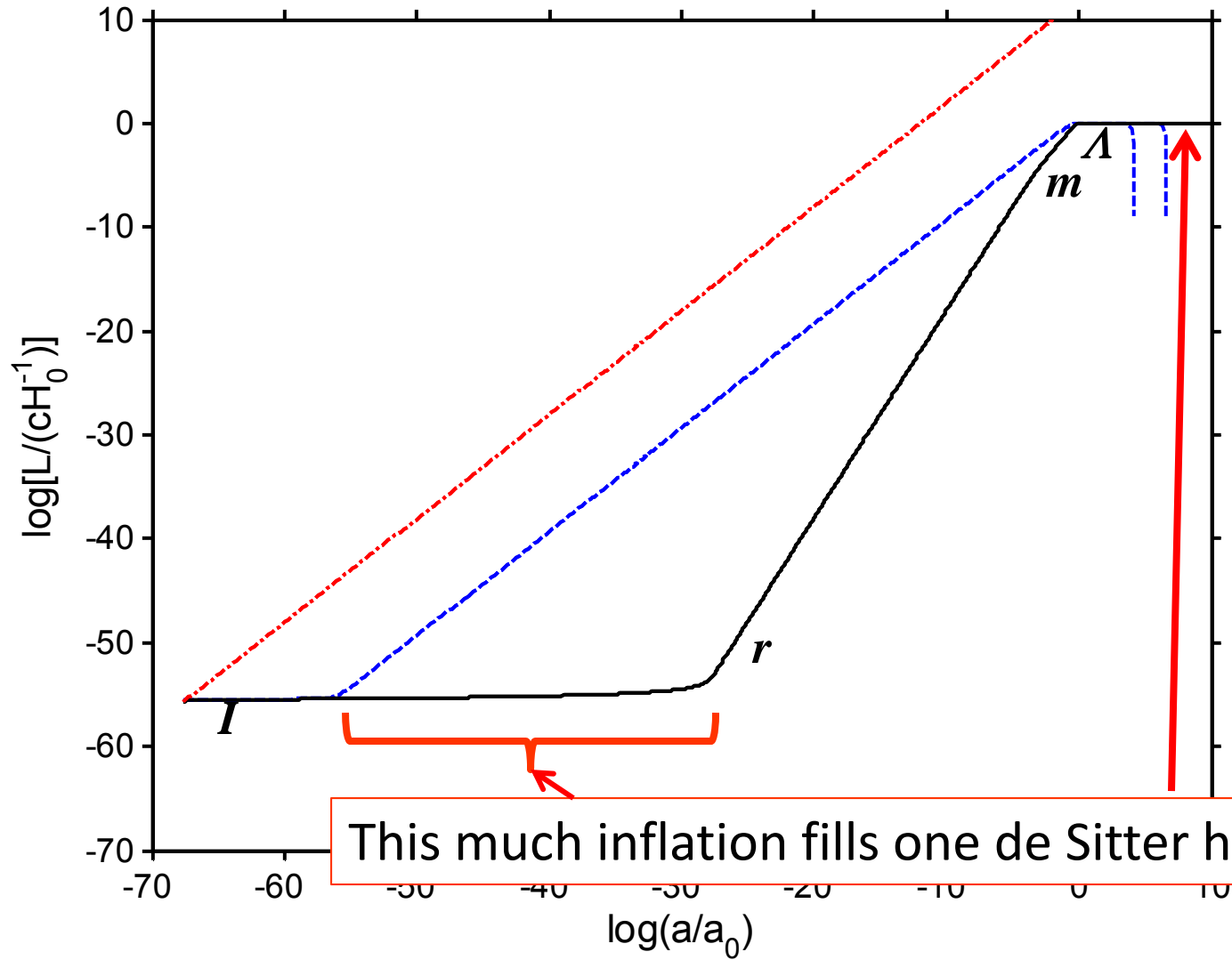


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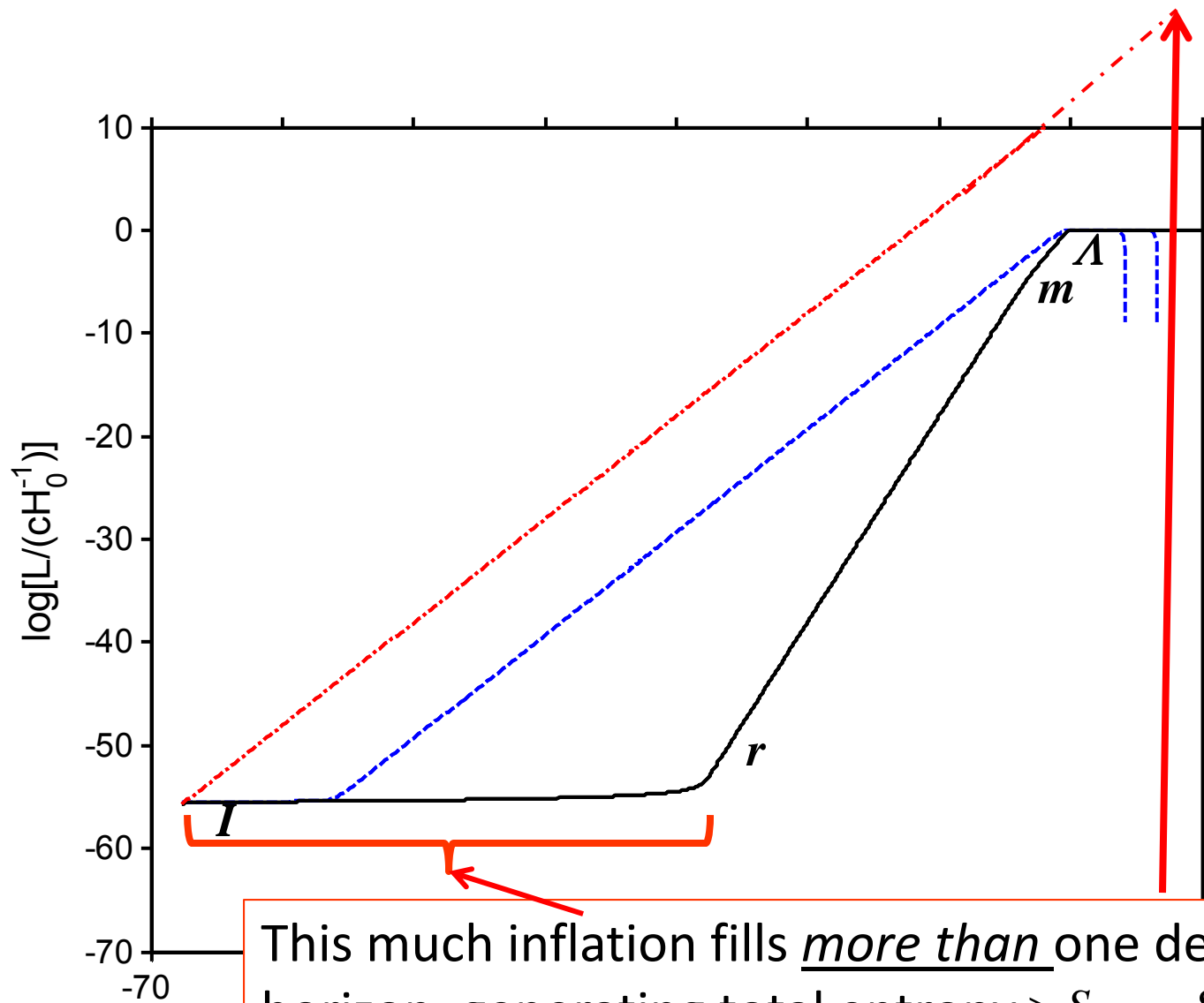
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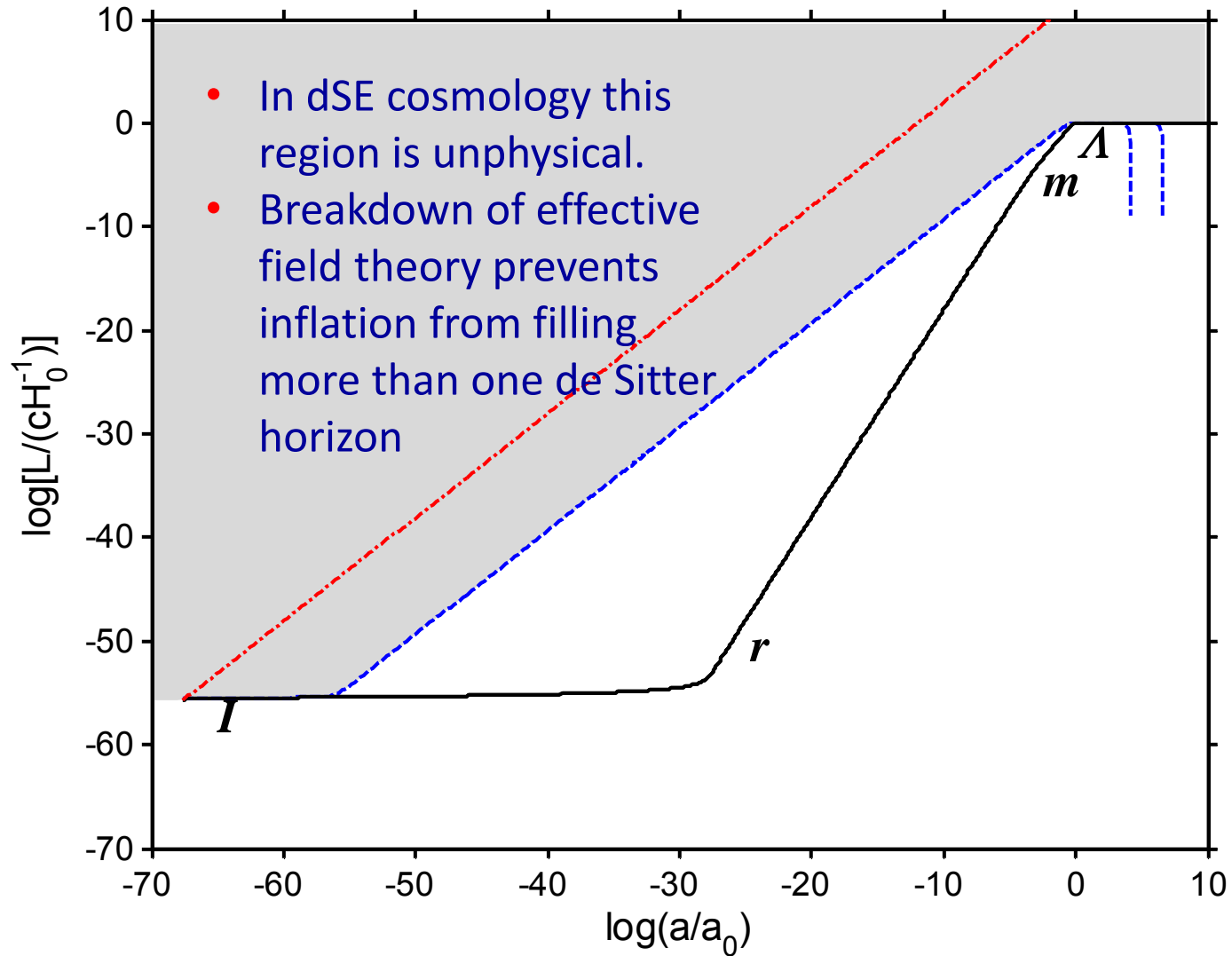


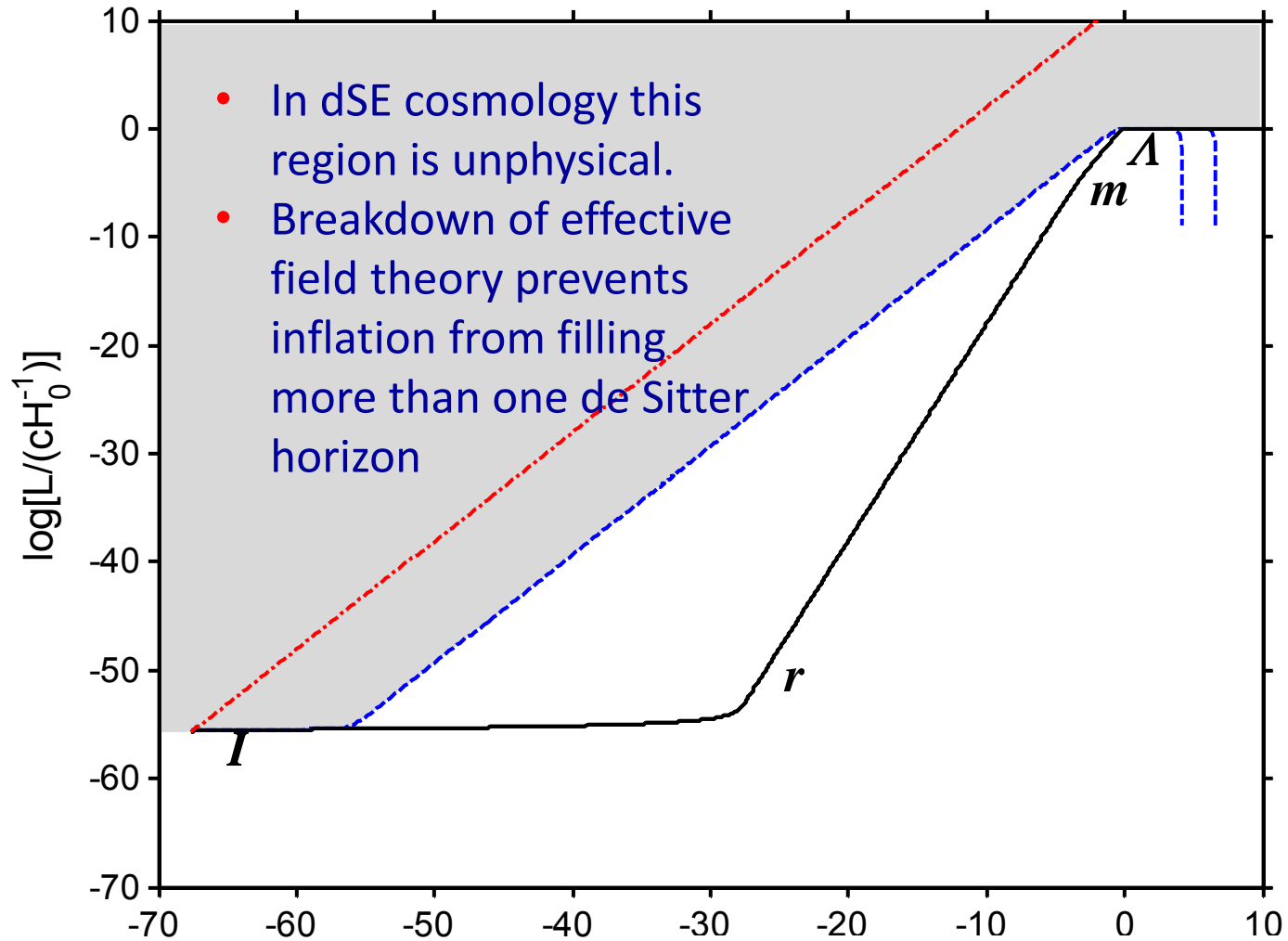


This much inflation fills one de Sitter horizon



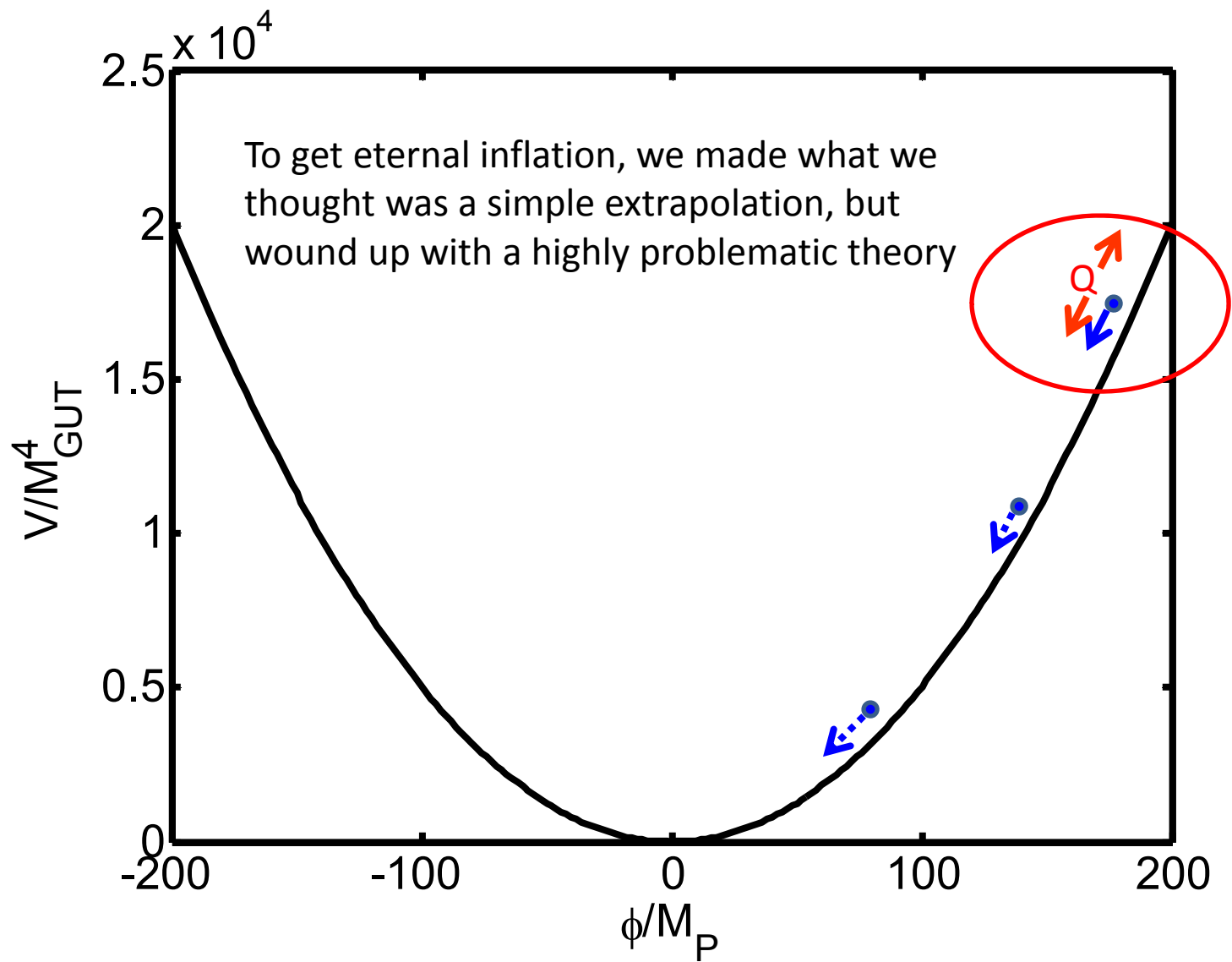
This much inflation fills more than one de Sitter horizon, generating total entropy  $> S_{Max} = S_{\Lambda}$  and affecting regions beyond the horizon of the observer

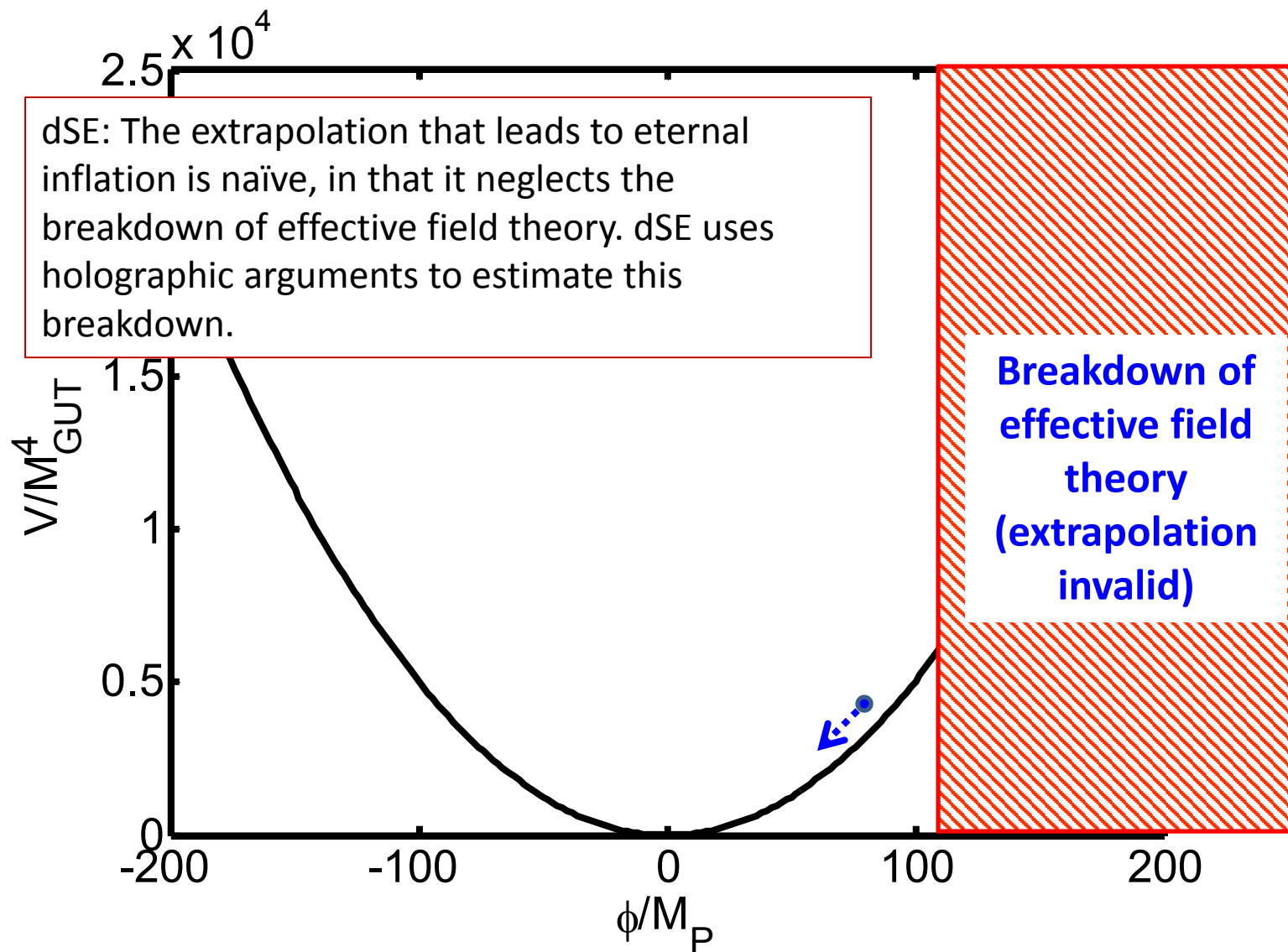




“Equivalent” to Banks-Fischler holographic constraint on number of e-foldings of inflation

Albrecht C (D Phillips & AA in prep)





dSE: The extrapolation that leads to eternal inflation is naïve, in that it neglects the breakdown of effective field theory. dSE uses holographic arguments to estimate this breakdown.

**Breakdown of effective field theory (extrapolation invalid)**

## Fluctuating from dSE to inflation:

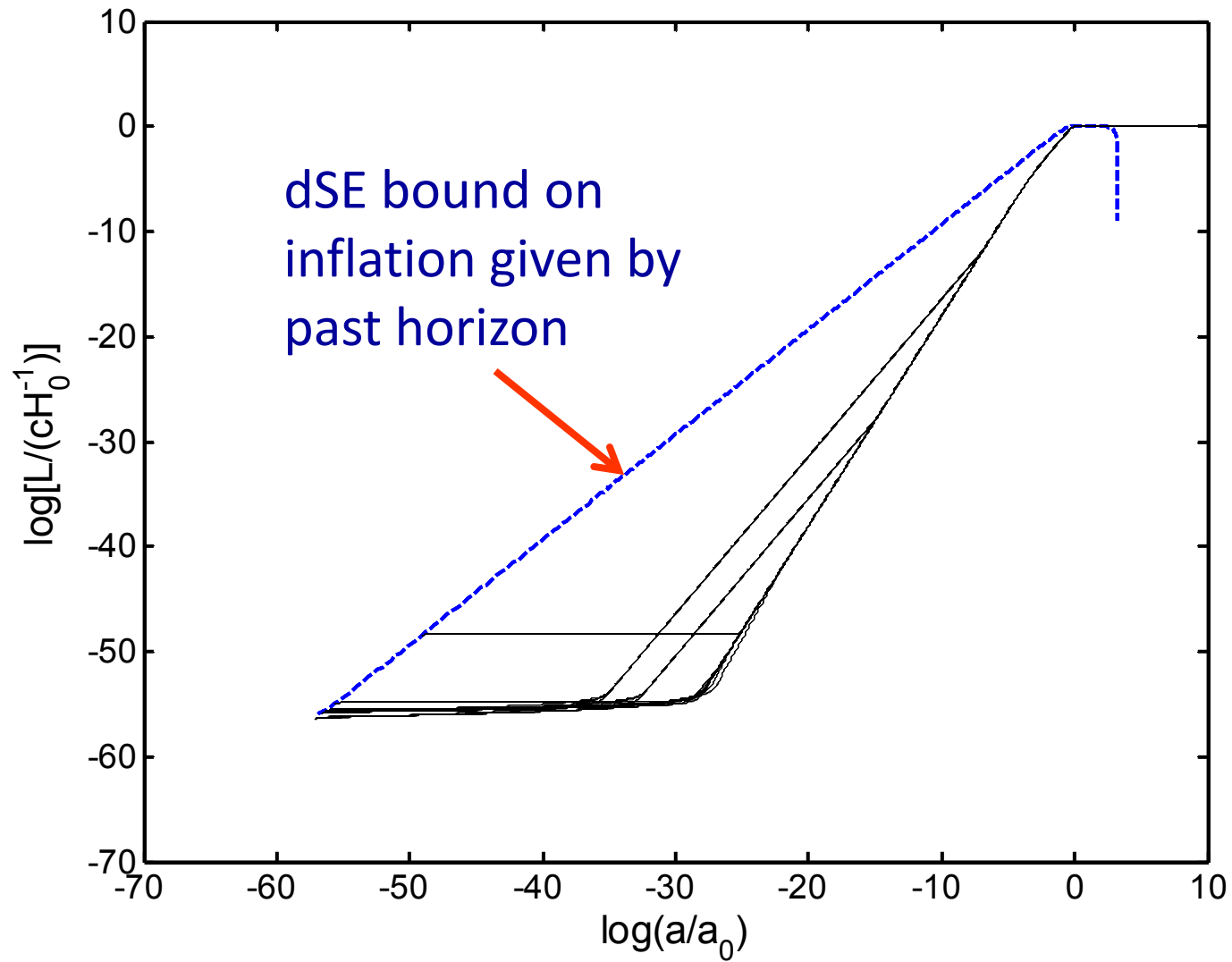
- The process of an inflaton fluctuating from late time de Sitter to an inflating state is dominated by the “Farhi-Guth Guven” (FGG) process
- A “seed” is formed from the Gibbons-Hawking radiation that can then tunnel via the Guth-Farhi instanton.
- Rate is well approximated by the rate of seed formation

$$\propto e^{-\frac{m_s}{T_{GH}}} = e^{-\frac{m_s}{H_\Lambda}}$$

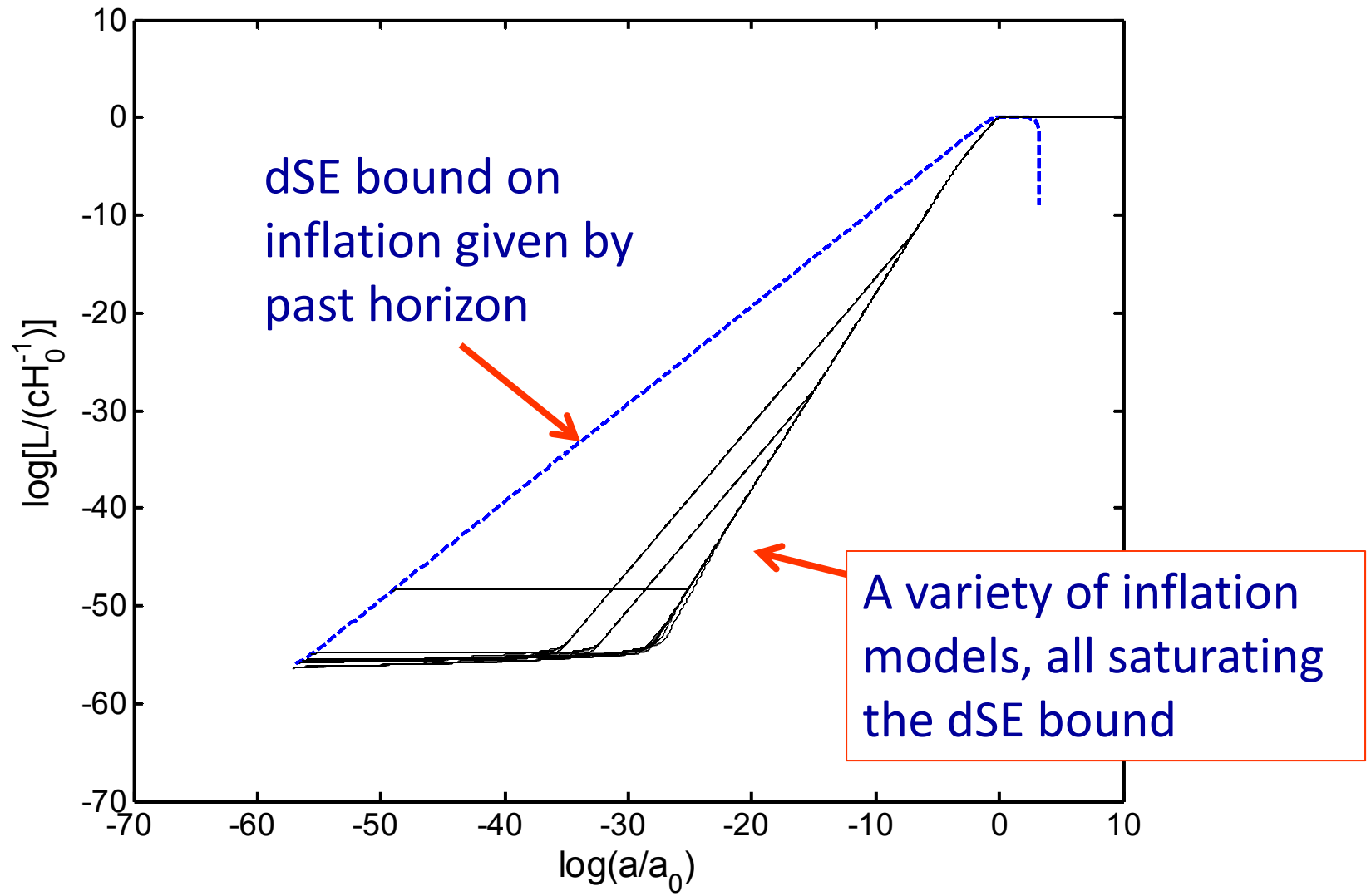
- Seed mass:

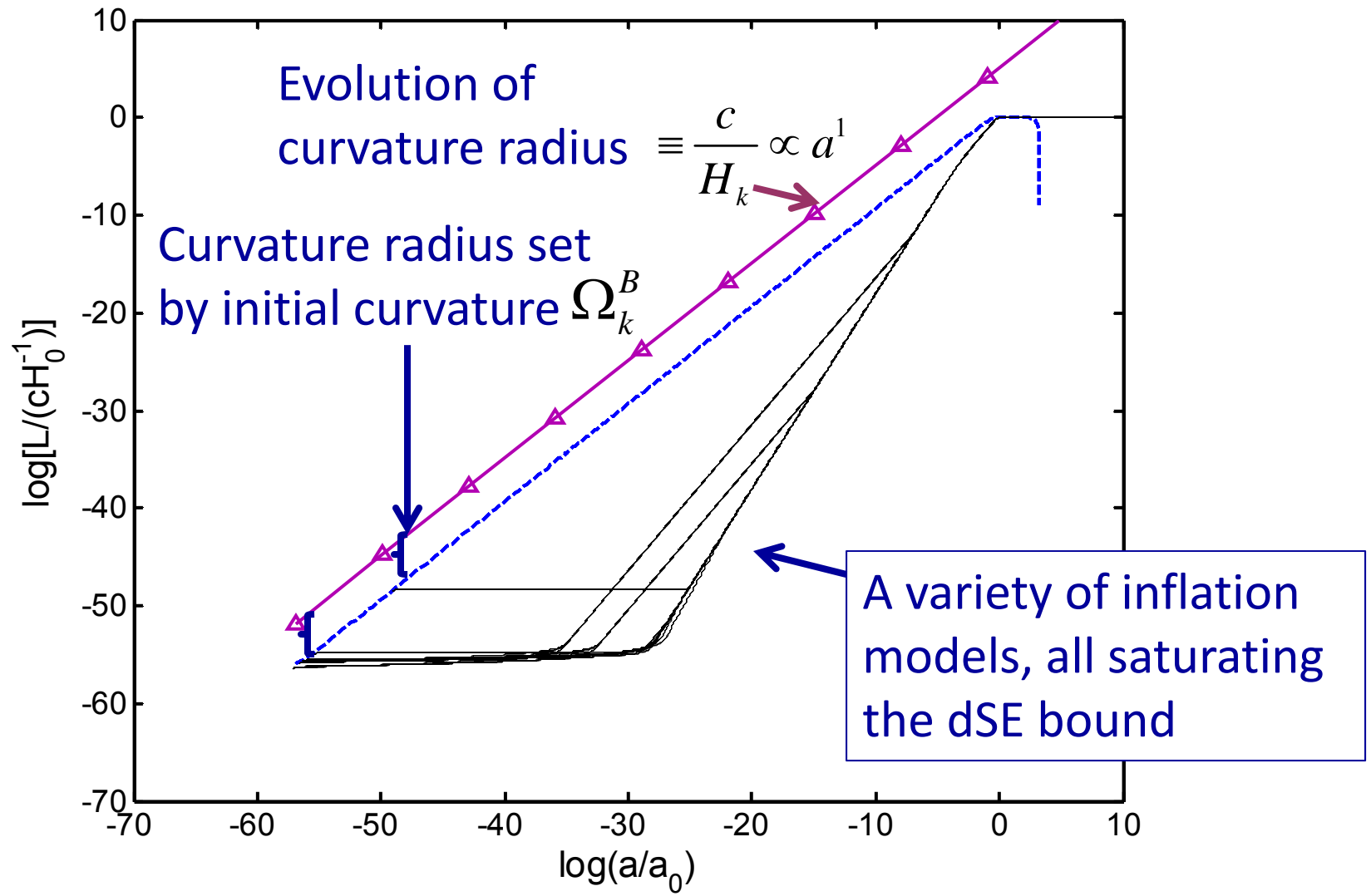
$$m_s = \rho_I (cH_I^{-1})^3 = 0.0013kg \left( \frac{(10^{16} GeV)^4}{\rho_I} \right)^{1/2}$$

Large  $\rho_I$   
exponentially  
favored  $\rightarrow$   
saturation of  
dSE bound

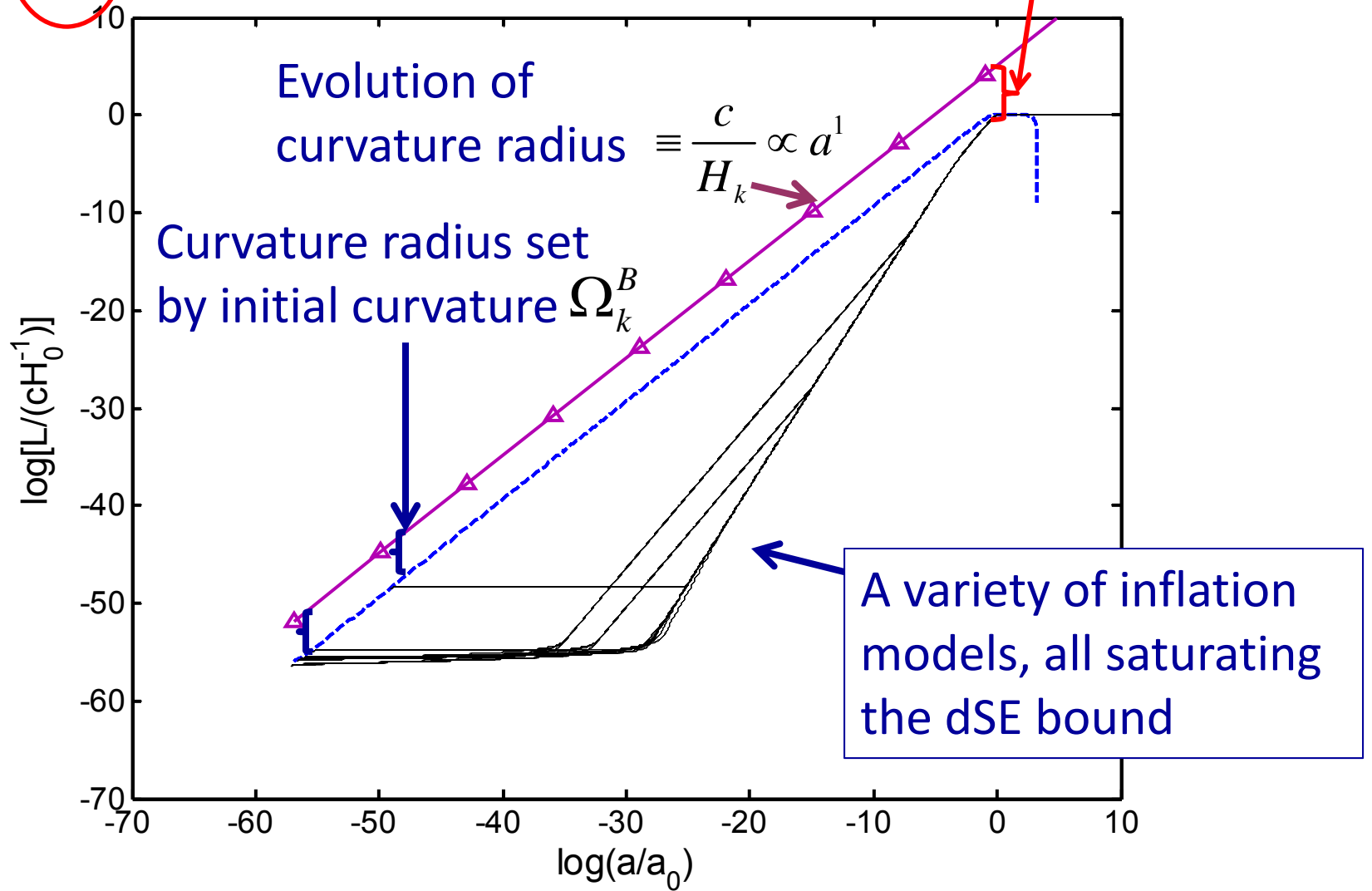


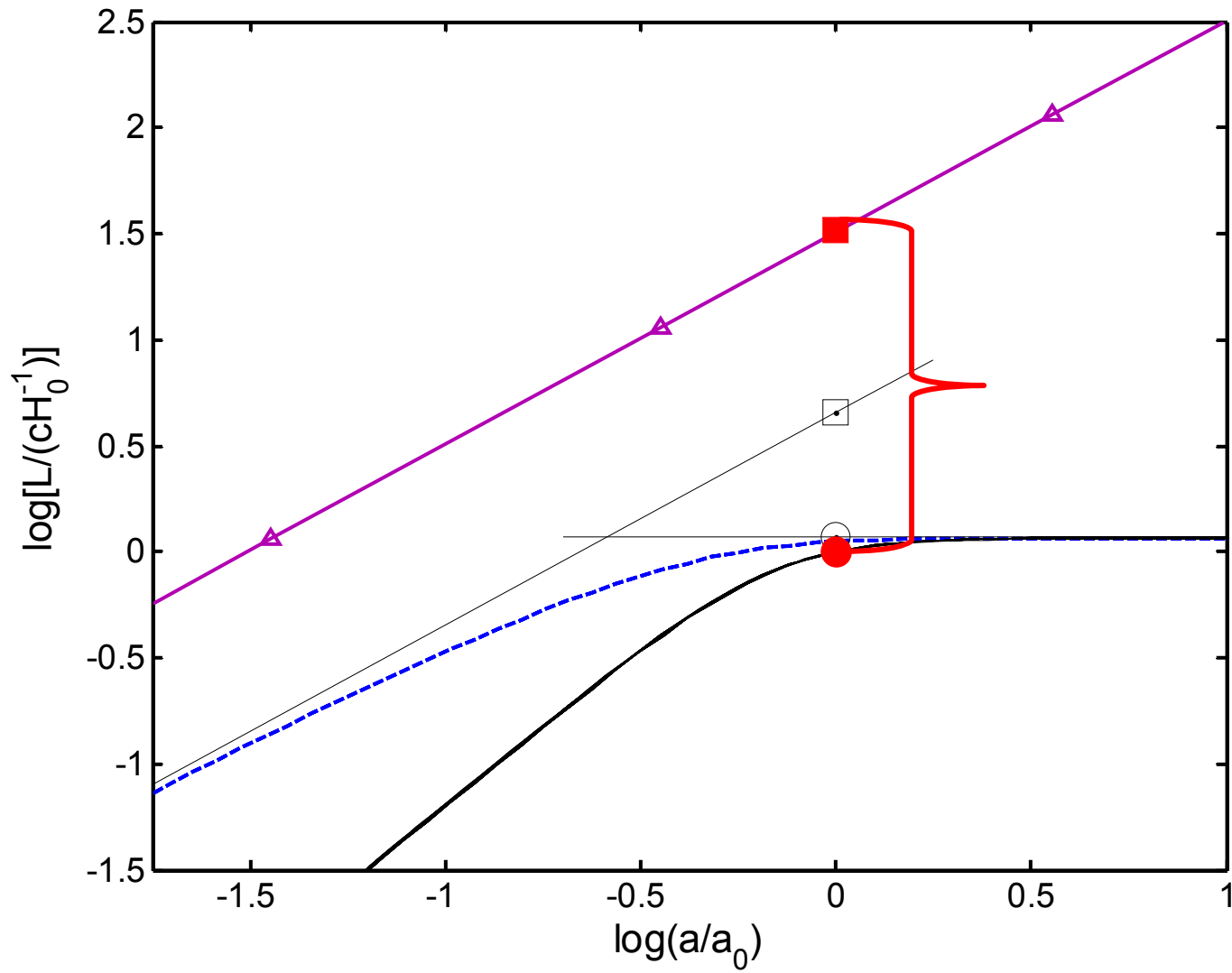






$\Omega_k \equiv \frac{\rho_k}{\rho_c} = \left(\frac{H_k}{H_0}\right)^2 \equiv \left(\frac{R_{H_0}}{R_k}\right)^2$  is given by this gap





AA: arXiv:1104.3315

## dSE Cosmology and cosmic curvature

- The Guth-Farhi process starts inflation with an initial curvature set by the curvature of the Guth-Farhi bubble  $\Omega_k^B$
- Inflation dilutes the curvature, but dSE cosmology has a minimal amount of inflation

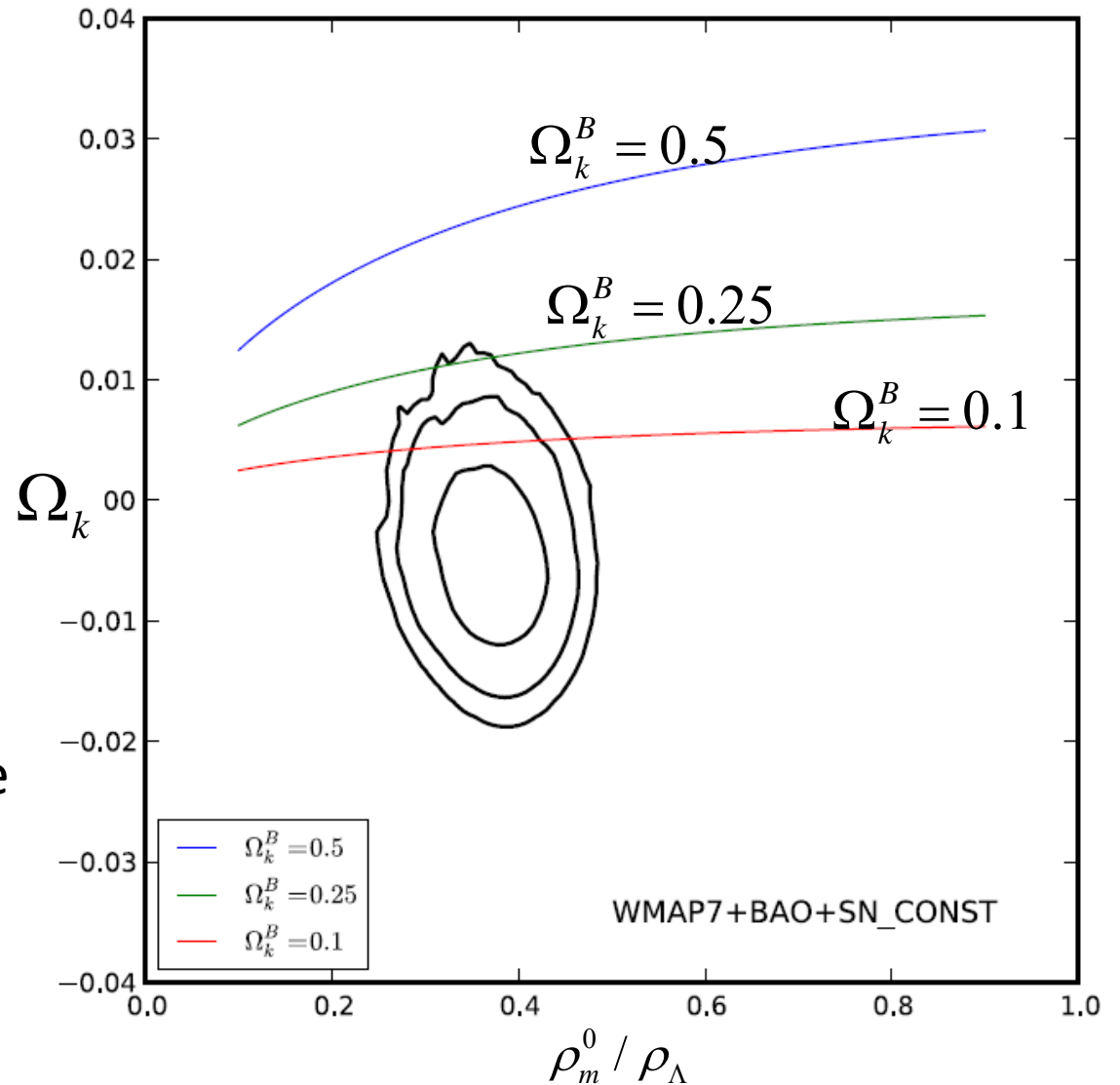
$$\Omega_k = \frac{1}{g^2} \frac{\Omega_k^B}{\left( \frac{\rho_m^0}{\rho_\Lambda} + \frac{\rho_k^0}{\rho_\Lambda} + 1 \right)}$$

where

$$g \left( \frac{\rho_m^0}{\rho_\Lambda}, \frac{\rho_k^0}{\rho_\Lambda} \right) \equiv \int_0^\infty \frac{dx}{x^2 \sqrt{x^{-3} \frac{\rho_m^0}{\rho_\Lambda} + x^{-2} \frac{\rho_k^0}{\rho_\Lambda} + 1}}$$

Predicted  $\Omega_k$   
from dSE cosmology  
is:

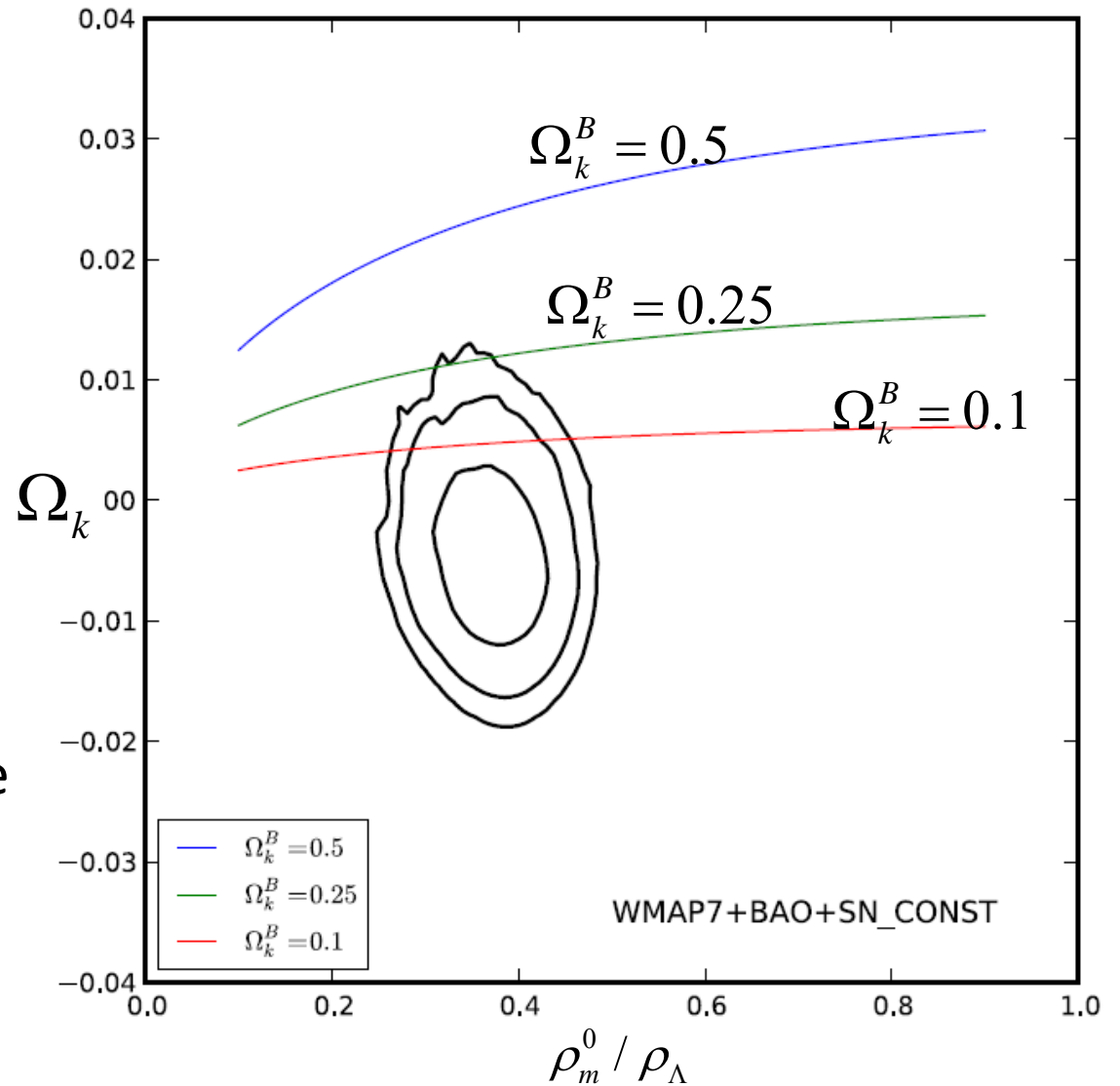
- Independent of almost all details of the cosmology
- Just consistent with current observations
- Will easily be detected by future observations



$$\Omega_k^B$$

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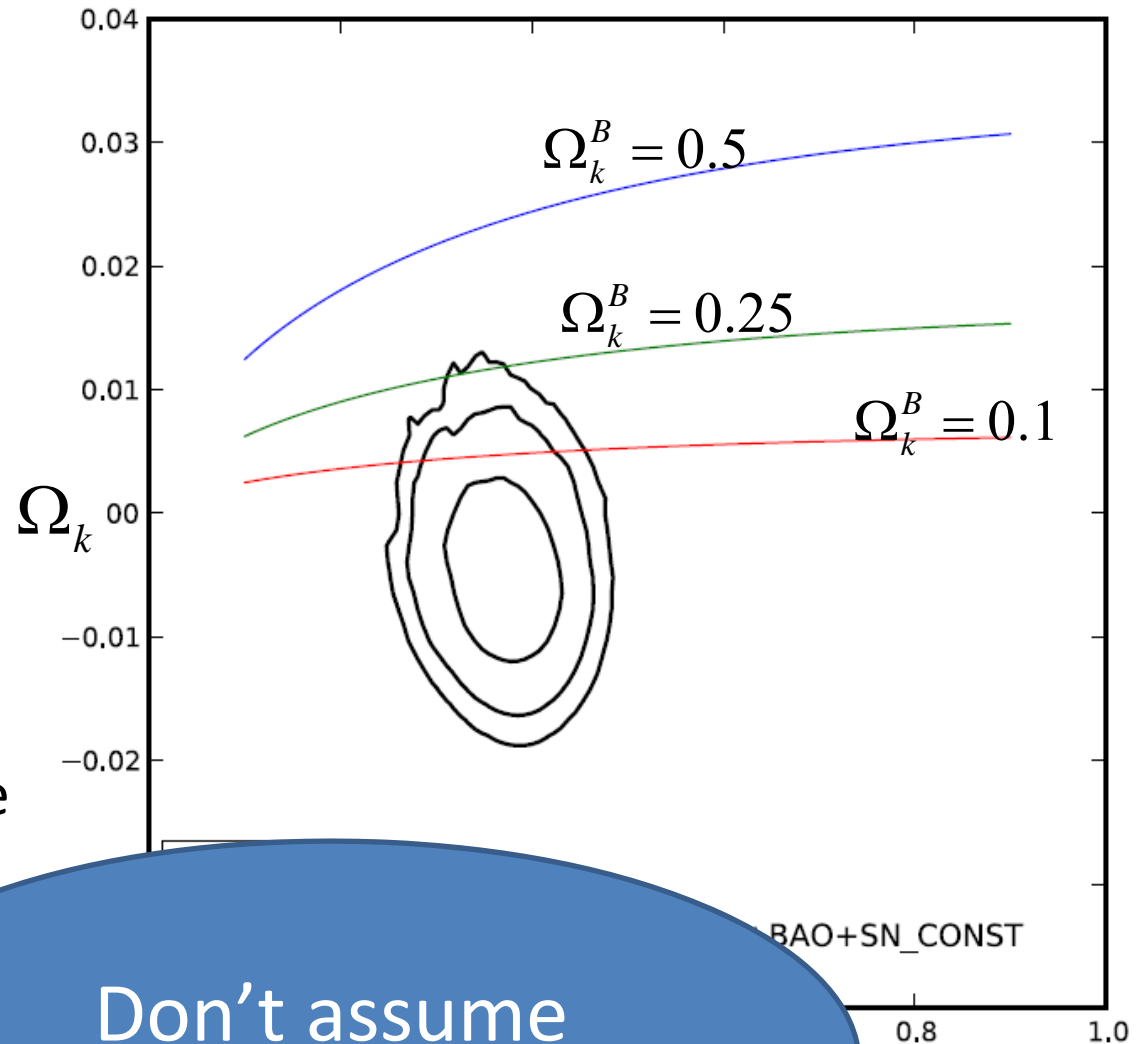
- **Independent of almost all details of the cosmology**
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$$\Omega_k^B$$

Predicted  $\Omega_k$   
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- **Independent of almost all details of the cosmology**
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Don't assume  
curvature = 0!


$\Omega_k^B$



## Outline

1. Introduction
2. Tuning & Entropy
3. Temporal Provincialism
4. Eternal Inflation, measures and probabilities
5. The Bunch Davies vacuum
6. de Sitter equilibrium cosmology ←
7. Conclusions

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## Concluding thoughts

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Starobinsky  
talk

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- 2) Questions of what went before, tuning, measures etc are tough ones. The ability of inflation theory (or any other theory) to provide deep insights into these is unclear.

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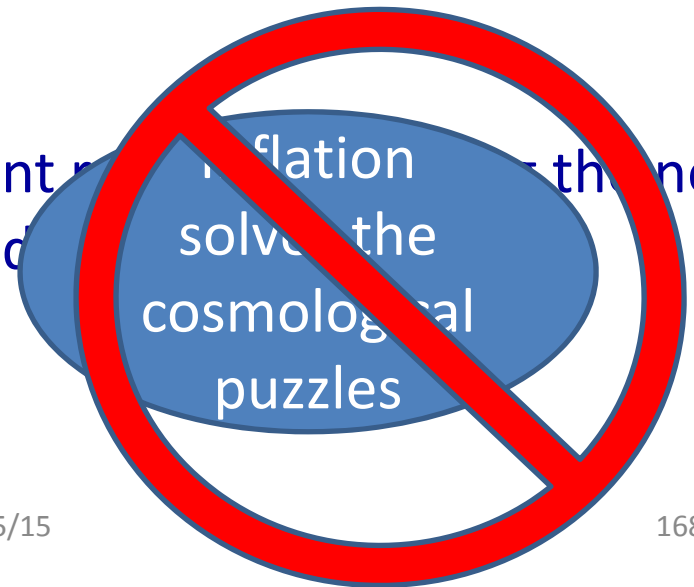
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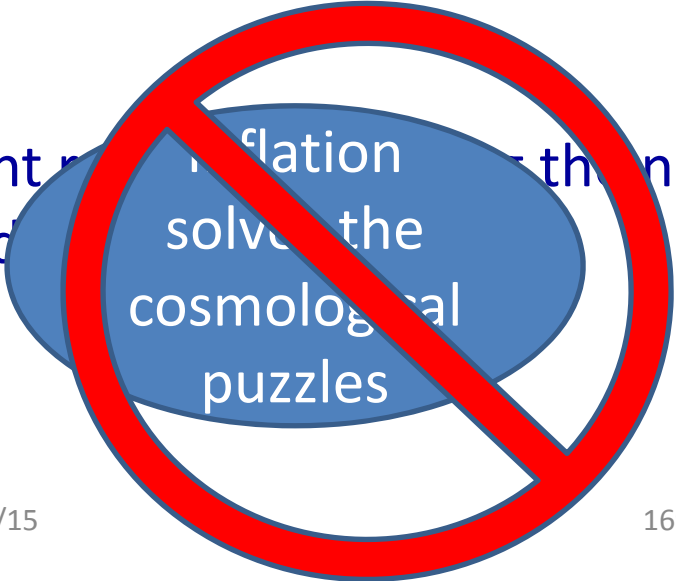
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inflation solve the cosmological puzzles

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- 4) These questions have an important role in stimulating the next level of progress in cosmology and fundamental physics.
- 5) Further progress will not be made using simply EFTs (thus dSE)

## How do ideas of dSE impact my research in practical terms:

- Search for finite quantum theory that looks approximately like de Sitter interior with finite thermal horizon (hard)
- Work on de Sitter equilibration
- Work on short inflation phenomenology.

1. *Transients in finite inflation*  
Andrew Scacco, Andreas Albrecht  
arXiv:1503.04872
  
3. *Holographic bounds and finite inflation*  
Daniel Phillips, Andrew Scacco, Andreas Albrecht (UC, Davis).  
Phys.Rev. D91 (2015) 4, 043513 arXiv:1410.6065
  
4. *Equilibration of a quantum field in de Sitter space-time*  
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5. *Cosmological Consequences of Initial State Entanglement*  
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Henry Stoltenberg, Andreas Albrecht (UC, Davis). Phys.Rev. D91 (2015) 2, 024004 arXiv:1408.5125
  
7. *Eternal Inflation with Arrival Terminals*  
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