Physics 262 Early Universe Cosmology

Homework 2

Assigned Jan 17

Due Jan 25

2.1) Using formulas from the FRW handout, consider a model for the total density of they Universe given by

$$\rho(a) = \rho_r(a) + \rho_m(a) + \rho_{\Lambda}(a) \tag{1.1}$$

where subscript "r" refers to relativistic matter, "m" refers to non-relativistic matter and " Λ " refers to "cosmological constant matter".

Produce an expression for $\rho_i(a)$ for each of the above ρ_i 's. Please use the convention that a = 1 today and use

$$\rho_m(1) = 0.28\rho_c(1) \tag{1.2}$$

$$\rho_{\Lambda}(1) = 0.72 \rho_{c}(1) \tag{1.3}$$

and use $\rho_r(1)$ given by the density of a photon gas at 2.7K. You my choose any units (correct for density) but please use the same units for all three! Use the value $H_0 = 65km/s/Mpc$.

Hints:

- 1) Many of the numbers you need can be found in the appendices of K&T 2) There is a small inconsistency with the above set of assumption at the ~0.001% level which you might not even notice. But if you do, ignore it. We will come back to it later.
- **2.2**) Plot $\log(\rho_i)$ vs $\log(a)$ for $i=r,m,\Lambda$. Please plot all three curves on the same plot. Take a in the interval $(10^{-6},1)$
- **2.3**) Find the values a_{eq} for which

$$\rho_r(a_{eq}) = \rho_m(a_{eq}) \tag{1.4}$$

and a_{Λ}

$$\rho_{m}(a_{\Lambda}) = \rho_{\Lambda}(a_{\Lambda}) \tag{1.5}$$

- **2.4)** Assuming the Universe is flat, Plot Ω_i vs $\log(a)$ for $i = r, m, \Lambda$ (all on the same plot, using the same range of a's as in problem 2.2)). Note: Please use a <u>linear</u> scale for the Ω axis.
- **2.5**) Integrate one of the equations from section 2 of the FRW notes to derive Eqn. 4.2 (from the same notes).